Variability in the timing of a β-catenin pulse biases a stochastic cell fate decision in C. elegans

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Summary

During development, cell fate decisions are often highly stochastic, but with the frequency of the different possible fates tightly controlled. To understand how signaling networks control the cell fate frequency of such random decisions, we studied the stochastic differentiation of the C. elegans P3.p cell, using time-lapse microscopy to measure the single-cell dynamics of key regulators of cell fate frequency. Strikingly, we observed that BAR-1/β-catenin, a key component in Wnt signaling, accumulated in a single, 1-4 hour pulse during the cell fate decision. Combining quantitative analysis and mathematical modeling, we found that the timing of the BAR-1/β-catenin pulse was a key determinant of the outcome of the cell fate decision. Our results highlight that timing of cell signaling dynamics, rather than its average level or amplitude, can play an instructive role in determining cell fate.

Keywords

cell fate; C. elegans; stochastic dynamics; single-cell dynamics; Wnt signaling; beta-catenin; pulses

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Introduction

During development, cells robustly obtain the correct cell fate to give rise to a viable adult organism, despite internal molecular noise and environmental variability. It is commonly assumed that suppressing this variability is essential for successful development. However, stochastic cell fate decisions, where cells randomly assume one cell fate out of a limited repertoire of different fates, is the cornerstone of many developmental processes (Johnston and Desplan, 2010). For example, the first cell fate decision in the mouse embryo, between trophectoderm and primitive endoderm fate, is stochastic (Zernicka-Goetz et al., 2009). Similarly, photoreceptor cells in the human retina randomly express either a red, green or blue photoreceptor gene (Roorda and Williams, 1999; Smallwood et al., 2002). In these stochastic decision processes, even though each individual outcome is random, the relative frequency of the different cells fates is often tightly controlled.

Currently, stochastic cell fate decisions are best understood in the context of single-celled organisms, where gene expression noise dominates as the key source of variability driving stochastic cell fate decisions (Balaban, 2004; Losick and Desplan, 2008; Maamar et al., 2007; Süel et al., 2006). However, it is unclear how stochastic cell fate decisions are regulated during animal development, as multicellular organisms pose unique constraints compared to single-celled organisms. Here, stochastic cell fate decisions have to be precisely coordinated with developmental timing, are potentially influenced by neighboring cells and rely on external, long-range signals mediated by a small number of key developmental signaling pathways. How these canonical signaling pathways drive stochastic cell fate decisions with strong control over cell fate frequencies is an open question.

Even though C. elegans development occurs in a largely invariant manner (Sulston et al., 1983), some cell fate decisions occur in a stochastic manner. One such decision is the specification of vulval precursor cell (VPC) competence group, beginning in the early in the L2 larval stage (Gleason et al., 2002; Myers and Greenwald, 2007). This group consists of six epidermal cells named P3.p-P8.p, which are subsequently patterned to various vulval cell fates by multiple signaling pathways (Eisenmann et al., 1998; Félix, 2012; Gleason et al., 2002; Gupta et al., 2012; Hill and Sternberg, 1993; Stemberg and Horvitz, 1986). The establishment of the VPC competence group is partly stochastic, as the P3.p cell assumes VPC fate in roughly 50% of wild-type hermaphrodites (Fig. 1a), while in the remainder, P3.p assumes hypodermal fate by fusing to a neighboring syncytial hypodermal cell, called hyp7 (Shemer and Podbilewicz, 2002; Stemberg and Horvitz, 1986). The exact cell fate ratio varies with environmental conditions and genetic backgrounds (Braendle and Félix, 2008; Pénigault and Félix, 2011a).

The Wnt pathway is a highly conserved signaling pathway that regulates many developmental events and cell fates (Clevers and Nusse, 2012; Hirabayashi, 2004; Hudson et al., 2013; Lindström et al., 2014; Mucenski et al., 2003; Ohyama, 2006). Previous investigations into the P3.p cell fate decision showed that its cell fate frequency is extremely sensitive to the dosage of Wnt ligands, particularly cwn-1, suggesting that variability in the ligand concentration
or in the response of the P3.p cell to Wnt ligands could provide the noise source driving the stochastic fate decision (Pénigault and Félix, 2011a, 2011b). In the canonical pathway, the presence of Wnt ligands leads to the accumulation of the transcriptional co-activator BAR-1/β-catenin, which co-regulates Wnt pathway target genes (Eisenmann et al., 1998; Korswagen, 2002; Korswagen et al., 2000; Sawa and Korswagen, 2013). In addition to the Wnt pathway, mutations in the C. elegans Hox gene lin-39 impact the Pn.p cell fate frequencies, by repression of cell fusion and promoting division of VPC fate cells (Clark et al., 1993; Koh et al., 2002; Maloof and Kenyon, 1998; Roiz et al., 2016; Shemer and Podbilewicz, 2002). Both Wnt signaling and LIN-39 inhibit hyp7/fusion fate, with loss-of-function mutants exhibiting increased frequency of cell fusion, including in the P4.p-P8.p cells that otherwise never assume hyp7/fusion fate (Gleason et al., 2006; Myers and Greenwald, 2007). However, what aspects of Wnt signaling and LIN-39 dynamics control the frequency of hyp7/fusion versus VPC fate in P3.p remains unknown.

Here, we use a novel time-lapse microscopy approach (Gritti et al., 2016) to observe gene expression and signaling dynamics in single Pn.p cells during specification of the VPCs, allowing us to directly connect variability during the decision process to the final cell fate outcome. Using this approach, we found that BAR-1/β-catenin accumulated in a single, ~1-4 hr pulse in the Pn.p cells at the time of the hyp7/fusion versus VPC fate decision, with strong variability in pulse slope and timing. Combining quantitative data analysis with mathematical modeling, we found that cell fate outcome depended strongly on the time of the BAR-1/β-catenin pulse onset, identifying the timing of Wnt signaling dynamics as a key control parameter of cell fate.
Results

Time-lapse microscopy of a stochastic cell fate decision

So far, whether P3.p undergoes fusion or assumes VPC fate in wild-type or mutant animals has been assessed only after the process has completed (Alper and Kenyon, 2001, 2002; Chen and Han, 2001; Eisenmann et al., 1998; Myers and Greenwald, 2007; Pénigault and Félix, 2011a, 2011b). To correlate early stochastic molecular events to eventual cell fate outcome it is essential to follow these processes directly in time. Here, we utilize a fluorescent time-lapse microscopy approach we developed recently to study single-cell dynamics inside moving and feeding C. elegans larvae for their entire ~40hr development (Gritti et al., 2016). We tested whether we could directly observe P3.p fusion events in single animals. We initially used two measures of cell fusion: first, imaging the apical junction protein AJM-1, which localizes on the apical edge of Pn.p cells but is degraded upon cell fusion (Brabin et al., 2011). Second, observing the flow of GFP from the hypodermis into the fused Pn.p cell, using animals carrying an extrachromosomal array targeting GFP expression to the hyp7 hypodermal syncytium. Initially the AJM-1::mCherry signal expanded along the A-P axis during the early L2 larval stage (Supplementary Movies 1-2, Fig. 1c). In animals with a fusing cell, this was followed by a sudden and pronounced ruffling of the AJM-1::mCherry signal and a rapid retraction of AJM-1::mCherry towards the posterior, with the fluorescent signal fully disappearing from P3.p within 1 hr (Fig. 1c). Inflow of GFP from the hypodermis into P3.p was observed as soon as AJM-1::mCherry retraction commenced (Fig. 1c,d), showing that both are accurate markers of (the time of) fusion. Because AJM-1::mCherry was more easily monitored, we used AJM-1 dynamics to establish fate and timing of P3.p fusion for all subsequent experiments.
Figure 1. **Stochastic cell fate decisions in Pn.p cells.**

(A) Overview of the hyp7/fusion versus vulva precursor cell fate (VPC) decision in the P(3-8).p cells. Cells assuming hyp7/fusion fate fuse (indicated by the dashed line) with the hypodermal syncytium hyp7 and lose the AJM-1 apical junction marker (green). Cell fusion requires the expression of the fusogen EFF-1 and is inhibited by the Hox protein LIN-39 and Wnt signaling through the β-catenin BAR-1. BAR-1 accumulation is induced by binding of Wnt ligands, such as CWN-1 (purple) to Wnt receptors (magenta).

(B) Measured hyp7/fusion frequencies in Pn.p cells in wild-type and mutant backgrounds. Mutants carried the ajm-1::gfp reporter except for lin-39(II) which carried ajm-1::mCherry. Wild-type animals carried either ajm-1::gfp (shown here) or ajm-1::mCherry (Supplemental Table S1), with no differences in fusion frequencies.

(C) AJM-1 dynamics in non-fusing (top) and fusing (bottom) P3.p cells carrying a nuclear dpy-7p:mCherry marker. Cell fusion occurred 6h20m after the start of L2, as shown by the appearance of GFP from the hypodermal syncytium hyp7 in P3.p (region enclosed by yellow line). Simultaneously, AJM-1 showed a pronounced ruffling, followed by its removal from P3.p. In contrast, no such AJM-1 dynamics was observed in non-fusing cells assuming VPC fate.

(D) Comparing GFP inflow from the hyp7 syncytium in fusing and non-fusing cells as a function of time after the start of the L2 larval stage. Shown is the ratio of GFP in P3.p to GFP in P4.p.
of GFP fluorescence intensity between P3.p and P4.p in the same animal, where P4.p never fused. The
blue and red line corresponds to the non-fusing and fusing cell in (C). Markers correspond to the time
points shown in (C). Arrow indicates the time of AJM-1 ruffling and coincides exactly with inflow of GFP
into the fusing cell. (E) Individual cell fusion times and box-and-whisker plots for P3.p (green) and P4.p
cells (magenta) in different genetic backgrounds. Fusion time was determined for AJM-1 dynamics and is
expressed as fraction of the L2 larval stage duration $T_{L2}$ (~8hrs for all backgrounds). Even though small,
but significant differences exist in average fusion time between strains (one-way ANOVA followed by
Student’s t-test, * indicates P<0.05), the full distributions show extensive overlap. (F) Distribution of
difference in cell fusion time between P3.p and P4.p cells, where both cells fuse (data pooled for all
genotypes with double fusions).

Even though changes to the frequency of P3.p hyp7/fusion versus VPC fate in mutants
are well studied (Alper and Kenyon, 2001, 2002; Chen and Han, 2001; Eisenmann et al., 1998;
Myers and Greenwald, 2007; Pénigault and Félix, 2011a, 2011b), it was not known how such
mutants impact the timing of this decision. We quantified the time of P3.p fusion in wild-type
animals and found that cell fusion occurred in a relatively narrow time window between 40-60%
of the L2 larval stage (Fig. 1f). We then examined mutants in which fusion frequency is
increased by removing inhibitory Wnt signaling or LIN-39 (Fig. 1b). We found that in these
mutants P3.p fusion occurred within the same time window as wild-type animals, with only small
differences between wild-type and mutant animals in average timing (Fig. 1f). Strikingly, even
though the exact time of fusion can vary as much as 2 hrs between animals, when multiple
VPCs fuse in a single animal, they typically do so at the same time (Fig. 1g). The observation
that, in the absence of key repressors of hyp7/fusion fate, cell fusion frequency is increased
independently of its timing provides evidence that a yet-unknown signal exists that activates cell
fusion at the appropriate time. In contrast, hyp7/fusion inhibitors (Wnt signaling, LIN-39) do not
control timing of fusion, but rather modulate hyp7/fusion versus VPC fate frequency.

Stochastic eff-1 induction precedes P3.p fusion

The most downstream regulator of the hyp7/fusion versus VPC fate decision is the gene
eff-1, a fusogenic protein whose expression is sufficient to induce cell fusion (Mohler et al.,
2002; Shemer et al., 2004). EFF-1 is a transmembrane protein that is required for most cell
fusions in C. elegans, and must be present on both the Pn.p and hyp7 plasma membrane to
induce fusion (Zeev-Ben-Mordehai et al. 2014; Smurova and Podbilewicz 2016). To understand
how cell fate frequency is regulated on the level of eff-1 expression, we counted eff-1 mRNA
molecules in Pn.p cells, using single molecule FISH (smFISH) (Raj et al., 2008). In wild-type
animals in the late L1 and early L2 stage (230 - 350 µm in body length), the stage of
development immediately preceding the hyp7/fusion versus VPC fate decision, we found that all
P3.p cells were unfused, as determined by the presence of the AJM-1 signal, and exhibited low
eff-1 expression in P3.p, <5 molecules (Fig. 2a,c), similar to the P4.p cell that always assumes
VPC fate in wild-type animals. However, in older, mid-L2 stage animals (350 - 395 µm in
length), corresponding to the time of fusion, we observed a subset of animals expressing ~30-
50 molecules in unfused P3.p cells, something not observed in P4.p (Fig. 2b-c). In fused P3.p
cells, we found similar number of eff-1 mRNA molecules located in close proximity to the cell
nucleus, suggesting that high eff-1 expression is maintained after fusion, before finally disappearing by the end of the L2 stage (Supplemental Fig. 1a,b). We confirmed that high eff-1 expression preceded cell fusion, rather than following it, by examining a temperature-sensitive loss-of-function point mutation in eff-1 (Mohler et al., 2002). Here, we still found high eff-1 mRNA levels in P3.p at the restrictive temperature, even as P3.p cell fusion was fully inhibited (Supplemental Fig. 1c).

![Diagram](image)

**Figure 2.** Stochastic eff-1 expression in Pn.p cells precedes cell fusion
(A), (B) Example of (A) low and (B) high eff-1 expression preceding cell fusion in wild-type animals of similar age, as determined by body length. Unfused cells with high eff-1 levels are rare, likely reflecting that such high expression levels rapidly lead to cell fusion. Single eff-1 mRNA molecules (red) were visualized using smFISH and nuclei with DAPI (blue). Unfused cells were selected based on AJM-1::GFP localization (green), with white brackets indicating intact apical junctions typical of unfused cells. (C) Panels (i) and (ii) show details of the P3.p cell region, corresponding to the area delineated by the dashed line in the panels in (A) and (B). (D) Number of eff-1 mRNA molecules in unfused P3.p and P4.p cells, for wild type animals and mutants with decreased (lin-39(++)) and increased (cwn-1(0)) cell fusion frequency. Late L1 and early L2 animals (230-350 µm body length) are at a developmental stage preceding the hyp7/fusion versus VPC fate decision, with fusion occurring only in mid-late L2 animals (350-400 µm body length). In wild-type animals, high eff-1 levels are found only in mid-late L2 stage in P3.p, but not P4.p, cells. In general, high eff-1 expression was observed more frequently with increasing average hyp7/fusion fate frequency (as indicated for P(3,4).p) and was observed in the P4.p cell only in the high-fusion frequency mutant cwn-1(0), where P4.p also exhibits fusion. The black percentage in each panel corresponds to the fusion frequency of that cell in the indicated genotype.

An interesting result is that the fraction of wild-type animals showing high (>20 molecules) eff-1 mRNA levels in P3.p was significantly smaller than the expected fraction of animals where P3.p assumes hyp7/fusion fate. For our analysis, we randomly sampled animals within the time window we expected fusion to occur. Given the observed variability in the time of
fusion (Fig. 1f), it is expected that some animals with low eff-1 expression would have ultimately fused at a later point. In particular, the fraction of animals observed with high eff-1 expression in unfused P3.p cells should increase with the average duration the cell expresses high eff-1 before this results in fusion. Hence, our results suggested that induction of high eff-1 expression was quickly followed by cell fusion.

To understand how eff-1 expression impacts cell fate frequency, we quantified eff-1 levels in a strain with a functional LIN-39::GFP insertion (lin-39(++) that caused low fusion frequency (~2% P3.p fusion frequency). Consistently, we no longer observed unfused P3.p cells expressing high (>20 molecules) eff-1 levels. (Fig. 2c). In contrast, in the cwn-1(0) mutant that lacks the dominant Wnt ligand and exhibited high (>80%) fusion frequency both in P3.p and P4.p, we found that the numbers of unfused cells observed with high eff-1 expression had increased substantially, most strikingly in P4.p (Fig. 2c). Together, this indicates that Wnt signaling and LIN-39 controlled cell fate frequency mainly by tuning the fraction of cells in which high eff-1 expression is induced.

Weak bias of cell fate decision by noise in LIN-39 protein level

The Hox transcription factor LIN-39 inhibits Pn.p hyp7/fusion fate by repressing eff-1 expression (Shemer and Podbilewicz, 2002), with lin-39 null mutations causing all Pn.p cells to fuse in the L1 larval stage (Clark et al., 1993; Wang et al., 1993). Hence, stochastic variability in LIN-39 protein levels could result in variability in induction of high eff-1 expression. It was shown previously that LIN-39 levels are similar between P3.p and P4.p in early L2 larval stage animals prior to cell fusion (Pénigault and Félix, 2011a), even though both cells have a different fate frequency (Fig. 1b). However, individual cells were not followed over time and linked to the eventual cell fate, and it is possible that small differences in LIN-39 between P3.p cells in different animals are sufficient to explain the outcome. To connect animal-to-animal variability in LIN-39 level with P3.p cell fate, we performed time-lapse microscopy on animals carrying an integrated low-copy lin-39::GFP translational fusion (Sarov et al., 2012) and ajm-1::GFP as a cell fusion marker (Fig. 3a,b). Since lin-39::GFP (lin-39(++)) is present as an insertion, it decreased the P3.p fusion rate from ~30% to ~2%, making it challenging to capture sufficient P3.p fusion events for analysis. For that reason, we further crossed this reporter into the cwn-1(0) mutant, increasing the P3.p and P4.p fusion rates to 20% and 14%, respectively.

We observed that LIN-39 was present in the P3.p nucleus at the start of the L2 larval stage and remained there for the entire larval stage when P3.p assumed VPC fate (Fig. 3a,c). However, in P3.p cells that fused, nuclear LIN-39 levels decreased rapidly after fusion commenced and fully disappeared within 90 mins (Fig. 3b,c), consistent with past observations of loss of LIN-39 in fused Pn.p cells (Pénigault and Félix, 2011a). LIN-39 levels were not significantly different in the cwn-1(0) mutant compared to wild type, further supporting the argument that LIN-39 and Wnt act independently in parallel pathways to repress eff-1 and cell fusion. We compared the distribution of LIN-39 levels, averaged over 3 hrs prior to fusion in P3.p cells that assumed hyp7/fusion fate with the distribution in P3.p cells that assumed VPC fate, averaged over 3hrs prior to the average time of P3.p fusion in this strain (Fig. 3d). We
found strong overlap between the two distributions, also when changing the size of the time window (data not shown), making it unlikely that fluctuations in LIN-39 levels are the main driver of stochastic eff-1 induction and cell fusion.

Figure 3. Variability in LIN-39 protein level.
(A), (B) Image sequence of a cell assuming (A) VPC or (B) hyp7/fusion fate. Nuclear LIN-39 levels are visualized using a LIN-39::GFP protein fusion, while cell fusion is determined using an ajm-1::GFP reporter. The red star indicates cell fusion has occurred. Times are relative to the start of the L2 stage (C).

Nuclear LIN-39 fluorescence in fusing (red) and non-fusing (blue) P3.p cells. For fusing P3.p cells, LIN-39 levels are variable prior to fusion (dark red) and fall rapidly after fusion (light red).

(D) Distribution of nuclear LIN-39 fluorescence in fusing (red) and non-fusing (blue) P3.p cells show strong overlap. In fusing cells, fluorescence was averaged over 3 hour window directly prior to fusion, whereas in non-fusing cells a time window of 3 hours prior to the average time of cell fusion was used.

(E) Nuclear LIN-39 fluorescence in P3.p (green) and P4.p (magenta) in an animal in which P3.p but not P4.p assumes hyp7/fusion fate. The arrow indicates the time window over which LIN-39 fluorescence is averaged in (D) and (F). The dashed line indicates the time of fusion.

(F) Nuclear LIN-39 fluorescence levels in P3p and P4.p for animals in which P3p assumes hyp7/fusion fate and the P4.p assumes VPC fate (green) or the reverse (magenta). Each marker corresponds to a single animal and is averaged over a 3 h time window prior to cell fusion. In general, LIN-39::GFP levels were lower in the cell that assumed hyp7/fusion fate.
These results leave open the question whether the observed variability in LIN-39 has any effect on the P3.p cell fate outcome. In lin-39::GFP; cwn-1(0) animals, P4.p also assumed hyp7/fusion fate in a stochastic manner, allowing us to test whether differences in LIN-39 levels between P3.p and P4.p are correlated with their eventual fate. First, we established that in this strain LIN-39 distributions for P3.p and P4.p were similar and also showed substantial overlap between fusing and non-fusing cells. We then selected animals in which one cell, either P3.p or P4.p, fused but the other assumed VPC fate (Fig. 3e). Indeed, in these animals absolute LIN-39 level was not predictive of the eventual fate of P3.p or P4.p, but we observed a significant correlation between fate and the difference in LIN-39 levels between P3.p and P4.p (Fig. 3f), with fusing cells having lower LIN-39 than their non-fusing neighbor cell (P = <0.01, Fisher’s Exact Test). This shows that noise in LIN-39 levels drives the hyp7/fusion versus VPC fate decision, but likely in conjunction with another noise source.

β-catenin activation dynamics during the cell fate decision

We next quantified activation of the Wnt pathway by monitoring the accumulation dynamics of BAR-1/β-catenin in a strain carrying a bar-1::GFP reporter. In the absence of Wnt ligands, β–catenin is continuously degraded by a degradation complex. Upon activation of Wnt receptors by Wnt ligands, activity of the degradation complex is stopped, allowing β-catenin to accumulate in the cell and nucleus (Sawa and Korswagen, 2013). In P3.p, the presence of BAR-1 is required to inhibit eff-1 expression and, hence, inhibit hyp7/fusion fate (Eisenmann et al., 1998). In contrast to β–catenins involved in the Wnt asymmetry pathway (Mila et al., 2015; Park and Priess, 2003), dynamics of BAR-1 during canonical Wnt signaling is poorly characterized. Here, we monitor BAR-1::GFP dynamics using an multi-copy integrated transgene, gals45, which rescues the bar-1(0) phenotype (Eisenmann et al., 1998) and has been used previously to study BAR-1 dynamics during male hook development (Yu et al., 2009). Similar transgenes have been used extensively to study the dynamics of the C. elegans β-catenins SYS-1 (Robertson et al., 2017) and WRM-1 (Kim et al., 2013). A disadvantage of using a multi-copy insertion is that the elevated BAR-1 level perturbed the observed P3.p fate frequency. However, a key advantage is its increased fluorescence signal, which is crucial for imaging its dynamics using our time-lapse imaging approach.

So far, Wnt ligand expression levels and its resulting spatial protein distribution are found to be largely constant in time (Coudreuse et al., 2006; Pani and Goldstein, 2018). Hence, we expected BAR-1 to show constant expression and dynamics in P(3-8).p cells, similar to LIN-39. Instead, we found that BAR-1::GFP levels were strikingly dynamic, with no BAR-1::GFP in P(3-8).p at the start of the L2 stage, followed by steady accumulation of BAR-1::GFP in P(3-8).p at the mid-L2 stage that lasted 1-4 hours and was strongly coordinated between cells (Supplemental Movie 3, Fig. 4a-c). After the accumulation phase, BAR-1 was rapidly degraded, with the overall dynamics of BAR-1 resembling a single pulse. The protein was detected in both the nucleus and cytoplasm. We found stochastic variability in the amplitude of the BAR-1 pulse between different Pn.p cells (Fig. 4b,c). It was speculated that P3.p, which is considered most distant to the source of Wnt ligands, receives a lower Wnt signal than P(4-8).p, thereby resulting in...
in its occasional hyp7/fusion fate (Harterink et al., 2011; Pénigault and Félix, 2011b). However, the BAR-1::GFP accumulation pulse in P3.p was frequently of similar or higher amplitude compared to the other Pn.p cells and, in general, we found no sign of a systematic spatial pattern in Wnt signaling. We also found significant variability in the amplitude and timing of the BAR-1::GFP pulse in the P3.p cell compared between different animals (Fig. 4d).

Figure 4. BAR-1 dynamics during cell fate decision.
(A) Image sequence of the BAR-1::GFP dynamics (green) over time in P3.p and P4.p cells in the same animal, with both cells assuming VPC fate. Animals also carry the ajm-1::mCherry marker (magenta).
(B),(C) Dynamics of cellular BAR-1::GFP fluorescence in P(3-6).p cells in two different animals. The animal in (B) corresponds to images in (A). Different cells show similar timing of BAR-1 pulse onset, but vary in amplitude. (D)-(F) BAR-1::GFP dynamics in non-fusing P3.p cells in (D) bar-1(++), (E) bar-1(++);lin-39(lf), (F) bar-1(++);cwn-1(0) animals. Traces for different animals are shifted along the vertical axis for clarity. Pulses show strong differences in time of onset and duration, even within the same strain. Traces run until the end of the L2 larval stage. Some bar-1(++);cwn-1(0) animals displayed significantly extended L2 stage duration (~15-20hr).
Since the BAR-1::GFP reporter is integrated as a functional multi-copy transgene, we expected this strain to act as a BAR-1 overexpression mutant and, indeed, observed no P(3-8).p cell fusions (Supplemental Table 1). Hence, we refer to this strain as bar-1(++)

To study how BAR-1 dynamics relates to cell fate frequency, we used different approaches to increase the frequency of hyp7/fusion fate. First, we decreased the level of the inhibitor LIN-39, using the lin-39(n709) temperature sensitive loss-of-function mutant (Supplemental Table S1). We found that bar-1(++);lin-39(lf) animals showed similar BAR-1::GFP dynamics (Fig. 4e). Interestingly, cells that fused always did so during the early accumulation phase of the BAR-1 pulse (Fig. 5a). Next, we sought to lower BAR-1 levels in the bar-1(++) background by decreasing activity of the Wnt signaling pathway, using the cwn-1(0) mutant that lacks the CWN-1 Wnt ligand (Fig. 1a). In these animals, BAR-1::GFP pulse amplitude was lower (Fig. 4f). In some bar-1(++);cwn-1(0) animals the L2 stage was significantly lengthened. Moreover, we found that BAR-1::GFP pulse occurred at significantly later times, as a fraction of larval stage duration, even in animals with a L2 larval stage duration similar to wild-type. Finally, the BAR-1 pulse also showed considerable variability in timing and amplitude in these mutants, and cell that fused always did so during the early accumulation phase of the pulse.

Variability in β-catenin dynamics

To characterize variability in BAR-1 accumulation dynamics, we used a minimal parameterization of the BAR-1 pulse shape to fit to the experimental data (Fig. 5a, Eq. 3 in Methods). Briefly, we assume that prior to the BAR-1 pulse, Wnt signaling is inactivated and BAR-1 is degraded. At pulse onset time \( t_0 \), Wnt signaling is activated, leading to inhibition of BAR-1 degradation and hence linear accumulation of BAR-1 in the cell. Linear BAR-1 accumulation continues for a pulse duration \( T \) in cells that assume VPC fate or until the time of fusion, \( t_{\text{fusion}} \), in cells that assume hyp7/fusion fate. Upon fusion BAR-1 vanishes immediately, as observed experimentally, whereas in cells that assume VPC fate, BAR-1 levels decrease exponentially once the pulse ends. This fitted the experimental data surprisingly well (Fig. 5a,b). Moreover, it allowed us to describe each BAR-1 pulse by three parameters: pulse onset time \( t_0 \), pulse slope \( s \) and pulse duration \( T \) for VPC cells or fusion time \( t_{\text{fusion}} \) for hyp7/fusion cells.

First, we compared the distribution of pulse onset time \( t_0 \) and linear slope \( s \) of each BAR-1 accumulation pulse between strains. We found that both were highly variable between animals in all strains (Fig. 5c,d). We found that the pulse parameters of bar-1(++) and bar-1(++);lin-39(lf) were similar, consistent with increase in hyp7/fusion fate frequency in this mutant resulting from the absence of the fusion inhibitor LIN-39 rather than changes in Wnt signaling. In contrast, we assumed that the increase in frequency of hyp7/fusion fate in bar-1(++);cwn-1(0) animals was due to a decrease in BAR-1 level. In the context of the observed BAR-1 pulse, this could be achieved in two independent ways, either by decreasing the slope \( s \) or by delaying the onset time \( t_0 \) of the BAR-1 pulse relative to the time of fusion (Fig. 6a,b). Given that BAR-1 accumulation is thought to be proportional to the amount of external Wnt ligands, we expected the cwn-1(0) mutant, that lacks the CWN-1 Wnt ligand, to have a decreased rate of BAR-1 accumulation. Surprisingly, we found that the pulse slope distribution was highly similar for bar-
1(++) and bar-1(++;cwn-1(0)) animals (Fig. 5c) and that the only different characteristic was the delayed pulse onset (Fig. 5d).

![Figure 5. Variability in BAR-1 dynamics.](image)

(A) Quantifying BAR-1 pulse dynamics. Markers are measured BAR-1::GFP levels in P3.p (green) and P4.p (magenta). Here, P3.p, but not P4.p, assumed hyp7/fusion fate. Solid lines represent a model of BAR-1 accumulation dynamics (Eq. 3 in Methods). Using the model, each BAR-1 pulse is described by three key parameters: pulse onset time $t_0$, pulse slope $s$ and pulse duration $T$ (for non-fusing VPCs) or time of fusion $t_{fusion}$ (for hyp7/fusion cells).

(B) Animals showing differences in (relative) timing of BAR-1 accumulation pulses. (C), (D) Distribution of (C) pulse slope $s$ and (D) pulse onset time $t_0$ in P3.p cells, in bar-1(++) (purple), bar-1(++;lin-39(If)) (orange) and bar-1(++;cwn-1(0)) mutants (green). $T_{L2}$ is the L2 larval stage duration. Strains differ in BAR-1 pulse onset time rather than pulse slope.

(E) Correlation in pulse onset time $t_0$ between P3.p and P4.p cells. Each marker corresponds to a P3.p and P4.p cell in a single animal where both assumed VPC fate. Arrows indicate the animals in (B). (F) Correlation between pulse onset time $t_0$ and pulse duration $T$ in non-fusing P3.p (circles) and P4.p cells (triangles). The dashed line is $T/T_{L2} = 0.66 - t_0/T_{L2}$. BAR-1 pulses that start later in the L2 larval stage have a shorter duration.

(G) Correlation between pulse onset time $t_0$ in a VPC and fusion time $t_{fusion}$ in a hyp7/fusion cell. Circles correspond to animals where P3.p, but not P4.p, assumed hyp7/fusion fate and triangles to animals where the cell fate assignment is reversed. The lines correspond to $t_{fusion}/T_{L2} = \Delta T + t_0/T_{L2}$, with $\Delta T = 0.2$ (orange) and $\Delta T = 0.1$ (green). The bar-1(++;cwn-1(0)) mutant has a shorter time delay $\Delta t$ between BAR-1 pulse onset and fusion.

We then compared the timing of the onset of BAR-1 accumulation between P3.p and P4.p cells. Both in bar-1(++) and bar-1(++;lin-39(If)) animals, considerable variability existed in
t₀, the time of the onset of the BAR-1 pulse, between these cells, with BAR-1 accumulation in P3.p preceding that in P4.p as often as the reverse (Fig. 5b,e). At the same time, pulse onset was correlated between P3.p and P4.p, meaning that if BAR-1 accumulation started late in the L2 larval stage in P3.p, it was also likely to start late in P4.p (Fig. 5e). Strikingly, we not only found that in the bar-1(++;cwn-1(0)) mutant the onset of the BAR-1 pulse was delayed, but also that the variability in pulse onset time between P3.p and P4.p was almost completely removed, with the onset of BAR-1 accumulation occurring in P3.p and P4.p within 20 min in all animals (Fig. 5e). This result suggests that the Wnt ligand cwn-1 not only controls the average onset of BAR-1 pulses, but also induces variability in pulse onset time between P3.p and P4.p.

We also observed variability in the duration of BAR-1 pulses when comparing the pulse in the same cell between animals (Fig. 5b,f). We examined whether the onset and the duration of the BAR-1 pulse was correlated. Because the duration of the L2 larval stage varied significantly between strains and animals, we examined the pulse onset time t₀/T₁₂ and duration T/T₁₂ relative to the duration of the larval stage, T₁₂. In this case, we found a striking anti-correlation, with late pulse onset resulting in shorter pulses (Fig. 5f). In fact, the data for all strains clustered along the line T/T₁₂ = 0.66 − t₀/T₁₂, consistent with a model in which the end of the BAR-1 accumulation occurs at 66% of the L2 larval stage independent of the BAR-1 pulse onset time. This correlation also held for the bar-1(++;cwn-1(0)) mutant, where not only the onset of the BAR-1 pulse was delayed but also the L2 larval stage was much extended. Hence, the BAR-1 pulse ended independent of its onset time t₀ in all mutants examined.

Given that we observed strong variability in pulse onset time relative to the time the pulse ceases (Fig. 5f), we asked whether the time of cell fusion was correlated with either the pulse start or end time. However, because cell fusion is immediately followed by rapid degradation of BAR-1, it was not possible to determine the pulse end time in cells that assumed hyp7/fusion fate. At the same time, P4.p cells often assumed hyp7/fusion fate in bar-1(++;lin-39(lf)) and bar-1(++;cwn-1(0)) animals. Therefore, we selected animals where one Pn.p cell, either P3.p or P4.p, assumed hyp7/fusion fate whereas the other assumed VPC fate. We then compared within the same animal the fusion time t_fusion in the hyp7/fusion cell with the pulse onset time t₀ (Fig. 5g) or the pulse end time t₀ + T (Supplemental Fig. 2) in the VPC. For bar-1(++;lin-39(lf)) animals, the time of fusion correlated most strongly with the pulse onset time (R=0.86, P3.p fusing only) rather than pulse end time (R=0.56). Specifically, the data clustered along the line t_fusion/T₁₂ = 0.2 + t₀/T₁₂, i.e. cell fusion occurs at a time 0.2T₁₂, or on average ~2 hrs, after the onset of the BAR-1 pulse. Because the bar-1(++;cwn-1(0)) mutant has the same pulse slope distribution as the bar-1(++) mutant (Fig. 5c), we examined whether the increased hyp7/fusion frequency in the bar-1(++;cwn-1(0)) mutant was due to a shorter delay between pulse onset and time of fusion. Indeed, we found that in bar-1(++;cwn-1(0)) animals the delay was halved, with cell fusion now occurring at a time 0.17T₁₂ after onset of the BAR-1 pulse (Fig. 5g). We found before that bar-1(++;cwn-1(0)) animals have a similar rate of BAR-1 accumulation as bar-1(++) (Fig. 5c). Delaying the pulse onset relative to the time of fusion would be an alternative mechanism to lower inhibitory BAR-1 levels.
Bias of cell fate decision by variability in β-catenin pulse timing

To elucidate the mechanism by which the dynamics of the BAR-1 pulse might impact eff-1 expression and cell fate frequency, we constructed a mathematical model of the cell fate induction network that takes into account variability in the BAR-1 pulse slope and timing (Fig. 6a-c, see Materials and Methods for details). In the model, hyp7/fusion fate requires sufficiently high eff-1 expression. We assumed that an activator controls the timing of cell fusion in the absence of the fusion inhibitors BAR-1 and LIN-39, consistent with our observations in Fig. 1f. In contrast, BAR-1 and LIN-39 then modulate cell fate outcome by inhibiting eff-1 expression. Specifically, eff-1 expression is induced only when the activator, but not BAR-1 and LIN-39 are bound to the eff-1 promoter (Fig. 6a). Here, BAR-1 is expected to control eff-1 expression in a complex with the Wnt effector POP-1 (Korswagen et al., 2000). In the model, we assumed that the activator is only present from time $t_{\text{fusion}}$ at a level $c_a$ (Fig. 6b). Also, we assumed that the level of the inhibitor Wnt signal, $c_W(t)$, followed the observed BAR-1 dynamics, rising from the pulse onset time $t_0$ with linear slope $s$ (Fig. 6b). Finally, we assumed stochastic variability in activator level, pulse slope and time of pulse onset and fusion.

We constrained almost all model parameters by experimental data (See Materials and Methods) as follows: using experimentally measured correlations between i) pulse onset time in different cells and ii) pulse onset time and time of fusion in the same cell, we estimated the relative contributions of global and cell-specific variability in timing of pulse onset and cell fusion. Next, we fitted the observed distribution of pulse slopes by a Gaussian distribution (Supplemental Fig. 3a). Finally, we adjusted the parameters governing the action of LIN-39 and the activator to reproduce the observed hyp7/fusion frequency in the different strains (Supplemental Fig. 3e). For all mutants, the resulting model provided an excellent fit to the observed distributions of pulse onset time $t_0$ and slope $s$ (Supplemental Fig. 3a-d), the joint distribution of $t_0$ in P(3,4).p (Supplemental Fig. 3f) and that of $t_0$ and fusion time $t_{\text{fusion}}$ (Supplemental Fig. 3g). In the model, the increased frequency of hyp7/fusion fate in $\text{bar-1}(++;)$; $\text{lin-39}(lf)$ animals was due to absence of LIN-39 increasing the range of activating and inhibitory signals $c_a$ and $c_W$ for which eff-1 is expressed sufficiently highly, whereas in the $\text{bar-1}(++;)$; $\text{cwn-1}(0)$ mutant, the reduced delay between $t_0$ and the time, $t_{\text{fusion}}$, when the activator becomes available causes lower inhibitory Wnt signals $c_W$ at $t_{\text{fusion}}$ (Supplemental Fig. 3e). We used the model to examine a hypothetical mutant that achieves the same hyp7/fusion frequency as the $\text{bar-1}(++;)$; $\text{cwn-1}(0)$ mutant, but by changing pulse slope rather than pulse onset time. We found that this mutant was clearly distinguishable from the $\text{bar-1}(++;)$; $\text{cwn-1}(0)$ mutant in terms of pulse slope distribution and delay between pulse onset and time of fusion (Supplemental Fig. 3b,g), providing further evidence that the change in pulse timing is the key reason hyp7/fusion fate is increased in the $\text{bar-1}(++;)$; $\text{cwn-1}(0)$ mutant.
Figure 6. Cell fate bias by variability in BAR-1 pulse timing.

(A) Mathematical model of hyp7/fusion versus VPC fate decision. eff-1 expression and, hence, hyp7/fusion fate is induced when the activator A, but neither BAR-1 (complexed with its co-activator TCF) nor LIN-39 is bound to the eff-1 promoter. LIN-39 is not shown as its level is constant in time. (B). Temporal dynamics in the model. The eff-1 expression level, $e(t)$ (red) as function of the dynamic activation level $c_a(t)$ (blue) and BAR-1 level $c_{BAR-1}(t)$ (green), which increases linearly from pulse onset time $t_0$. Cell fusion is activated at time $t_{fusion}$, but only occurs for high activation $c_a(t)$ and low inhibition $c_{BAR-1}(t)$, when eff-1 is expressed above a threshold level $e_{th}$ (dashed line). (C) In this model, fusion frequency can be changed both by changing the slope (left panel) and onset time (right panel) of BAR-1 pulses. (D), (E) Distribution of the difference in pulse slope $s$ for BAR-1 pulses in P3.p and P4.p, both for the (D) model and (E) experiments. Shown are distributions for bar-1(++) animals (black), where no Pn.p cells fuse, and bar-1(++;lin-39(0)) animals where P3.p, but not P4.p, fused (blue) or where neither P3.p nor P4.p fused (red). Fusing P3.p cells have a bias towards low pulse slope. (F), (G) Distribution of the difference in pulse onset time $t_0$ for BAR-1 pulses in P3.p and P4.p, both for the (F) model and (G) experiments. Color indicates the same scenarios as in (D). Fusing P3.p cells tend to have a delayed pulse onset. (H), (I) Comparing BAR-1 levels at the time of cell fusion between bar-1(++;lin-39(0)) (orange) and bar-1(++;cwn-1(0)) animals (green), both for the (H) model and (I) experiments. For the experiments, data for fusing P3.p and P4.p cells was pooled. The delayed BAR-1 pulse onset in bar-1(++;cwn-1(0)) animals (Fig. 5g) caused lower BAR-1 levels at the time fusion was initiated.
We next used the model to ask whether variability in BAR-1 pulse timing impacts the outcome of individual cell fate decisions, focusing on the \textit{bar-1(++)};\textit{lin39(lf)} mutant that produced most hyp7/fusion cells. We examined the difference in pulse slope and onset time in \textit{bar-1(++)};\textit{lin-39(lf)} animals, comparing animals where P3.p fused but P4.p assumed VPC fate with animals where both P3.p and P4.p assumed VPC fate. The model predicted that for animals where both cells assume VPC fate, the distributions of difference in pulse slope, and \(P\left(t_{0,p4.p}-t_{0,p3.p}\right)\), of difference in pulse onset time, are symmetrical (Fig. 6d,f, blue line). However, the model predicted a bias towards low pulse slope and late pulse onset time in fusing P3.p cells compared to non-fusing P4.p cells (Fig. 6d,f, red line), because both decrease the amount of inhibitory BAR-1. In agreement with the model, we found that the experimentally obtained distributions of difference in pulse slope and onset time between P3.p and P4.p were symmetrical, both in \textit{bar-1(++)} animals, where P(3,4).p never fuse, and \textit{bar-1(++)};\textit{lin-39(lf)} animals selected so that both cells assumed VPC fate (Fig. 6e,g, black and blue lines). However, in \textit{bar-1(++)};\textit{lin39(lf)} animals where P3.p, but not P4.p, assume hyp7/fusion fate, we found a weak bias towards lower pulse slope in P3.p and a significantly stronger bias towards delayed BAR-1 pulse onset in fusing P3.p cells compared to non-fusing P4.p cells (Fig 6e,g, red line), with only one animal with a fusing P3.p cell showing BAR-1 accumulation in P3.p prior to P4.p. This difference was particularly striking compared to the \textit{bar-1(++)} strain, which otherwise showed no difference in relative timing of BAR-1 pulse onset between P3.p and P4.p relative to \textit{bar-1(++)};\textit{lin-39(lf)} animals (Fig. 5c).

Even though the above results indicated that BAR-1 pulse timing biased the hyp7/fusion versus VPC fate decision, it left open whether variations in pulse timing achieve this by specifically modulating BAR-1 levels at the time the decision to fuse or not is made. The model predicted that at the time of fusion cells assuming hyp7/fusion fate in \textit{bar-1(++)};\textit{cwn-1(0)} mutants should have lower BAR-1 levels than fusing cells in \textit{bar-1(++)};\textit{lin-39(lf)} mutants, where fusion frequency is instead increased by removing the inhibitor LIN-39 (Fig. 6h). Indeed, when we compared BAR-1::GFP fluorescence at the time of cell fusion in \textit{bar-1(++)};\textit{lin-39(lf)} and \textit{bar-1(++)};\textit{cwn-1(0)} animals, we found a bias towards lower BAR-1 levels in fusing P3.p and P4.p cells in the \textit{cwn-1(0)} background (Fig. 6i).

To further link BAR-1 levels to inhibition of cell fusion, we quantified \textit{eff-1} transcripts using smFISH in \textit{bar-1(++)} animals and indeed found a negative correlation: Pn.p cells with visible BAR-1::GFP had few \textit{eff-1} transcripts, while unfused Pn.p cells without BAR-1::GFP often showed high \textit{eff-1} levels (Supplemental Figure 4). Together, these results show that changes in the timing of BAR-1 accumulation pulses are a key determinant of the hyp7/fusion versus VPC fate decision, likely by impacting the BAR-1 level at the time of the decision.
Discussion

BAR-1/β-catenin pulse dynamics

Here, we combined a novel time-lapse microscopy approach with quantitative analysis and mathematical modeling to study, in developing C. elegans larvae, how the outcome of a stochastic cell fate decision is controlled by random variability in the dynamics of the underlying signaling network. Surprisingly, we found that BAR-1/β-catenin, a core component of the Wnt pathway, accumulated in Pn.p cells in a dynamic, pulsatile manner (Fig. 4) that was precisely timed to influence their stochastic choice between vulva precursor or hypodermal fate, with the latter fate inhibited by BAR-1/β-catenin. Moreover, we found that the timing of the BAR-1/β-catenin pulse was a key control parameter influencing the relative frequency of these two cell fates: first, we observed that the increase in hypodermal fate frequency in bar-1(++;cwn-1(0)) mutants, compared to that in bar-1(++) mutants, was not due to systematic changes in the slope of the BAR-1/β-catenin pulse, but rather to a systematic decrease in the time delay between the pulse onset and the time of the cell fusion event that defines hypodermal fate (Fig. 5). Second, in the bar-1(++;lin-39) mutant we found that Pn.p cells that assume hypodermal fate have a later pulse onset than those cells in the same animal that assume vulva precursor fate (Fig. 6). Experiments and modeling suggest that pulse timing influences the cell fate decision by changing the level of BAR-1/β-catenin, and hence the amount of inhibition of hypodermal fate, at the time that hypodermal fate and cell fusion are induced (Fig. 6). Overall, these results indicate that for the cell fate decision studied here, it is not the absolute BAR-1/β-catenin level per se, as is generally assumed, but rather the timing of its accumulation dynamics relative to other developmental events, that is a key factor determining the stochastic cell fate outcome. A similar method of regulatory control was seen in Saccharomyces cerevisiae, where proteins Msn2 and Mig1 regulated gene expression through the modulation of their relative pulse timing and overlapping expression over time (Lin et al., 2015).

Mechanism of BAR-1/β-catenin single pulse generation

A striking feature of the BAR-1/β-catenin pulse dynamics is their body-wide coordination: despite considerable differences in time of pulse onset, both between mutants (Fig. 5d) and between Pn.p cells within the same mutant (Fig. 5e), the pulse is otherwise synchronized between the multiple adjacent Pn.p cells (Fig. 4), with the time of the end of the pulse highly similar in all mutants (Fig. 5f). It is an important question how the BAR-1/β-catenin pulse is generated. BAR-1/β-catenin accumulation could be controlled by changes in the level of the Wnt ligands outside of the cell or rather by changes in the Wnt pathway components inside the cell, such as changes to Wnt receptor levels or presence/activity of components of the β-catenin destruction complex. We currently favor the latter hypothesis, since neuronal cells close to the Pn.p cells show BAR-1::GFP expression in the late L1/early L2 stage when Pn.p cells do not, with a significantly decreased BAR-1::GFP signal in those cells in a cwn-1(0) background. This suggests that Wnt ligands are already present and able to activate Wnt signaling at this time and position in the body. An important question is whether the observed pulse dynamics is
influenced by the elevated levels of BAR-1 in the reporter strain used. Most importantly, the absence of BAR-1::GFP prior to the pulse and its rapid disappearance directly afterwards showed that the increased bar-1 expression level was still sufficiently low to not overwhelm the destruction complex. Hence, if the BAR-1 accumulation pulse is controlled by the activity of the destruction complex, as is expected, BAR-1 should exhibit the same pulse dynamics under wild-type conditions.

Our observations differ significantly from the current model of Wnt signal propagation at a number of points. First, as ligand-activated Wnt receptors sequester and thereby inactivate the destruction complex that induces β-catenin degradation, it was expected that changing Wnt levels would predominantly impact the rate of β-catenin accumulation (Clevers and Nusse, 2012; Sawa and Korswagen, 2013). However, using the cwn-1(0) mutant we found that removing a Wnt ligand instead changed only the timing of the induced BAR-1/β-catenin pulse (Fig. 4, 5c,d), which is difficult to explain based on our current knowledge of the Wnt pathway. Particularly surprising is that loss of cwn-1 almost completely removed the variability in BAR-1/β-catenin pulse timing between adjacent Pn.p cells in the same animal (Fig. 5e). In absence of CWN-1, other Wnt ligands such as EGL-20 repress hypodermal fate, albeit at reduced efficiency (Pénigault and Félix, 2011b). Our results indicate that CWN-1 acts in a significantly more stochastic manner, either on the level of ligand/receptor interaction or the delivery of ligands to the Pn.p cells, than the other Wnt ligands in the body, even though it is the Wnt ligand expressed closest to the Pn.p cells (Eisenmann, 2005; Harterink et al., 2011). It was also suggested that cells respond to fold change rather than the absolute level of β-catenin (Goentoro and Kirschner, 2009). However, this is inconsistent with our observation that cell fate frequency is impacted by changes in timing of BAR-1/β-catenin pulse onset, which do not impact fold change, rather than changes in pulse slope (Fig. 5c,d). Moreover, we find higher levels of inhibitory BAR-1/β-catenin at the time of cell fusion in mutants that lack the parallel hypodermal/fusion fate inhibitor LIN-39 (Fig. 6i), another indication that absolute BAR-1/β-catenin levels control the frequency of hypodermal fate.

It is an open question how the decay of the BAR-1/β-catenin pulse is controlled in time. Negative feedback of the Wnt/β-catenin pathway has been shown to occur through the regulator Axin, which could be responsible for shutting off β-catenin accumulation (Jho et al., 2002). However, this negative feedback model implies that the end of the pulse would be tightly linked to the pulse onset, rather than occurring at a fixed point in the larval stage independent of the start of the pulse, as we observed (Fig 5f). We speculate, based on the link between the BAR-1/β-catenin pulse end time and the timing of the larval stage, that this aspect of pulse timing is regulated by the molting cycle. In particular, it has been shown that many genes show body-wide gene expression oscillations, peaking once every larval stage but at different phases (Hendriks et al., 2014). Some of these genes might be responsible for switching of BAR-1/β-catenin accumulation in all Pn.p cells simultaneously. Our data indeed suggested that a Wnt-independent timing mechanism is present, as the time of cell fusion was unperturbed in a bar-1(0) mutant (Fig. 1f). In general, our observations suggest that timing of BAR-1/β-catenin accumulation dynamic can be regulated both by Wnt-dependent signals and Wnt-independent developmental timing cues.
Role of β-catenin pulse dynamics in development

It is increasingly clear that many of the canonical metazoan signaling pathways control development using temporal information encoded in their dynamics (Levine et al., 2013; Shimojo et al., 2008). In particular, pulses in the output of signaling pathways have now been identified in vivo in a number of developmental systems. For example, a recent study showed that EGF signaling acts in a pulsatile manner in the VPCs, with signaling strength transmitted in the frequency of pulses instead of a continuous graded signal (de la Cova et al., 2017). Moreover, time-lapse imaging of oscillatory, rather than pulsatile dynamics of Notch and Wnt signaling during segmentation of mouse embryos showed that the relative phase of the two oscillations instructs the segmentation process by an unknown mechanism (Sonnen et al., 2018). In this study, Wnt signaling was monitored indirectly, using an Axin rather than a β-catenin reporter. So far, the dynamics of β-catenin accumulation have rarely been studied directly. Single pulses of β-catenin have been observed (Murphy et al., 2014, Kafri et al., 2016), although mostly in cell lines following exogenous application of Wnt ligands rather than in the natural context of the body. For all these studies, timing of the individual β-catenin pulse was not directly linked to a specific cell fate outcome.

It remains an open question what the advantage is of activating BAR-1/β-catenin as a pulse rather than the being present continuously like the parallel hypodermal fate inhibitor LIN-39 (Fig. 3). Our mathematical model indicates one potential advantage, namely that BAR-1/β-catenin pulsatile dynamics allows for pulse timing as an additional control parameter, next to BAR-1/β-catenin accumulation rate, to tune cell fate frequency (Fig. 6). Whether cells receive Wnt input is tightly controlled in space, e.g. by regulating Wnt receptor expression. Pulsatile dynamics could be a powerful mechanism to control precisely when cells respond to ligands in time. This might be particularly important because the same signaling pathways are used many times during development, sometimes even in the same cell, to control different developmental events. Reading out these signaling pathways only at particular time points would allow the reconfiguration of the pathway from executing one developmental decision to another. Interestingly, Wnt signaling is used in VPCs at the mid-L3 stage, ~10 hrs after the hypodermal versus VPC decision, to control the anteroposterior orientation of their asymmetric divisions (Green et al., 2008). Here, EGL-20 plays an important role, whereas BAR-1 and CWN-1 have a smaller contribution. The decay of the BAR-1/β-catenin pulse at the end of the L2 stage might be crucial to avoid temporal crosstalk between the outputs of the Wnt pathway as the VPCs transition from one process to the next.

In conclusion, we have shown here that β-catenin accumulation can be highly dynamic during development, with temporal information instructing development contained in its dynamics. Many (stochastic) cell fate decisions in organism from nematodes to humans are controlled by Wnt signaling and it will be interesting to see whether pulsatile β-catenin plays a similar role in biasing cell fate frequencies in those systems. The quantitative approach we employed here, combining in vivo time-lapse imaging of β-catenin dynamics with measurements...
of key dynamical parameters such as pulse slope and pulse timing, can provide a template for such future studies.
Materials and Methods

CONTACT FOR REAGENT AND RESOURCE SHARING

Further information and requests for resources and reagents should be directed to and will be fulfilled by the Lead Contact, Jeroen van Zon (j.v.zon@amolf.nl).

EXPERIMENTAL DETAILS

Strains

All strains were handled according to the standard protocol on Nematode growth medium (NGM) agar plates with OP50 bacteria (Brenner, 1974). Experiments were performed on L2 stage hermaphrodites. Strains were obtained from the CGC unless otherwise indicated.

The following mutations were used in this study:

LGII: cwn-1(ok546) (The C. elegans Deletion Mutant Consortium, 2012),
LGX: bar-1(ga80) (Eisenmann et al., 1998)

The following transgenes were used in this study:

ncIs13[ajm-1::GFP], (Liu et al., 2005),
sls11337[pCesY37A1B.5::GFP + pCeh361)] (MCKAY et al., 2003),
ouls20 [ajm-1::mCherry + unc-119+] (gift from Alison Woollard),
itts37[pie-1p::mCherry::H2B::pie-1 3'UTR + unc-119(+)] IV ,
stls10116[his-72(promoter)::his-24::mCherry::let-858 3'UTR + unc-119(+)],
stls10311[lin-39::TGF(3D3)::GFP::TY1::3xFLAG]
(Sarov et al., 2012),
gals45[pDE218(bar-1::bar-1::GFP)] (gift from David Eisenmann) (Eisenmann et al., 1998), and
stls10226[his-72p::HIS-24::mCherry::let-858 3' UTR + unc-119(+)] (Sarov et al., 2012).

The presence of the cwn-1(ok546) homozygous deletion was confirmed by nested PCR screening. The following primers were used: outer left ('5-TCGTTTCTGACATGGCTCAC-3'), outer right ('5-ACCCATCCTTTCCCAATCTC-3'), inner left ('5-ACCATCTTTCTCAATCTC-3') and inner right ('5-AGAATCTTCACACCGGG-3').

Time-lapse imaging

The microchamber size used in the study was 190 μm x 190 μm, with a depth of 10 μm and made as previously described and imaged with a custom time-lapse microscope (Gritti et al., 2016). Using an eyelash attached to a glass pipette, OP50 bacteria were used as “glue” to transfer eggs into the microchambers using M9 solution to keep the microchamber moist. A Nikon Ti-E inverted microscope with a large chip camera (Hamamatsu sCMOS Orca v2) and a 60 X magnification objective ( NA=1.4 oil immersion) was used for imaging. Transmission imaging was performed using an LED light source (CoolLED pE-100 615nm), while 488 and 561 nm fluorescence images were acquired using Coherent OBIS LS 488-100 and OBIS LS 561-100 lasers, respectively. Images were acquired in a temperature controlled room at 19° with a sample temperature of 22°. Exposure time was 10 ms and approximately 25 images were taken
with a z-distance of 1 μm. Images were taken every 20 min. Images were 2048 x 2048 pixels and saved in 16-bit TIFF format. Fusion times were determined by ajm-1::GFP localization and morphology.

**Quantitative Image Analysis**

For all experiments, transmitted light images were used to identify molt times. Custom Python scripts and ImageJ were used to quantitatively analyze the acquired images (Schindelin et al., 2012; Schneider et al., 2012). First, images to be used for quantitative analysis were corrected for uneven laser illumination in the following manner: flat field intensity for the particular experiment was obtained by imaging a uniformly fluorescent (488nm) testing slide, and averaging the result of 10 images. We divided each pixel's intensity value in the experimental images by the corresponding flat field pixel’s intensity, normalized to the median value of the entire flat field image. This normalization procedure corrects for position-dependent variation in light intensity due to the Gaussian profile of the laser beam. The region of interest was cropped at this time. Pn.p cells were manually identified by stereotyped nuclear position location and the domains of ajm-1::gfp/mcherry expression, if present. To measure LIN-39::GFP expression, a mask was manually drawn around the nucleus and the mean fluorescence intensity of the pixels within the mask was calculated. The z-slice closest to the center of the nucleus was used. A background fluorescence measurement for each image was obtained by creating a mask of the intranuclear space in a region near P3.p and P4.p along the axis of the ventral nerve cord. The mean background fluorescence value was then subtracted from the mean fluorescence value of the reporter for the same image. To measure BAR-1::GFP expression, a mask was manually drawn around the Pn.p cytoplasmic region using AJM-1::mCherry signal as a positional guide, with background corrections performed similarly as described above. For the Supplementary Movies, fluorescence images were computationally straightened and aligned, using the animal's body shape and position of the Pn.p cells as measured from the fluorescent markers.

**Single-molecule fluorescence in situ hybridization (smFISH)**

Probe design and smFISH hybridization to visualize eff-1 mRNA transcripts were performed as previously described (Huelsz-Prince and van Zon, 2017; Raj et al., 2008). Custom probes were designed against the exons of the eff-1 gene by utilizing the Stellaris® RNA FISH Probe Designer (Biosearch Technologies, Inc., Petaluma, CA). The probes were hybridized with the Cy5 dye (Huelsz-Prince and van Zon, 2017). The sequences of the oligonucleotide probes used in this study are listed in Supplementary Methods Table 1. Animals were collected by washing plates with M9 and were fixed in 4% formaldehyde in 1 X PBS for 45 min at room temperature. Fixed animals were permeabilized in 70% ethanol at least one night at 4°C. Subsequently, animals were incubated with the 0.5 μl probes overnight at 30°C in Stellaris® Hybridization Solution containing 10% formamide. The next day, animals were quickly washed two times with 10% formamide and 2 X SSC, followed by an incubation wash for 30 min at 30°C. DAPI was added at 0.01 μg/ml in a final incubation step for 20 min at 30°C. Animals were mounted in Glox Buffer with catalase and glucose oxidase, and images were acquired with a Nikon Ti-E inverted fluorescence microscope, equipped with a 100X plan-apochromat oil-immersion objective and an Andor Ikon-M CCD camera controlled by μManager software.
(Edelstein et al., 2014). Stacks of each animal were taken with a z-distance of 0.33 μm and approximately 30 images were taken per animal. Cy5 exposure time was 3 s, while DAPI and GFP exposure time were 100 ms and 500 ms, respectively. Animals were then imaged at 40X to determine their body length, which was measured using ImageJ by drawing a spline from the tip of the head to the end of the tail. smFISH images were analyzed with a custom Python script using techniques previously described (Raj et al., 2008). The ajm-1::gfp transgene was used to determine the cell fusion status. For Supplemental Figure 4, ImageJ was used to quantify GFP fluorescence in the Pn.p cellular region of P3-P6.p by selecting the slice most central to the nucleus. The cellular region was then manually outlined and the mean fluorescence value of the cellular region was quantified.

MODEL DETAILS
Parameterization and fitting of BAR-1::GFP dynamics

To fit the experimentally measured BAR-1::GFP dynamics, we assume the following minimal model of BAR-1 production and degradation:

\[
\frac{dc_{\text{BAR-1}}}{dt} = k_p - k_d \frac{1}{1 + \alpha S(t)} c_{\text{BAR-1}},
\]

where \(c_{\text{BAR-1}}\) is the BAR-1 level and \(k_p\) is the BAR-1 production rate. In the absence of Wnt signaling, \(S(t)=0\), the degradation complex degrades BAR-1 at a basal rate \(k_d\). However, in the presence of Wnt signaling, \(S(t)=1\), the degradation complex is inhibited (Eisenmann, 2005) and degradation occurs at a reduced rate \(\frac{k_d}{1+\alpha}\) with \(\alpha > 1\). In the model, we assume the BAR-1 pulse is generated by changes in Wnt signaling level \(S(t)\). In particular, we assume Wnt signaling is activated at a constant level \(S(t)=1\) starting at time \(t_0\) and ending at time \(t_0 + T\), where \(T\) is the pulse duration. For other times, Wnt signaling is not activated, \(S(t)=0\). These assumptions yield the following expression for the BAR-1 dynamics:

\[
c_{\text{BAR-1}}(t) = \begin{cases} 
\frac{k_p}{k_d} t < t_0 \\
\frac{k_p}{k_d} (1 + \alpha) - \alpha \frac{k_p}{k_d} e^{-k_d t - t_0} e^{-k_d (t - t_0 - T)} & t_0 \leq t < t_0 + T \\
\frac{k_p}{k_d} + \alpha \frac{k_p}{k_d} (1 - e^{-k_d (t - t_0 - T)}) e^{-k_d (t - t_0 - T)} & t_0 + T < t
\end{cases}
\]

For sufficiently long pulse duration \(T\), the BAR-1 level will reach a steady state \(c_{\text{BAR-1}} = \frac{k_p}{k_d} (1 + \alpha)\). However, in the experimentally obtained data we never observed BAR-1::GFP levels reaching a steady state before the end of the pulse. Instead, we found that BAR-1::GFP accumulation remained approximately linear throughout the full duration of the pulse. Indeed, when the pulse duration is sufficiently short or the Wnt-mediated inhibition of BAR-1 degradation is sufficiently strong, i.e. \((1 + \alpha) \gg k_d T\), the exponential term in \(c_{\text{BAR-1}}(t)\) for \(t_0 \leq t < t_0 + T\) reduces to an expression that linearly with time in linear fashion, giving rise to the following expression used to fit the experimental data:
\[ c_{\text{BAR-1}}(t) = \begin{cases} \frac{k_p}{k_d} & t < t_0 \\ \frac{k_p}{k_d} + \frac{k_p}{k_d} \frac{\alpha}{1 + \alpha} (t - t_0) & t_0 \leq t < t_0 + T \\ \frac{k_p}{k_d} + \frac{k_p}{k_d} \frac{\alpha}{1 + \alpha} T e^{-k_d(t-t_0-T)} & t_0 + T < t \end{cases} \] (3)

We fitted this expression to the experimental BAR-1::GFP data by least-square fitting, using the implementation of the Levenberg-Marquardt algorithm, as implemented in the Python function `scipy.optimize.curve_fit` (Eric Jones et al., 2001) and using \( k_p, k_d, \alpha, t_0 \) and \( T \) as fit parameters. We obtained these fit parameters for each Pn.p cell by independent fitting. For fusing cells, we fitted \( c_{\text{BAR-1}}(t) \) to the experimental data only for time points until the experimentally determined time of fusion, \( t_{\text{fusion}} \). We found that cell fusion always occurred before the end of the pulse, i.e. \( t_0 + T > t_{\text{fusion}} \) and, hence, \( T \) was not defined for fusing cells. In general, this fitting procedure provides good fits for most BAR-1::GFP trajectories, but fails to converge to a correct fit for trajectories with very low pulse amplitude or no apparent pulse. In that case, we assume \( c_{\text{BAR-1}}(t) = 0 \), with \( t_0 \) and \( T \) not defined. To characterize pulse dynamics for non-fusing cell, we compare pulse onset time \( t_0 \), pulse duration \( T \) and pulse slope \( s = k_p \frac{\alpha}{1 + \alpha} \). For fusing cells, pulse duration is not defined and instead we compare the time of fusion.

**Mathematical model of stochastic Pn.p cell fate decision**

**Wnt signaling and eff-1 expression.** The model is briefly summarized in Fig. 6A,B of the main text. We assume that Wnt signaling (through BAR-1) and LIN-39 inhibit eff-1 expression, whereas an activator A, whose identity is currently not known, induce eff-1 expression. BAR-1 likely controls eff-1 expression as a complex with the TCF/LEF transcription factor POP-1 (Korswagen et al., 2000). However, it is not known whether POP-1 and LIN-39 control eff-1 expression in Pn.p cells by binding directly to the eff-1 promoter, or whether they regulate the expression of other transcription factors that do. For simplicity, here we assume that these transcription factors bind directly and independently of each other to specific binding sites in the eff-1 promoter and control eff-1 expression in a combinatorial manner, with eff-1 production only occurring when the activator A, but not LIN-39 and the BAR-1/POP-1 complex, are bound (Fig. 6A in the main text). Assuming that transcription factor (un)binding is rapid compared to eff-1 expression dynamics, we have the following expression for eff-1 level \( e_i(t) \) in time:

\[ e_i(t) = \left( \frac{K_W^n}{K_W^n + [c_{\text{BAR-1},i}(t)]^n} \right) \left( \frac{K_L^n}{K_L^n + [c_{\text{LIN-39},i}]^n} \right) \left( \frac{[c_A,i(t)]^n}{K_A^n + [c_A,i(t)]^n} \right), \] (4)

where \( c_{\text{BAR-1},i}, c_{\text{LIN-39},i} \) and \( c_A \) are the level of BAR-1, LIN-39 and the activator A in cell \( i \), \( n \) is a Hill coefficient and \( K_B, K_L \) and \( K_A \) are the dissociation constants for the inhibition (BAR-1, LIN-39) and activation (A) of eff-1 expression, respectively. Here, we assume that BAR-1 and activator levels vary in time but LIN-39 levels remain constant (based on Fig. 3 in the main text). Moreover, we assume that the level of the BAR-1/POP-1 complex scales linearly with \( c_{\text{BAR-1}} \). To determine whether cell \( i \) assumes hyp7/fusion or VPC fate, we calculate the eff-1 level \( e_i(t) \) as...
function of \( c_{\text{BAR-1},i}(t) \) and \( c_A(t) \) using Eq. 4. If \( \epsilon_i(t) \) is larger than a threshold value \( \epsilon_{\text{th}} \) for any given time \( t \), cell \( i \) assumes hyp7/fusion rather than VPC fate. Based on the observed BAR-1 dynamics (Figs. 4 and 5 in the main text), we assume that the BAR-1 level increases linearly with slope \( s_i \) from the BAR-1 pulse onset time, \( t_0^i \), onwards, with the level at time of fusion, \( t_f^i \) given by:

\[
c_{\text{BAR-1},i}(t_f^i) = \begin{cases} 
  s_i(t_f^i - t_0^i) & t_f^i > t_0^i \\
  0 & t_f^i \leq t_0^i
\end{cases},
\]

For the dynamics of the activator, we assume \( c_{A,i}(t) = 0 \) for \( t < t_f^i \) and a positive constant value \( c_{A,i} \) for \( t \geq t_f^i \). We observe significant variability in the slope of the BAR-1 accumulation pulse (Fig. 5 in the main text). For that reason, we allow the pulse slope \( s_i \) in cell \( i \) to vary stochastically as:

\[
s_i = \langle s \rangle + \eta_s^i,
\]

where \( \langle s \rangle \) is the average slope and \( \eta_s^i \) is a white noise term that is intrinsic to cell \( i \), i.e. \( \langle \eta_s^i \rangle = 0 \) and \( \langle \eta_s^i \cdot \eta_s^j \rangle = \delta_{i,j}(\sigma_s)^2 \) where \( \delta_{i,j} \) is the Kronecker delta and \( \sigma_s \) is the standard deviation of the noise. Similarly, we assume variability in the level of the activator A:

\[
c_{A,i} = \langle c_A \rangle + \eta_A^i.
\]

Pulse and fusion timing. We experimentally observed variability in pulse onset time and fusion time that can impact the inhibitory BAR-1 level at the time of fusion and, hence, control the frequency of hyp7/fusion versus VPC fate. We assume that the pulse onset time in cell \( i \) is given by:

\[
t_0^i = \langle t_0 \rangle + \eta_0^c + \eta_0^i,
\]

where \( \langle t_0 \rangle \) is the average observed pulse onset time, \( \eta_0^c \) is a white noise term common to all cells in an individual animal and \( \eta_0^i \) is a white noise term that is intrinsic to each cell \( i \), i.e. \( \langle \eta_0^i \rangle = 0 \) and \( \langle \eta_0^i \cdot \eta_0^j \rangle = \delta_{i,j}(\sigma_0^c)^2 \). For the cell fusion time, we assume:

\[
t_f^i = \langle t_0 \rangle + \eta_0^c + \langle \Delta t_f \rangle + \eta_f^i,
\]

where \( \langle \Delta t_f \rangle \) is the delay between the average pulse onset time and the average time of fusion and \( \eta_f^i \) is a cell-intrinsic white noise term with standard deviation \( \sigma_f \). Equations 8 and 9 correspond to a picture where a common signal impacts the Pn.p cells at time \( t = \langle t_0 \rangle + \eta_0^c \) to trigger both the start of the BAR-1 pulse and, after a delay \( \langle \Delta t_f \rangle \), activation of cell fusion, but with added cell-intrinsic variability in the timing of both events.

Constraining model by experiments. We can constrain many of the model parameters using our experimental observations. For each mutant, we obtain the average pulse slope \( \langle s \rangle \) and standard deviation \( \sigma_s \) from the experimentally observed values, allowing us to approximate the
experimental observation with a Gaussian distribution with mean \( \langle s \rangle \) and standard deviation \( \sigma_s \) (Supplemental Fig. 3a,b). We calculate mean pulse onset time as the average of the mean onset time in P3.p and P4.p, \( \langle t_0 \rangle = \frac{1}{2}(\langle t_0^3 \rangle + \langle t_0^4 \rangle) \), i.e. the average of the mean pulse onset times observed in non-fusing P3.p and P4.p cells. For the variability in pulse onset time, we obtain estimates for the standard deviations \( \sigma_0^s \) and \( \sigma_0^{int} \) using the correlation function \( C_{i,j}^0 = \langle(t_i^1 - \langle t_i^1 \rangle)(t_j^1 - \langle t_j^1 \rangle)\rangle \). In particular, we calculated the standard deviation of the common noise from the cross-correlation between the pulse onset in P3.p and P4.p, \( (\sigma_0^c)^2 = C_{3,4}^0 \). Next, using Eq. 8, we calculated the standard deviation of the cell-intrinsic noise as \( (\sigma_0^{int})^2 = \frac{1}{2}(C_{3,3}^0 + C_{4,4}^0 - 2C_{3,4}^0) \). Using the estimated parameters, we obtained a good fit with the experimentally observed distribution of pulse onset time in P3.p (Supplemental Fig. 3c,d) and were able to reproduce the experimentally measured joint distribution of pulse onset time in P3.p and P4.p in Fig. 5e in the main text (Supplementary Fig. 3f). Fusing P3.p cells in the bar-1(++);lin-39(0) mutant often exhibit a pulse with very low amplitude, making it challenging to determine the exact time of pulse onset. However, pulse onset is often strongly correlated between cells in the same animal. To measure the time between pulse onset and time of fusion, we therefore calculate the delay between the pulse onset in P4.p and time of fusion in P3.p, as \( \langle \Delta t_f \rangle = \langle t_f^3 - t_0^3 \rangle \). To estimate the standard deviation \( \sigma_f \) we followed different strategies for the two mutant strains that exhibited Pn.p fusions, bar-1(++);lin-39(0) and bar-1(++);cwn-1(0). For the bar-1(++);lin-39(0) strain, P3.p had a much higher fusion frequency than P4.p (Supplementary Table 1) and we only considered animals where P3.p assumed hyp7/fusion fate and P4.p assumed VPC fate. Here, using Eq. 9, we estimated the standard deviation in fusion time as \( (\sigma_f)^2 = C_{ff} - C_{f0} \), where \( C_{ff} = \langle(t_f^3 - \langle t_f^3 \rangle)^2 \rangle \) and \( C_{f0} = \langle(t_f^3 - \langle t_f^3 \rangle)(t_0^3 - \langle t_0^3 \rangle)\rangle \). For the bar-1(++);cwn-1(0) strain, P3.p and P4.p have similar, but low hyp7/fusion frequencies. Hence, we considered all animals where one cell, either P3.p or P4.p, assumed hyp7/fusion fate and the other assumed VPC fate. We estimated the standard deviation in fusion time as \( (\sigma_f)^2 = C_{ff} + C_{00} - 2C_{f0} - (\sigma_0^{int})^2 \), where \( C_{ff} = \langle(t_f - \langle t_f \rangle)^2 \rangle \), \( C_{00} = \langle(t_0 - \langle t_0 \rangle)^2 \rangle \) and \( C_{f0} = \langle(t_f - \langle t_f \rangle)(t_0 - \langle t_0 \rangle)\rangle \). Here, \( \sigma_0^{int} \) is the standard deviation of the cell-intrinsic pulse onset noise as estimated from the pulse onset timing data. Using the estimated parameter values, the model reproduced the experimentally observed correlation between cell fusion time and BAR-1 pulse onset time (Supplemental Fig. 3g).

Parameter values. Even though we could estimate many model parameters directly from the experiments, this was not possible for all parameters. Because we did not observe cell fusions in the bar-1(++) strain, we were unable to measure the parameters \( \langle \Delta t_f \rangle \) and \( \sigma_f \) that dictate the timing of expression of the activator A. For that reason, we assumed that the value of these two parameters was the same as for the bar-1(++;lin-39(0) strain. For the threshold eff-1 level above which cell fusion occurs, we chose \( c_{th} = \frac{1}{2} \) and we assumed that eff-1 induction occurred with Hill coefficient \( n = 3 \) for both inhibitors and the activator. The remaining parameters \( C_A, \sigma_A, K_A, C_{LIN-39} \) and \( K_L \) were chosen so that the resulting frequency of hyp7/fusion fate matched the experimentally observed frequencies (Supplemental Table S1, Supplementary Fig. 3e), with the
constraint that \( c_{\text{LIN-39}} = 0 \) for the \( \text{bar-1}(++) ; \text{lin-39}(0) \) strain. In addition to the simulations for the experimentally examined strains, we also simulated a hypothetical mutant that has the same hyp7/fusion frequency as the \( \text{bar-1}(++) ; \text{cwn-1}(0) \) mutant, but achieves this by reducing the \( \text{BAR-1} \) pulse slope rather than the pulse onset time. For this hypothetical mutant, we used the same parameters as for the \( \text{bar-1}(++) \) strain, but lowered the average pulse slope \( \langle s \rangle \) until the desired hyp7/fusion frequency was found. For the \( \text{bar-1}(++) \) mutant, we were unable to find parameter combinations for which the hyp7/fusion frequency in the simulations was close to zero, as observed experimentally. This is likely because the fitted distribution of pulse slopes overestimates the number of cells with low pulse slope (Supplemental Fig. 3a) and, hence, low levels of inhibitory \( \text{BAR-1} \). A complete list of all parameters is given in the table below:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>( \text{bar-1}(++) )</th>
<th>( \text{bar-1}(++) ; \text{lin-39}(0) )</th>
<th>( \text{bar-1}(++) ; \text{cwn-1}(0) )</th>
<th>Low pulse slope mutant</th>
<th>Parameter estimated from experiment</th>
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<tr>
<td>( \langle s \rangle )</td>
<td>0.33</td>
<td>0.27</td>
<td>0.31</td>
<td>0.20</td>
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</tr>
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<td>( \sigma_s )</td>
<td>0.15</td>
<td>0.21</td>
<td>0.13</td>
<td>0.15</td>
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<tr>
<td>( \langle t_0 \rangle )</td>
<td>0.29</td>
<td>0.30</td>
<td>0.53</td>
<td>0.29</td>
<td>Yes</td>
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<tr>
<td>( \sigma_{t_0} )</td>
<td>0.051</td>
<td>0.095</td>
<td>0.121</td>
<td>0.051</td>
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<tr>
<td>( \sigma_{t_0}^{\text{int}} )</td>
<td>0.074</td>
<td>0.132</td>
<td>0.018</td>
<td>0.074</td>
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<tr>
<td>( K_B )</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
<td>No</td>
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<tr>
<td>( \langle \Delta t_f \rangle )</td>
<td>0.21</td>
<td>0.21</td>
<td>0.11</td>
<td>0.21</td>
<td>Yes</td>
</tr>
<tr>
<td>( \sigma_f )</td>
<td>0.048</td>
<td>0.048</td>
<td>0.034</td>
<td>0.048</td>
<td>Yes</td>
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<tr>
<td>( \langle T_{L_2} \rangle )</td>
<td>11.2</td>
<td>10.2</td>
<td>12.8</td>
<td>11.2</td>
<td>Yes</td>
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<tr>
<td>( \langle c_A \rangle / K_A )</td>
<td>1.3</td>
<td>1.3</td>
<td>1.3</td>
<td>1.3</td>
<td>No</td>
</tr>
<tr>
<td>( \sigma_A / K_A )</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
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</tr>
<tr>
<td>( c_{\text{LIN-39}} / K_L )</td>
<td>0.8</td>
<td>0.0</td>
<td>0.8</td>
<td>0.8</td>
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<tr>
<td>( e_{\text{th}} )</td>
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<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
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<tr>
<td>( n )</td>
<td>3</td>
<td>3</td>
<td>3</td>
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<td>No</td>
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**Simulation.** For all simulations, we generated data for two cells, P3.p and P4.p, in \( 1 \cdot 10^4 \) animals. For each cell \( i \), we generated stochastic values for \( s_i, c_{A,i}, t_0^i \) and \( t_f^i \) according to Eqs. 6-9, where we discarded pulse slope values \( s_i < 0 \) as they are an artifact of fitting the experimental distribution by a Gaussian. Based on the values for pulse onset time and pulse slope, we calculated for each cell the inhibitory \( \text{BAR-1} \) level \( c_{\text{BAR-1}} \) according to Eq. 5, the resulting \( \text{eff-1} \) level according to Eq. 4 and marked each cell as hyp7/fusion rather than VPC fate if the \( \text{eff-1} \) level exceeded the threshold value \( e_{\text{th}} \). In the above table, all times are expressed as fraction of larval stage duration. However, to facilitate comparison with the experimental distribution, the average pulse slope \( \langle s \rangle \) and its standard deviation \( \sigma_f \) are in units of fluorescence increase per hour. For that reason, when used the pulse slope to calculate the \( \text{BAR-1} \) level \( c_{\text{BAR-1}} \) in the experimental units of fluorescence (Fig. 6h), we first converted the
time between pulse onset and fusion from dimensionless units to hours, by multiplying the dimensionless time with the average L2 larval stage duration \(\langle T_{L2} \rangle\).

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Author Contributions


Declaration of Interests

The authors declare no competing interests.
References


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### Table S1

<table>
<thead>
<tr>
<th>Genotype</th>
<th>Fusion rates (%) (^a)</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>ncI\(_\text{s13}[\text{ajm-1::GFP}]\)</code>(^b)</td>
<td>28</td>
</tr>
<tr>
<td><code>ou\_\text{Is20}[\text{ajm-1::mCherry}]\)</code>(^b)</td>
<td>37</td>
</tr>
<tr>
<td><code>c\_\text{w1}(\text{ok546};n\_\text{cIs13}[\text{ajm-1::GFP}]\)</code>(_\text{cwn-1(0)})`</td>
<td>90</td>
</tr>
<tr>
<td><code>bar\_\text{-1(\text{ga80});nc\_Is13}[\text{ajm-1::GFP}]\)</code>(_\text{bar-1(0)})`</td>
<td>80</td>
</tr>
<tr>
<td><code>\text{lin-39(\text{gk893});nc\_Is13}[\text{ajm-1::GFP}]\)</code>(_\text{lin-39(0)})`</td>
<td>100</td>
</tr>
<tr>
<td><code>\text{lin-39(n709);ou\_Is20}[\text{ajm-1::mCherry}]\)</code>(_\text{lin-39(\text{lf})})`</td>
<td>69</td>
</tr>
<tr>
<td><code>\text{lin-39::GFP;}\text{HIS24-\text{H2B::mCherry;}nc\_Is13}[\text{ajm-1::GFP}]\)</code>(_\text{lin-39(++)})`</td>
<td>2</td>
</tr>
<tr>
<td><code>c\_\text{w1}(\text{ok546};\text{lin-39::GFP;}\text{HIS24-\text{H2B::mCherry;}nc\_Is13}[\text{ajm-1::GFP}]\)</code>(_\text{cwn-1(0); lin-39(++)})`</td>
<td>20</td>
</tr>
<tr>
<td><code>bar\_\text{-1::GFP;}\text{ou\_Is20}[\text{ajm-1::mCherry}]\)</code>(_\text{bar-1(++)})`</td>
<td>0</td>
</tr>
<tr>
<td><code>bar\_\text{-1::GFP;}\text{c\_w1(\text{ok546};ou\_Is20}[\text{ajm-1::mCherry}]\)</code>(_\text{cwn-1(0); bar-1(++)})`</td>
<td>6</td>
</tr>
<tr>
<td><code>bar\_\text{-1::GFP;}\text{lin-39(n709);ou\_Is20}[\text{ajm-1::mCherry}]\)</code>(_\text{lin-39(\text{lf}); bar-1(++)})`</td>
<td>24</td>
</tr>
</tbody>
</table>

\(^a\) Fusion rates are rounded to the nearest percentage. Fusion events were counted by the loss of `\text{ajm-1}` staining during the L2 stage, and non-fusion animals were only counted if the animal reached the L3 ecdysis without a fusion event.  

\(^b\) No statistical difference between P3.p fusion rates in these marker strains, (\(P= 0.47\), Fisher’s Exact Test).  

\(^c\) P3.p – P8.p fused prematurely in the L1 stage in the null mutant.
Figure S1. The gene eff-1 is expressed at a high level before cell fusion. 

(A) Example of an animal with both P3.p and P4.p showing evidence of recent fusion, due to the currently degrading and ruffled appeared of AJM-1::GFP, marked by dashed-white brackets in the composite image (bottom panel). (B) Quantification of the number of eff-1 spots in cells that have recently fused as in (A). Different genetic backgrounds show similar levels of eff-1 expression at the time of fusion. Dots correspond to individual cells and are plotted with the average and standard error. No significant differences are present in the average number of eff-1 spots (Student’s t-test). (C) Image of a mid-L2 stage eff-1(hy21) temperature-sensitive-mutant with a point mutation that renders the protein non-functional, but allows for mRNA staining with smFISH probes. High levels of eff-1 expression are seen in P2.p and P3.p, despite them remaining unfused (marked by white brackets).
Figure S2. Correlation between BAR-1 pulse end time and time of fusion

Correlation between BAR-1 pulse end time $t_0 + T$ in a VPC and fusion time $t_{\text{fusion}}$ in a hyp7/fusion cell, where $t_0$ is the pulse onset time and $T$ the pulse duration. Circles correspond to animals where P3.p, but not P4.p, assumed hyp7/fusion fate and triangles to animals where the cell fate assignment is reversed. Color indicates the $\text{bar-1}(+);\text{lin-39}(lf)$ (orange) and $\text{bar-1}(+);\text{cwn-1}(0)$ (green) mutants. The lines correspond to $t_{\text{fusion}}/T_{L2} = \Delta T + t_0/T_{L2}$, with $\Delta T = 0.2$ (orange) and $\Delta T = 0.1$ (green), and are the same as those in Fig. 5g in the main text. The correlation between pulse end time and time of fusion is weaker than that between pulse start time and time of fusion (Fig. 5g in the main text).
Figure S3. Fitting minimal model to experimental observations. 

(A) Experimentally observed distribution of BAR-1 pulse slope \( s \) in the P3.p cell (markers) and the Gaussian fit used in the model (solid line). Color denotes the \( \text{bar-1}(++) \) (purple), \( \text{bar-1}(++);\text{lin-39}(lf) \) (orange) and \( \text{bar-1}(++);\text{cwn-1}(0) \) (green) mutants. 

(B) Comparison of pulse slope distributions in the model. Included are the distributions for the mutants in (A) and a hypothetical mutant with hyp7/fusion frequency similar to \( \text{bar-1}(++);\text{cwn-1}(0) \) but achieved by decreasing pulse slope rather than delaying pulse onset. 

(C) Experimentally observed distribution of BAR-1 pulse onset time \( t_0 \) (markers) in the P3.p cell and the Gaussian fit (solid line). Color indicates the different mutant strains. 

(D) Comparison of pulse onset time between the different mutants. The distributions for the \( \text{bar-1}(++) \) (purple) and low pulse slope (black) mutants overlap. 

(E) Model simulations of cell fate decisions in the \( \text{bar-1}(++) \) (purple), \( \text{bar-1}(++);\text{lin-39}(lf) \) (orange), \( \text{bar-1}(++);\text{cwn-1}(0) \) (green) and low pulse slope (black) mutant. Each marker indicates the activator level \( c_A \) and inhibitory Wnt level \( c_W \) at the fusion time \( t_{\text{fusion}} \) for a single simulation. The red line indicates the boundary between activator and Wnt inhibition levels that result in hyp7/fusion fate (high \( c_A \), low \( c_W \)) or VPC fate (other). The lack of LIN-39 inhibition enlarges the hyp7/fusion region in the \( \text{bar-1}(++);\text{lin-39}(lf) \) mutant. For each mutant the hyp7/fusion frequency, calculated from 1-10^6 simulations, is given. 

(F) Correlation between pulse onset time in the P3.p and P4.p cell in the same animal, generated by the model. Data is for the different mutants in (E). 

(G) Correlation between pulse onset time in P4.p and time of fusion in P3.p in animals where P3.p, but not P4.p, assumes hyp7/fusion fate. Color corresponds to the different mutants in (E). The lines correspond to \( t_{\text{fusion}}/T_{L2} = \Delta T + t_0/T_{L2} \), with \( \Delta T=0.2 \) (dashed line) and \( \Delta T=0.1 \) (dotted line).
Figure S4. Inverse relationship between $eff-1$ expression and BAR-1::GFP levels.
Number of $eff-1$ mRNA molecules, as measured using smFISH, compared to the BAR-1::GFP fluorescence level in different Pn.p cells, with each marker corresponding to a single cell. BAR-1::GFP levels are permissive for high levels of $eff-1$ expression, while high levels of BAR-1::GFP fluorescence block $eff-1$ expression.
Supplemental Movies

**Movie S1**: (Top panel) Apical junction marker AJM-1::mCherry and (bottom panel) GFP expressed in the hypodermal syncytium hyp7 for a P3.p cell assuming hyp7/fusion fate. At the time of fusion with hyp7, 6h20m after the start of the L2 larval stage, pronounced ruffling of AJM-1 is followed by its removal from P3.p. Concomitantly, GFP flows from the hyp7 syncytium into P3.p, as indicated by the yellow arrow. A dpy-7p::mCherry nuclear marker was used for cell identification (top panel).

**Movie S2**: (Top panel) Apical junction marker AJM-1::mCherry and (bottom panel) GFP expressed in the hypodermal syncytium hyp7 for a P3.p cell that assumes vulva precursor cell fate. AJM-1 is present in P3.p throughout the entire L2 larval stage and no inflow of GFP into P3.p is observed. A dpy-7p::mCherry nuclear marker was used for cell identification (top panel).

**Movie S3**: Pulsatile BAR-1 dynamics in P(3-5).p cells in a single animal. Time is relative to the start of the L2 larval stage. Each panel corresponds to a single cell. Shown are the apical junction marker AJM-1 (magenta) and BAR-1::GFP (green). The animal examined corresponds to that shown in Fig. 4a,b.
Supplemental Methods Table 1

smFISH probes used to hybridize with eff-1 mRNA molecules

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