Optics for Terawatt-Scale Photovoltaics – Review and Perspectives

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Abstract: Photovoltaics—a mature technology—is set to play a vital role in achieving a carbon-free energy system. This article examines the pivotal role of optics in advancing photovoltaics. We identify key scientific research areas where the optics community can make significant contributions. We are guided by the central question: How can optics facilitate the large-scale deployment of photovoltaics necessary for decarbonizing our societies?

Contents

1. Introduction

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Photovoltaics (PV) installations reached a global capacity of two terawatt (2 TW) by November 2024 [1], and the rates of growth and cost reduction are remarkably high [2]. We took these achievements as an opportunity to reflect on how the optics research community can contribute to the further growth of PV, which is crucial for the transition to a carbon-free energy system. We were guided by the questions:

> *How can optics help to further support the growth of PV?*
>
> *Which innovations in the field of optics are needed today to overcome current limitations in efficiency, distribution, and social acceptance?*

We also identified optical concepts that might not yet be economically viable and where yet not all open questions have been answered, but which are developing very dynamically and have great potential for further pushing PV technology. Figure 1 outlines this article, which is based on the optical challenges derived from the current pressing needs of photovoltaics on terawatt scale.

The pivotal Chapter 2 deals with the current status of *Photovoltaics on terawatt-scale*. From this chapter we derive the topics to which the optics community can contribute to facilitate such a large-scale exploitation. The chapter summarizes the different PV technologies ranging from crystalline silicon photovoltaics and thin-film solar cells to multi-junction solar cells. As illustrated in Fig. 1, the following major challenges are identified (colored arrows): sustainable PV production, increasing the power conversion efficiency (PCE) of PV modules, maximizing the energy yield of PV systems, and the integration of PV in the environment. From these challenges we derive research topics (rectangles) that are discussed in the chapters of this article.

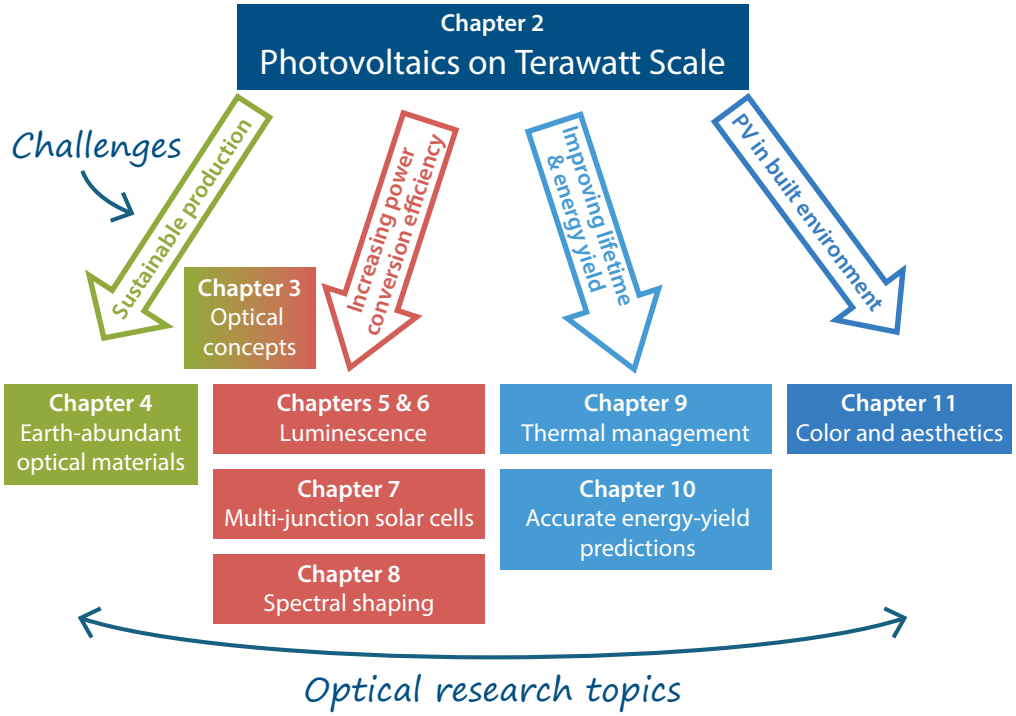

Fig. 1. Outline of the article. Optical research topics derived from the current challenges of photovoltaics entering the terawatt scale.

Chapter 3 summarizes important *Optical concepts* that have been used in photovoltaics in the past. This includes anti-reflective coatings, random and periodic textures for anti-reflection and light trapping, and concentrating photovoltaic systems. Further, illumination conditions different from standard testing conditions are discussed.

Chapters 4–11 delve into the research topics outlined in Fig. 1, forming the core of this article. Each chapter concludes with a summary of the identified *Advances Needed*.

Because the global PV production is growing exponentially, using earth-abundant materials is of utmost importance. However, in state-of-the-art silicon solar modules, large amounts of rare materials such as indium and silver are used. In Chapter 4, *Ecodesign for solar cells by using earth-abundant optical materials*, we address the development of alternative optical materials based on earth-abundant elements.

Luminescence of solar cells, discussed in Chapter 5, has been identified as vivid research area giving insights into both the electrical and optical solar cell properties. With increasing opto-electronic quality of current solar cell absorber materials in terms of photoluminescent quantum yield, the exploration of internal luminescence to increase the voltage in single-junction solar cells, and luminescent coupling in multi-junction solar cells is picking up speed. Further, a new perspective on luminescence in solar cells is introduced considering *Luminescence as Two Distinct Photon Gases Present Inside Every Solar Cell* in Chapter 6.

Silicon solar cells have been dominating the PV market with a current share of more than 90%. Silicon technology is already so far developed that it reaches PCEs close to its physical limit. *Multi-junction solar cells* are regarded as the most promising concept to surpass the single-junction efficiency limit. Chapter 7 introduces the general multi-junction solar cell concept and summarizes recent multi-junction solar cell technologies based on III–V semiconductors, silicon, CIGS and perovskites. At the end, we discusses the specific optical challenges and specific scientific and technological questions to be addressed in the future.

While multi-junction solar cells are the most promising route to overcome the efficiency limitation of single-junction solar cells, *Spectral shaping* aims to convert the solar spectrum into a spectrum that better matches to bandgap of the solar cell, which has a similar effect on the achievable efficiency. Chapter 8 discusses developments on down-conversion of high-energy photons into a larger number of lower-energy photoexcitations, up-conversion of below-bandgap photons into a (lower number) of above-bandgap photons, and concentration of the sunlight in luminescent solar concentrators.

Thin-film and photonic strategies can increase the front surface emissivity of the cover glass on the module, thereby allowing the module to take better advantage of *Thermal Management of Photovoltaic Modules* and maintain a lower steady-state temperature. Further, enhancing the reflectance of sub-bandgap photons can prevent these photons from penetrating into the module and cause parasitic heating. Chapter 9 discusses, how optimizing both elements in a low-cost and scalable way represents an important opportunity for optics to improve thermal aspects of photovoltaic modules.

The performance of PV systems is assessed by a variety of key performance indicators such as levelized cost of electricity (LCOE), energy payback time, specific CO_2 emissions, or resource efficiency. All these performance indicators require the total amount of energy harvested from the PV installation, taking into consideration seasonal and daily variations in irradiation conditions, spectrum, temperature, as well as all the details of the installation (e.g. module orientation, type of tracking, shadows, soiling, etc.). Therefore, accurately predicting the *Energy yield (EY)*, discussed in Chapter 10, is pivotal for PV system and device architecture design of solar modules.

An appealing *Color and aesthetics of photovoltaic modules* has been identified as essential for social acceptance of PV, because stakeholders in rural and urban areas prefer to harmonize the aesthetic appearance of photovoltaic modules with their surroundings. The final Chapter 11 summarizes the most commonly used coloring techniques in the production of PV modules.

2. Advancing photovoltaics to the terawatt scale

I. GORDON, A. FEJFAR

In this chapter, we will give an overview of the state-of-the-art of photovoltaics, the main PV technologies currently being industrially produced and being developed, and the main technological challenges still remaining for a massive production and deployment of PV technology in the future.

2.1. Global PV production in 2023

The number of worldwide installed PV systems has grown almost exponentially since 2010, resulting in a cumulative installed PV capacity of roughly 1.5 Terawatt peak (TW_p) at the end of 2023 [2], compared to only 39 GW_p installed at the end of 2010 (1 TW_p = 1000 GW_p and W_p denotes the maximum power a PV module can deliver when it is illuminated with the standardized AM1.5 solar spectrum at a module temperature of 25°C). In 2023, around 300 GW_p of PV modules were installed worldwide and it is expected that this yearly installation rate will rapidly increase in the coming decade to 1-3 TW_p per year.

In terms of PV module technology, around 95% of PV modules currently produced are based on crystalline-silicon technology, while the remaining 5% are based on thin-film technology. Crystalline-silicon technology uses crystalline silicon wafers with a thickness of 150-180 microns as the absorber material for the incoming light. Thin-film technology, on the other hand, is based on the use of thin layers of a light absorber (mostly CdTe or chalcopyrite materials), grown on a substrate such as glass, a polymer, or a metal sheet. The thin-film absorber thickness is typically in the range of 100 nm to 2 microns.

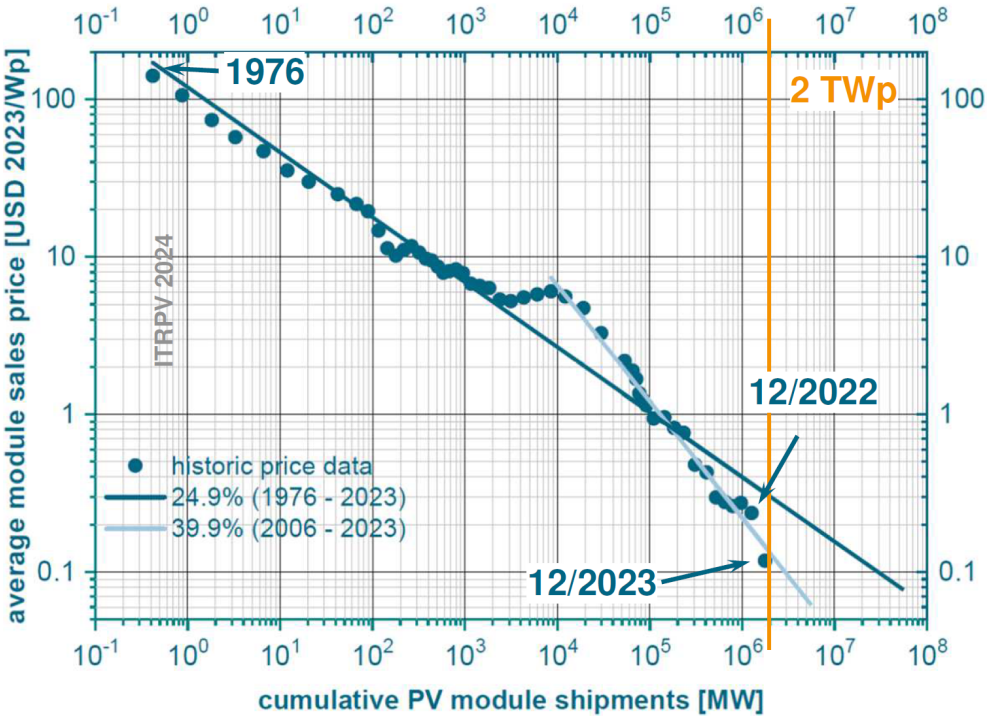

Fig. 2. The learning curve for crystalline silicon PV modules (reprinted from Ref. [3] with permission from VDMA).

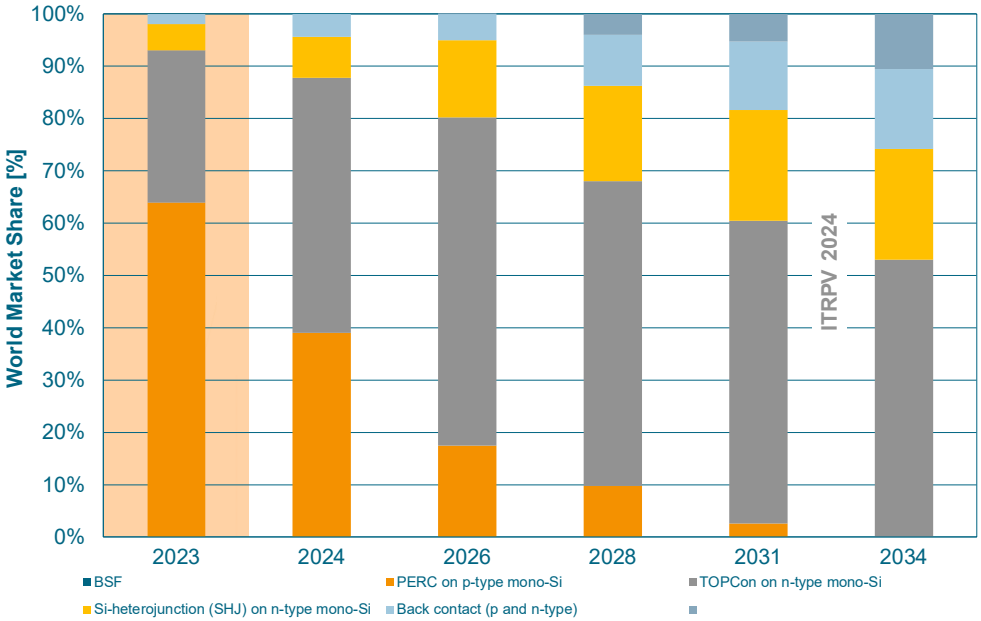

Fig. 3. Market shares for different crystalline silicon cell technologies (reprinted from Ref. [3] with permission from VDMA).

The rapidly growing PV market is driven by the decreasing cost of PV technology. Figure 2 shows the learning curve for crystalline silicon PV modules from 1976 to 2023 [3]. Prices have fallen by almost 25% with each doubling of installed volume, accelerating to 40% since 2006 due to increased global production. At the end of 2023, the average calculated spot market price for silicon PV modules cost was as low as 0.12 USD per W_p. This cost reduction results from upscaling, manufacturing improvements, and technological innovations in materials and device structure, including optics and light management (Chapter 3).

In 2023, PV modules for systems over 10 MW_p made up about 1/3 of system costs, with the balance of system (BoS) contributing 2/3 [4]. BoS includes components like racking, wiring, inverters, and maintenance. The PV module cost share is expected to drop to 20% in the next decade [4]. Higher efficiency PV modules reduce BoS costs by generating more power per area.

2.2. Main and upcoming PV technologies

In this section, we will present the various PV technologies and device architectures that are in mass production in 2024, as well as those PV technologies and device structures that are currently being developed and that can be expected to become mass produced relatively soon.

2.2.1. Crystalline Silicon PV technologies

Crystalline silicon PV technology uses crystalline silicon wafers as the active light-absorbing material for the PV devices. Typically, large-area monocrystalline silicon wafers with near perfect crystal structures are processed into individual solar cells, which are then interconnected and laminated into a solar module [5]. The crystalline silicon solar cells can be classified based on the device architecture that is used.

Figure 3 shows an overview of the current and anticipated future market shares of the main crystalline-silicon PV cell architectures [3]. BSF stands for *Back Surface Field* cell which was the main workhorse of the PV industry until around 2018. In 2023, more than 70% of crystalline

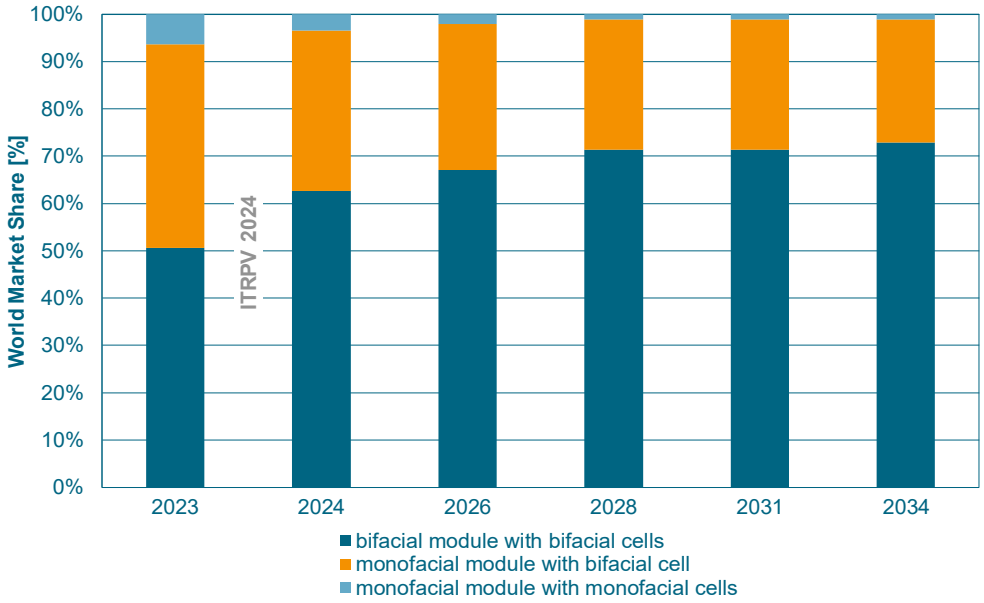

Fig. 4. Evolution of the market share for bifacial modules (reprinted from Ref. [3] with permission from VDMA).

silicon solar cells processed worldwide were based on the PERC device architecture which is an acronym for *Passivated Emitter and Rear Cell*. Upcoming silicon device architectures in industrial production are the TOPCon cells (*Tunnel Oxide Passivated Contacts*) and SHJ cells (*Silicon HeteroJunction*). Finally, *backcontact technology* refers to solar cells where the metal contacts of both polarities are placed at the backside of the solar cell.

Currently, there is a trend in the photovoltaic industry to produce more and more bifacial cells and modules (see Figure 4). In 2023, the market share for bifacial silicon solar cells was around 85% [3], meaning that the light can enter the solar cell both from the front as well as from the rear side. To make silicon solar cells bifacial, the electrical contacts need to be designed appropriately and the light management and optics of the device need to be adapted. The market share of bifacial solar cells is expected to increase further to 90% within the next decade [3].

PERC. These solar cells have replaced BSF cells in industrial production in recent years because they show much higher energy conversion efficiencies, mainly because of a much better rear surface passivation and a better rear surface light reflection enabling increased carrier densities leading to higher open-circuit voltages (V_{oc}) (see Chapters 5 and 6). This is achieved using rear surface passivation by dielectric layers and a smaller metal/semiconductor contact area [6]. The insertion of a dielectric passivation layer between metal and silicon also substantially increases the reflection of light at the rear silicon surface. Although the first paper describing a PERC cell architecture (see Figure 5a) already appeared in 1989 [7], it took more than three decades before the technology could be industrialized [8]. Typical energy conversion efficiencies at cell level that can be reached by this technology are above 24%.

TOPCon. In 2013, a new silicon solar cell technology called TOPCon was developed by Fraunhofer ISE in Germany [9]. The schematic of the TOPCon solar cell is depicted in Figure 5b. In the TOPCon cell architecture, the entire rear surface of the n-type silicon solar cell is passivated by a thin SiO_x layer of around 1–2 nanometers. In addition, an n-type doped

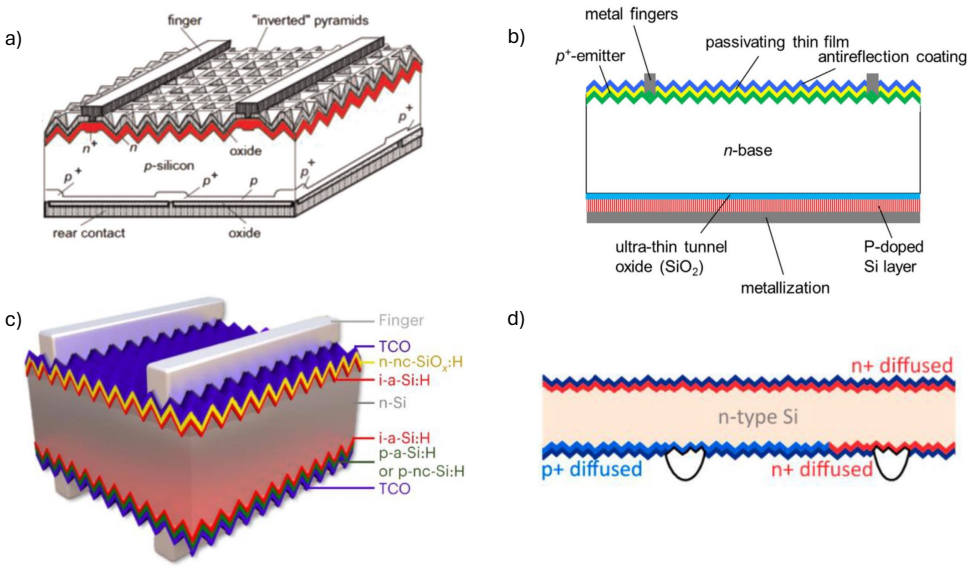

Fig. 5. Four of the main silicon solar cell architectures currently in production: a) PERC solar cell, b) TOPCon solar cell, c) 2-side contacted silicon heterojunction solar cell, and d) IBC solar cell [(a) reprinted from Ref. [7], with the permission of AIP Publishing; (b) reprinted from Ref. [9], with permission from Elsevier; (c) reprinted from Ref. [11]; (d) reprinted from Ref. [12]].

polysilicon layer is formed on top of the SiO_x layer to further enhance the passivation at the rear surface by field-effect passivation. This cell structure is an example of a so-called passivated contact cell structure. The charge carriers can move through the thin interfacial SiO_x by either pure tunneling or pinhole-assisted tunneling [6]. Moreover, due to band bending and high doping of the poly layer, the structure provides carrier selectivity. Advantages of TOPCon technology over PERC technology are among others a higher energy conversion efficiency potential (at the moment of writing, the highest reported efficiency for a TOPCon solar cell is 26.7% [10]) and the absence of the need to make point-contact holes at the rear surface. As a result, it is expected that TOPCon devices will soon replace PERC as the dominant technology in industrial silicon PV production (see Figure 3).

Silicon heterojunction (SHJ). The SHJ solar cell is another example of a so-called passivated contact cell structure that is finding its way into mass production. The schematic structure of a 2-side contacted SHJ solar cell is shown in Figure 5c. The main feature of SHJ cells is the use of thin intrinsic and doped a-Si:H layers of a few nanometers on both sides of the crystalline silicon absorber to passivate the silicon and to create emitter and back surface field (or front surface field) layers. This symmetric cell structure allows to extract electrons and holes selectively and can be created via low temperature processing, which makes SHJ cells compatible with the use of thin crystalline-silicon wafers. The highest energy conversion efficiency obtained at the moment of writing this article with the 2-side contacted SHJ cell architecture is 26.8% [11].

Backcontact solar cells. Finally, silicon backcontact solar cell architectures aim at achieving even higher energy conversion efficiencies by placing both n-type and p-type contacts at the rear of the cells, thereby reducing the shadowing losses at the front of the cell [4]. There are

different types of silicon backcontact solar cells that can be divided into three classes [13], namely back-junction cells (e.g. interdigitated backcontact cells, see Figure 5d), emitter-wrap-through cells (EWT) and metallisation wrap-through cells (MWT). In this section, we will focus on interdigitated backcontact cells (IBC) since these cells are currently the closest to mass-scale industrialization and have the highest efficiency-potential. To reach the highest energy conversion efficiencies, the IBC architecture can be combined with the use of carrier-selective contacts (TOPCon or SHJ). In May 2024, the company Longi broke the world record energy conversion efficiency for a single-junction crystalline silicon solar cell with an SHJ-IBC solar cell showing an efficiency of 27.3% [14].

2.2.2. Thin-film PV technologies

Thin-film photovoltaics refers to photovoltaic devices that are based on the use of a thin film of material as sunlight absorber. Since crystalline silicon has an indirect bandgap, crystalline silicon wafers used in photovoltaics are typically around 150–200 µm thick to enable sufficient absorption of the incoming light without the need of very advanced light trapping schemes. However, when a material with a direct bandgap is used as sunlight-absorbing layer, much thinner absorbers can be used and these absorbers can then be deposited as thin films on top of a substrate (e.g. glass, metal foil, . . .).

The basic architecture of a thin film solar cell consists of a sunlight-absorbing layer sandwiched between two contact layers [6]. One or more layers may be further required to passivate the interfaces between the layers. Thin film solar cells can be grown in two different configurations, namely substrate or superstrate configuration [6]. In substrate configuration, the sunlight enters the device from the opposite side of the substrate onto which the device has been grown. In superstrate configuration, the sunlight enters the device through the substrate onto which the device has been grown and hence that substrate needs to be transparent in this case. In this section we briefly describe the main thin-film PV technologies.

Cadmium telluride. In 2023, CdTe photovoltaics had the second biggest market share worldwide after crystalline silicon photovoltaics. One of the reasons of the success of CdTe photovoltaics lies in its combination of a high energy conversion efficiency potential with low processing costs. CdTe is a polycrystalline p-type semiconductor material belonging to the II–IV group with a direct bandgap of 1.45 eV [6]. Whereas the theoretical maximum energy conversion efficiency is above 30%, the highest efficiency demonstrated for a small area CdTe cell is currently 23.1% [15]. Because of its direct bandgap, a CdTe layer thickness of around 1 micron is sufficient for sunlight absorption purposes, which also relaxes the minority carrier lifetime requirements of the material. Typically, a CdTe solar device consists of a heterojunction between p-type CdTe and n-type CdS [6]. Some of the main challenges of CdTe photovoltaics are directly related to the absorber material used, namely toxicity issues related to cadmium and the scarcity of tellurium. Both issues limit the mass production and widely spreading of the technology.

CIGS. $Cu(In, Ga)(S, Se)_2$ is another thin film solar cell technology that is being industrially produced, be it still in relatively small quantities compared to crystalline silicon PV and even CdTe PV. The CIGS semiconductor material has a chalcopyrite crystal structure with a tunable bandgap in the range of 1.0–1.6 eV [6]. CIGS is a direct bandgap material with p-type conductivity that arises due to Cu vacancies [6]. The conductivity of the material can therefore be tuned by changing the ln to Cu ratio during deposition. Similar to CdTe, a CIGS solar device also makes use of a heterojunction with an n-type material such as CdS or Zn(O, S) [6]. At the end of 2023, the highest independently confirmed energy conversion efficiency demonstrated for a small area CIGS cell was 23.6% [15]. Some of the main challenges of CIGS photovoltaics are the use of the scarce element In, and homogeneity problems of the compound material when grown on

large areas which typically leads to much lower energy conversion efficiencies for large devices compared to small lab-scale devices.

III–V semiconductors. Materials such as InP and GaAs are direct bandgap semiconductors with significantly higher sunlight absorption compared to silicon [16], and have been used for photovoltaic devices for many decades. Their high sunlight absorption allows for the fabrication of ultra-thin, reliable, and highly efficient solar cells. III-V solar cells can be single junction devices (such as a GaAs cell), or they can be multi-junction devices in which multiple III-V semiconductor materials with different bandgaps are grown or stacked on top of each other [17]. The cost of III-V solar devices is significantly higher (up to two orders of magnitude) than that of silicon solar cells, making them mostly used in niche applications such as space solar cells and concentrated photovoltaics (CPV) [16]. The highest energy conversion efficiency ever reached with a solar cell to date is 47.6% which was achieved in 2022 with a four-junction wafer-bonded III-V solar cell (GaInP/GaInAs ; GaInAsP/GaInAs) under an irradiance of 665 suns [15, 18].

Amorphous silicon. Hydrogenated amorphous silicon (a-Si:H) has been used since the 1970s for photovoltaic applications. It has a direct bandgap of around 1.6–1.8 eV (tunable by changing the hydrogen content) and can be deposited at low temperatures on a variety of substrates [6]. Due to its direct bandgap and comparatively high sunlight absorption coefficient, a-Si:H layer thicknesses of just a few 100 nm are sufficient for solar cell purposes. The main drawback of a-Si:H solar cells are their low energy conversion efficiencies and their instability under light illumination called the Staebler-Wronski effect [6]. Since the highest stabilized energy conversion efficiency reached with an amorphous silicon solar cell is only 10.2% [15], multi-junction devices have been investigated in which the a-Si:H material is combined with so-called nano-crystalline silicon (nc-Si) or amorphous SiGe alloys to boost the efficiency. This had led to tandem devices with a best efficiency of 12.7% and triple junctions with a best efficiency of 14.0% [15].

Organic photovoltaics. These cells make use of thin films of organic semiconductors to convert sunlight into electricity, and offers the potential of low cost, flexible devices and semi-transparency [19]. The organic semiconductors used are π-bonded small molecules or polymers that are made up of carbon, hydrogen, and other atoms such as nitrogen, sulfur, and oxygen [19]. Light absorption in these organic materials generates tightly bonded Frenkel excitons instead of free charges in inorganic semiconductors [19]. Organic solar cells typically consist of a bulk heterojunction formed by a donor material and an acceptor material to enhance exciton dissociation and charge collection. Over the last two decades, many different photo-active organic materials have been synthesized and tested for organic photovoltaics. The resulting energy conversion efficiency of organic solar cells is highly dependent on the materials used. Moreover, morphological control of donor and acceptor domains on the nanoscale is needed to enhance efficient exciton diffusion and dissociation, carrier transport and suppression of recombination losses [20]. The highest certified energy conversion efficiency reported for organic photovoltaics to date is 19.2% [15, 20].

Perovskites. The term perovskite refers to a class of materials with the general chemical formula ABX_3 that typically have a cubic or octahedral crystal structure [21]. Perovskite materials with photovoltaic properties are typically hybrid organic-inorganic perovskites containing both organic (e.g. methylammonium CH_3NH_3) and inorganic components (e.g. inorganic cations like Pb and Sn, as well as halides based on I, Cl and Br). One of the most widely used perovskite materials for photovoltaics are methylammonium lead iodides ($CH_3NH_3PbI_3$) with an energy bandgap of 1.55 eV [21], but by tuning the material composition (e.g. mixing various halides) different material properties such as different bandgaps or different electrical transport characteristics can

be achieved. The most successful perovskite-based solar cells have the planar heterojunction device structure in which the perovskite light-absorbing layer is sandwiched between an electron transport layer (ETL) and a hole transport layer (HTL). Electron-hole pairs are generated in the perovskite layer by sunlight absorption and charge carrier separation and collection is facilitated by the band alignment between the HTL, perovskite and ETL. Depending on whether the sunlight first enters through the ETL or the HTL, the solar cell is called a n-i-p or a p-i-n device respectively. The highest certified energy conversion efficiency reported for single-junction perovskite solar cells to date is 26.7% [15].

2.2.3. Multi-junction PV technologies

In the previous two sections, we shortly described the main single-junction photovoltaic technologies based on crystalline-silicon wafers or thin-film absorber materials. In this section, we will discuss so-called multi-junction solar cells in which two or more sunlight absorbers with different bandgaps are placed or grown on top of each other to increase the energy conversion efficiency of the solar device. The main energy losses in a single-junction solar device come from the non-absorption of the photons with an energy below the bandgap of the absorber material and from thermalization losses of the excess energy of the absorbed photons. As a result, the upper theoretical energy conversion efficiency limit of the most common single-junction solar cells is in the range 29%–33%, depending on the bandgap of the absorber material used [22]. By stacking multiple junctions made of materials with a different bandgap on top of each other, the upper theoretical energy conversion efficiency limit can be pushed upwards (e.g. to a value well above 40% for devices with 2-junctions, so-called tandems) by a more efficient conversion and utilization of the incoming photon energy. Since the last few years, tandem devices based on a crystalline-silicon bottom cell are heavily being investigated because single-junction crystalline-silicon solar devices, even those in industrial production, are rapidly nearing their practical energy conversion efficiencies, and tandems are seen as the way forward to crystalline-silicon-based device efficiencies beyond the single-junction limit [3]. Especially perovskite materials are attracting a lot of attention as potential high-bandgap top cell for silicon-based tandem devices. Currently, the highest independently confirmed energy conversion efficiency for a perovskite/silicon tandem device is 34.6% [15], which is indeed well above the record efficiencies for single-junction crystalline-silicon and perovskite solar cells.

2.3. Challenges related to the further deployment of photovoltaics

To keep the Earth's average temperature rise to less than 1.5°C, as set by the Paris agreement in 2015, requires rapid defossilisation coupled with a transition of the energy system to 100% renewable energy, using solar photovoltaic energy along with wind, hydro, geothermal, and biomass energy, to power directly or indirectly all sectors of the economy and society [23]. A massive electrification of the world's energy system is therefore needed, with an estimated required global PV generating capacity of about 50–70 TW_p by 2050 [23, 24], whereas at the end of 2023 only 1.5 TW_p was installed (see Section 2.1). The PV industry therefore needs to rapidly grow its production capacity to about 3 TW_p per year to reach this objective [23], which is roughly a ten-fold increase from the current yearly production rate. This required massive deployment of PV modules in the coming three decades with production and installation rates of several TW_p per year, will lead to important socio-economical challenges as well as to new challenges in the field of material and system technology besides the traditional R&D-subjects like performance increase and cost reduction.

In the following subsections, we will describe the main technological challenges and how optics can help resolve those challenges. For the socio-economic challenges we refer to Ref. [25].

2.3.1. Sustainable production of PV systems

Although solar radiation is an inexhaustible renewable energy source, the future required large-scale production and deployment of photovoltaic technology demands a sustainability analysis in terms of raw materials demand, energy required to manufacture the PV systems, and environmental impacts of production and operation of the PV systems [26]. In particular, sustainable PV production should ensure the proper usage of materials (e.g. minimizing the use of rare materials, avoiding toxic materials, etc.), the minimization of energy usage and greenhouse gas emission during the production process, and the proper way of dealing with the end-of-life of PV modules and systems. Ensuring a true long-term sustainable production of PV systems in the future will require new materials, adapted device concepts, and improved production technologies.

Advanced and novel optics can be of help here in many different ways, as we will illustrate in Chapter 4 of this article. That chapter will show that by a smarter ecodesign of the PV devices, we can make use of less amounts of critical rare materials like indium and silver while maintaining high device performance. Chapter 3 on the other hand will illustrate the general optical concepts in photovoltaics that can help to reduce the thickness of the silicon solar cell wafers which will reduce the CO_2 footprint of the technology.

2.3.2. PV modules with higher energy conversion efficiencies

In 2023, the cost of a large-scale PV system (> 10 kW_p) was determined for 70% by the cost of the Balance-of-System (BOS) and only for roughly 30% by the cost of the modules [4]. It is expected that the relative cost of the PV modules in the total PV system cost will lower even further in the coming years to roughly 20% [4]. Since the BOS cost typically scales with the area needed for the system, this increases the need for producing PV modules with very high energy conversion efficiencies. As a result, the industry is currently switching from the production of PERC-like devices towards the production of devices with passivated contacts (such as TOPCon and SHJ, see section 2.2.1) [3], since the latter lead to PV modules with higher conversion efficiencies. On the medium to long term, multi-junction solar devices will be needed to reach energy conversion efficiencies at module level beyond 30%.

2.3.3. PV systems with higher energy output

With the rapidly increasing number of PV systems installed worldwide, it becomes more and more important for these systems to operate at maximum performance and for the energy system operators to be able to accurately predict the energy output of the PV systems connected to the electrical grid. The higher the energy output of a given PV system or PV power plant over its period of operation, the lower the resulting levelized cost of electricity (LCOE). The maintenance and analysis of failures of PV systems and PV power plants are therefore becoming more and more important [27]. To further lower the LCOE of PV systems, one possible way is the enhancement of the operational lifetime well beyond 30 years. In the past, PV modules were made in mass production without discrimination to the climate in which the modules would be used. This has sometimes led to systems that showed an actual operational lifetime of only 10–12 years instead of the typical 20–25 years warranty lifetime [27]. To avoid early failure of PV modules and systems, especially for integrated applications where the operational conditions might be completely different from those in standard PV powerplants, the PV module design and the materials used need to be tuned to the specific operation conditions (e.g. climatic conditions) that the system will likely undergo during its lifetime. Currently, a lot of research is ongoing into advanced energy yield and lifetime prediction models that will help to increase the operational lifetime and energy yield of various standard and integrated PV applications.

Again, optics can contribute a lot to increase the energy output of PV systems hence decrease their LCOE. Chapter 10 deals with state-of-the-art illumination models that can accurately predict

the (spectral) irradiance of PV modules, which is crucial to obtain reliable energy-yield modelling tools for both standard as well as integrated PV applications. Moreover, thermal management, as described in Chapter 9, will also help to extend the operational lifetime of PV modules and systems, while also increasing the energy yield of the system.

2.3.4. Integration of PV systems in their environment

The massive deployment of photovoltaic systems also raises the question of where all these systems should be installed, especially in densely populated areas like Western Europe. The ability to use a certain space or land for multiple uses including energy generation is therefore very important. So-called integrated photovoltaics, in which the PV system is seamlessly integrated into its environment, provides this possibility. Examples are among others building-integrated PV, vehicle-integrated PV, infrastructure-integrated PV, and agrivoltaics (the combination of agriculture with photovoltaics). Integrated photovoltaics have an enormous potential and typically have better aesthetics and therefore can also lead to easier social acceptance. For these applications, the PV technology needs to be adapted to the specific operating conditions in which it will be used and a customized fabrication technology is needed to meet customer requirements for aesthetics (color, layout and shape), flexibility in shape and size, and integration (facades, canopies).

2.4. Summary

In this chapter, we described the various device architectures in production for crystalline-silicon PV as well as the various absorber materials being used and developed for thin-film PV. We also explained why multi-junction PV technology is considered the future of PV technology. We identified four major technological challenges (Fig. 1) for future mass production and deployment of photovoltaic technology in order to achieve the goal of climate neutrality and indicated how optics could help resolve these challenges. The four main challenges (Fig. 1) are

- Sustainable production of PV systems
- Higher energy conversion efficiencies
- Higher energy output and operational lifetime
- Integration of PV systems in their environment

The next chapters will delve deeper into the details of how optics will further improve photovoltaic solar energy technology in the future.

3. Optical concepts in photovoltaics

K. JÄGER, B. BLÄSI, H. HELMERS, R. SAIVE, M. SCHMID

For a highly efficient PV module the absorption of light in the absorber layer of the solar cells must be maximized. To maximize the absorption, first, reflective losses should be minimized—or, *vice versa*—coupling of the incident light into the solar cell should be maximized. Second, for weakly absorbing semiconductors, such as silicon, the absorption should be maximised, which is known as *light trapping*. Third, parasitic absorption in the supporting layers must be minimized. These three strategies are often summarized under the term "light management." For multi-junction solar cells optical concepts are used to redistribute the light between the junctions. Further, optics also can be used to improve the aesthetics of solar cells, for example by making them appear in a certain color.

In this chapter, we explain the different optical concepts, mention historical milestones and we discuss the relevance of these concepts for PV on terawatt scale. The chapter starts with the very basic concept of *antireflective coatings* in Section 3.1, we discuss the probably most relevant concept of *textured interfaces and structured materials* in Section 3.2 and also emphasize the importance of *parasitic absorption* in Section 3.3. After that we elaborate on *spectrally selective concepts* in Section 3.4, look at optimizing the *energy yield* in Section 3.5 and concepts using *concentrated light* in Section 3.6.

3.1. Antireflective coatings

Antireflective coatings, illustrated in Fig. 6a, are applied to the surface of solar cells and cover glass for photovoltaic modules to increase light absorption and conversion into electricity. They reduce the reflectance of the solar cell, allowing more light to enter the cell. The coating is designed to have a refractive index between that of air and the front material of the solar cell or PV module. Reflection is minimized, when the thickness of the coating is one quarter of the wavelength. Then the phase shift between the beams reflected from the front and rear is $\Delta\phi = \pi$.

In the early years after the first 'modern' crystalline silicon (c-Si) solar cell was produced in 1954 [30], antireflective coatings (ARC) from SiO_2 and TiO_2 were used. In 1972, an optimized ARC made from tantalum oxide (Ta_2O_5) was used to build a "violet" solar cell with a significantly boosted optical performance [31]. Other materials used for antireflective coatings are silicon nitride (Si_3N_4), lithium fluoride (LiF) and magnesium fluoride (MgF_2). SiO_2, TiO_2 and Si_3N_4 also are used as passivating layers in silicon solar cells [32].

3.2. Textured interfaces and structured materials

Texturing the front of a solar cell has a antireflective effect for a large angular and spectral range. Especially for large incident angles textures can outperform ARC. For wavelength much shorter than the typical dimensions of the texture, the antireflective effect can be explained with the effective medium approach. For textures much larger than the wavelength, the antireflective effect can be explained with geometrical optics [33]. Further, texturing increases the absorption in the low-absorbing region because of path-length enhancement, as illustrated in Fig. 6b. In the very low absorbing region of the wavelength spectrum close to the bandgap, texturing can increase the absorption up to a factor of $4n^2$, where n is the refractive index of the absorber [34].

Random textures are created by etching or crystal growth processes. However, depending on the thickness of the solar cell layers, the typical dimensions of these textures differ largely and therefore cover different optical regimes: while the interaction of light with the large pyramids used in c-Si solar cells, illustrated in Figs. 6c and 6d, can be described with *geometrical (ray) optics*, the interaction of the small textures used for thin-film silicon solar cells is in the wave-optical regime.

Already in 1974, Haynos and coworkers presented a c-Si solar cell with square-shaped pyramids

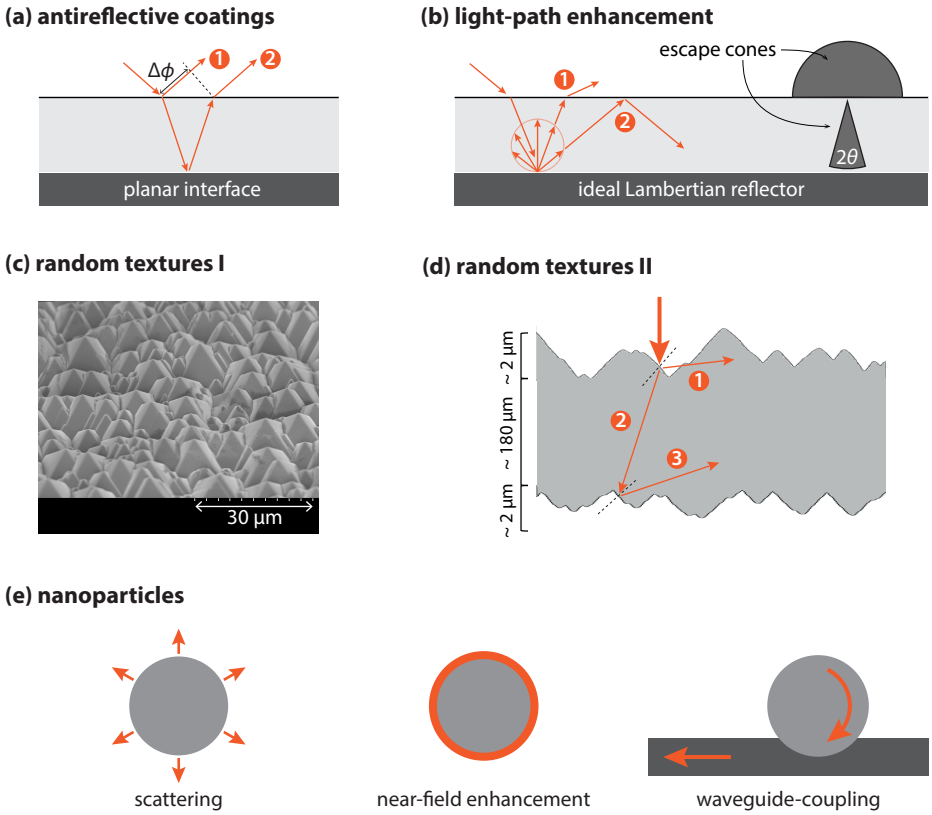

Fig. 6. Optical concepts used in photovoltaics. (a) In antireflective coatings the strongest antireflective effect is achieved, when the phase shift $\Delta\phi$ between the beams reflected from the front (1) and rear (2) is π, 3π, $5\pi\ldots$ (b) Schematic of light with energy close to the bandgap passing through a thin silicon slab with ideal Lambertian reflector on the rear side. The escape cone with opening angle $\theta = 16.3°$ within the silicon and the air escape/acceptance cone that corresponds to the full hemisphere are shown. Depending on its angle, scattered light reaching the front surface will (1) either escape or (2) encounter total internal reflection (adapted from [28]). (c–d) Random textures: (c) Scanning electron microscopy (SEM) image of a textured silicon solar cell. (d) Schematic of three ways in which pyramids randomize light: (1) reflecting on textured front, (2) transmission through textured front, and (3) reflection on textured rear. (adapted from [28]). (e) Effects of nanoparticle–light interaction: scattering, near-field enhancement, and coupling into waveguide modes. [(a), (b) and (d) adapted from Ref. [28]. (e) redrawn from Ref. [29], Fig. 3, DOI: 10.1088/1361-6641/aa59ee; © IOP Publishing. Reproduced with permission. All rights reserved.]

on top, which were created by etching [35]. As of 2024, anisotropically wet-etched pyramids are still a benchmark for light trapping in c-Si technology [11], because they reduce reflective losses across the whole wavelength range and are almost perfect Lambertian scatterers, enlarging the light path in the absorber. Therefore they enhance the absorption in the long wavelength range, where silicon is weakly absorbing.

For c-Si solar cells, also **inverted pyramids** were investigated [36]. Combining pyramids with small **nanocones** leads to almost perfect light trapping. Here, special attention must be put on passivating the textured surface to preserve the electronic quality of the solar cell [37].

Since the 2000s, **advanced photonic concepts** have been studied. Numerical studies suggest that nanophotonic textures can enhance absorption even much stronger than $4n^2$ within narrow spectral and angular boundaries [38–40].

Despite extensive efforts to develop various photonic textures for improved light trapping, they have typically exhibited limitations, offering enhanced light trapping only within specific wavelength ranges or narrow incident angle tolerances [28]. For thin-film silicon solar cells, **periodic structures** yielded comparable optical performance as standard random nanotextures under broadband solar irradiation [41]. In some applications light trapping is only relevant within a limited spectral range, such that the restricted wavelength range is no considerable limitation. In fact, rear side gratings have contributed to record efficiencies [42, 43].

Quasiperiodic structures enable broadband and wide-angle light trapping capabilities. In contrast to random pyramid textures, quasiperiodic photonic structures with feature sizes on the order of 100 nanometers present a viable approach also for thin film solar cell designs [44–49].

Another concept to realize strong absorption enhancement was the introduction of ***plasmonic* metal nanoparticles** that support surface plasmons, which are excitations of electrons at the interface between a metal and a dielectric [50–53]. Despite the positive effects of large-angle scattering, coupling into waveguide modes, and field enhancement, illustrated in Fig. 6e, plasmonic nanoparticles have only found restricted applications in solar cells [54–56]. For thin-film silicon solar cells, they could not outperform standard random nanotextures for thin-film [57, 58].

As an alternative approach, **dielectric nanoparticles** may be inherently stable and absorption-free while equally offering antireflection behavior, resonance effects, field localization, and light redirection [59]. They have found successful integration into different types of solar cells including e.g., thin-film Si, GaAs and CIGSe solar cells [60–63].

The tunable wavelength-selective response of photonic structures makes them attractive for tailoring the reflected, absorbed, and transmitted spectrum. However, so far only very few concepts have been able to demonstrate their potential to improve solar cell performance beyond the state of the art. Furthermore, the cost efficient production of photonic structures on large scale necessary for terawatt PV remains an open challenge.

3.3. Reducing parasitic absorption

To maximize the optical performance of solar cells, it is essential that light is predominantly absorbed within the active absorber layer. Hence, unintended absorption must be minimized in supporting structures such as antireflective coatings, textured interfaces, photonic structures, nanoparticles, reflectors, and electric contacts. For instance, parasitic absorption can by significantly reduced utilizing lowly absorbing transparent conductive oxides (TCOs) [64] like zirconium-doped or hydrogen-doped indium oxide (In_2O_3) [65, 66], and low-doped zinc oxide (ZnO) [67, 68]. Parasitic absorption in the back metal is caused by the excitation of surface plasmons and can be strongly reduced by interlayers consisting of TCOs [69, 70] and dielectrics [70].

3.4. Spectrally selective concepts

3.4.1. Semitransparency

While in most cases, reflection and transmission are to be minimized, for some applications absorption is desired only in a very specific spectral range. Partial transmission or semitransparency finds a variety of applications like solar windows, agrivoltaics, or multi-junction solar cells. On purpose, not all of the incident light is absorbed by the solar cell but the spectrum required for, e.g. indoor lighting, crop cultivation, or bottom solar cell operation is transmitted. For semitransparent solar cells, wavelength-selective optical concepts like thin-film coatings or nanophotonic concepts, as outlined above, can be used. Finally, semitransparency may also be exploited for bifacial operation [71, 72].

3.4.2. Multi-junction solar cells

In multi-junction solar cells, solar cells with different bandgaps are stacked onto each other. Besides light incoupling and light trapping, here light management has to account for a third task: optical structures that redistribute the light between the subcells, and increase the transmission of light into the bottom cell. The role of optics for multi-junction solar cells is discussed in detail in Chapter 7.

3.4.3. Spectral shaping

An effective strategy to counteract the challenges posed by the broadband nature of sunlight involves altering the incident spectrum impinging onto the solar cell, achievable through down-shifting, down-conversion, or up-conversion processes. Down-shifting involves the absorption of a high-energy photon followed by the emission of a low-energy photon. In down conversion, one high-energy photon can result in the emission of two lower-energy photons. Conversely, up-conversion entails the absorption of two or more photons that excite a state within a material, leading to the emission of a single photon of higher energy upon radiative recombination. These techniques can be integrated into layers in front or behind of the active solar cell layer, respectively, or employed within luminescent solar concentrators (LSCs) to which solar cells are attached or optically coupled through free space, as outlined in Ref. [73]. This approach not only mitigates losses due to sunlight's broad spectrum but also enhances the efficiency of solar cells by more effectively harnessing the available light. Spectral shaping is discussed in detail in Chapter 8.

3.4.4. Color appearance

With the further integration of solar modules in buildings, also *aesthetics* become more relevant. Different optical concepts have been used to make solar modules with attractive color appearances. Chapter 11 is devoted to the role of aesthetics and color for photovoltaics.

3.5. Optics for optimized energy yield

To be relevant for terawatt scale, optical concepts not only must perform well in laboratory settings under standard testing conditions, but also demonstrate enhanced performance under real-world outdoor conditions. Outdoors, light not only reaches a solar module directly from the sun but is also scattered by clouds and surroundings, resulting in what is known as scattered light, incident from various angles and with spectral distributions deviating from the standard solar spectrum.

To assess the performance of PV modules in the outdoors, the concept of energy yield (EY) is used, which is the total amount of energy harvested from a PV system installation, taking into consideration seasonal and daily variations in irradiation conditions, spectrum, temperature, as well as other relevant details of the PV system.

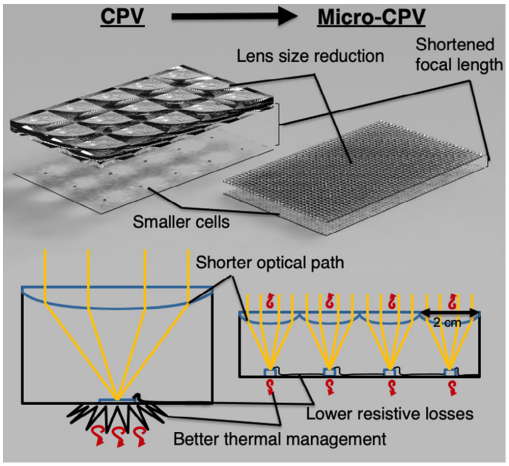

Fig. 7. Illustration of the main functional benefits of micro-CPV modules compared to conventional CPV. The reduction of the solar cell size and the optical aperture result in shorter optical paths, lower resistive losses and better thermal management. An additional benefit is more flexibility for different interconnection schemes and for tracking, which can avoid power losses generated by misalignments between solar cells and optics. (Reprinted from Ref. [77]).

An elegant solution to capture light from diverse angles is the utilization of *bifacial* solar panels, which accept light not only from the front but also from the rear. It's noteworthy that around 85% of currently produced solar cells are bifacial, and it is projected that the majority of modules will follow suit within a few years [3]. The energy yield also can be increased by texturing the module cover for improved in-coupling of radiation incident under large angles. Light-redirecting films can increase the performance from guiding light away from solar-cell edges [74]. For multi-junction solar cells, fine-tuning of bandgaps and absorber thicknesses can increase the yield under different illumination conditions.

The increased acceptance of light from different angles underscores the importance of considering ground-reflected light, known as *albedo light*. Moreover, there is potential to strategically design albedo to achieve enhanced energy yields under realistic conditions. Understanding, bench-marking, and designing the effects of albedo remain active areas of research, demanding robust optics knowledge and modeling capabilities. More details on these topics can be found in Chapter 10.

3.6. Concentrating photovoltaics

In **concentrating photovoltaic** (CPV) systems [75] direct sunlight is concentrated by factors in the range of several hundreds to a thousand, so that the amount of required energy intensive and costly semiconductor material for solar energy conversion is greatly reduced. As a consequence, CPV has shown the lowest embodied energies and fastest energy payback times of all PV technologies [76]. Moreover, the solar cell efficiency increases under concentration due to higher carrier concentrations and resulting gain in output voltage. Record efficiencies have been demonstrated with III-V based multi-junction concentrator solar cells (see Chapter 7).

In **micro-concentrating** photovoltaics [77–80] the solar-cell size is reduced to the sub-mm range, as illustrated in Figure 7. This reduction in size reduces the heat load per cell, eliminating the need for specific heat sinks and enabling the use of simple and low-cost circuit board substrates. Additionally, reduced current lowers series resistance losses and very high-voltage modules become feasible, while series/parallel interconnection schemes offer flexibility in adjusting for

cell to cell tolerances [81].

However, miniaturization also leads to an increasing influence of perimeter recombination, which is counterbalanced by high enough concentration: For a 500-µm cell and a concentration ratio of 1000 the related voltage loss is below $1\%_{\text{rel}}$ [78]. In terms of manufacturing, miniaturization requires accurate assembly and interconnection of thousands of micro-concentrator solar cells per square meter. In this regard, parallelized and/or high throughput processes from other industries, such as panel level packaging in micro- and optoelectronics, micro-/mini-light-emitting diode (LED) display technology, and advanced circuit board technologies can be applied and promise low-cost. For example, surface tension driven self-alignment [82–85] enables µm-precision without the need for accurate chip placement. In fact, the forced motion of the chip during solder melting caused by an initial displacement has been shown to even increase the self-alignment accuracy [84, 85]. For Cu(In, Ga)Se_2 microabsorbers both top-down [86, 87] and bottom-up [88, 89] fabrication processes were explored.

Another concept are **luminescent solar concentrators** (LSC), which consist of large sheets of transparent materials embedded with pigments known as dyes or luminophores. Luminophores absorb sunlight and subsequently re-emit fluorescent light, which is then guided and concentrated towards small solar cells positioned either at the back or at the edges of the sheet. This dramatically reduces the area of solar cells needed, as in traditional concentrators. Unlike conventional light concentrating methods (i.e. with lenses), LSCs can effectively concentrate diffuse irradiance, a significant component of solar radiation scattered by the atmosphere and terrestrial surfaces, and thus it eliminates the need for tracking. More details on LSCs are given in Section 8.3.

3.7. Summary

In this chapter we briefly discussed essential optical concepts for photovoltaics. After introducing *antireflective coatings* in Section 3.1, we discussed *textured interfaces and structured materials* in Section 3.2 and *parasitic absorption* in Section 3.3. Then, we elaborated on *spectrally selective concepts* in Section 3.4, looked at optimizing the *energy yield* in Section 3.5 and concluded the chapter with optics for *concentrating photovoltaics* in Section 3.6. The concepts presented in this chapter establish a foundational understanding that will support the advanced topics explored in the subsequent chapters.

4. Eco-design for solar cells by using earth-abundant optical materials

D. MUNOZ, H SAI, T. GAGEOT, W. FAVRE

4.1. Introduction to eco-design

Eco-design is defined by the International Organisation for Standardisation (ISO 14006, 2011) [90] as "the integration of environmental aspects into the design and development of products, with the aim of reducing negative environmental impacts throughout the life cycle of a product". Therefore, eco-design is an approach that reduces the negative impacts of a product throughout its life cycle while maintaining its quality of use (cost, technical performance, etc.). Adopting an eco-design approach consists in three steps [91]. Firstly, an environmental assessment is necessary to provide a good initial understanding of the environmental problems caused by the reference product. Secondly, eco-design strategies are suggested to reduce the environmental impacts in the development of the new solution. Finally, these strategies need to be validated from social, technical, and economic points of view. It is important to highlight that the eco-design is not limited to environmental evaluation but must also include strategies to improve the product before production.

The life cycle assessment (LCA) approach allows for the assessment of environmental impacts by using relevant and appropriate information about the product for each phase of its life cycle: raw material extraction, manufacturing, distribution, use, and end of life. The carbon footprint is one of the many output parameters [92].

4.2. Eco-design definition in PV

Regarding PV technology development, carbon footprint reduction is key but depends mostly on the energy mix in the production country [92], which has little impact on technology design. On the contrary, raw material use is extremely relevant in the design phase. The eco-design criteria defined by the French government consider the reduction of critical raw material (CRM) as a mandatory step for the eco-design approach (among others). Several CRMs as assessed by the European Commission [93] are used commonly in PV. Their criticality is defined according to supply risk and economic importance, some examples are shown in Table 1, which also includes a composite index for a global ranking of critical materials as defined by the International Renewable Energy Agency (IRENA) [94].

As shown in Table 1, indium, which is commonly used in heterojunction (SHJ), thin film, and perovskite solar cells, is the most critical material today, followed by copper and silver. Metal silicon is a CRM because of its economic importance, supply risks, and significant environmental impact during production, even though silicon is among the most abundant elements. The challenges of PV community today are to reduce or even replace these materials with more abundant ones and to ensure their 100% recyclability in the context of an rapidly growing demand for the upcoming years.

4.3. High efficiency solar cells and raw materials limitations

Crystalline silicon (c-Si) solar cells dominate the current PV market, and this trend is expected to continue in the coming decades, whether in single junction or tandem configuration. To date, the highest efficiency among various types of c-Si solar cells has been achieved with SHJ architecture [11].

One of the optical functional materials used in SHJ cells is transparent conductive oxides (TCOs), which provide both high light transmittance and high electrical conductivity simultaneously. TCOs are also important building blocks for thin-film solar cells including metal-halide perovskite and perovskite/c-Si tandem cells. The most common TCO material is indium oxide. In_2O_3-based TCO offers the best opto-electronic performance among various TCOs, but as a CRM,

Table 1. Supply risk and economic importance for different critical raw materials (CRM) used in PV technology, as assessed by the European Commission in 2023 [93]; and a composite index for a global ranking of critical materials, as defined by the International Renewable Energy Agency (IRENA) in 2024 [94]. A larger number means a larger supply risk, economic importance, or criticality, respectively.

Material		Supply risk	Economic importance	Composite index
Indium	(In)	0.6	2.6	0.68
Copper	(Cu)	0.1	4.0	0.52
Silver	(Ag)	0.8	4.6	0.49
Silicon metal	(Si)	1.3	4.9	0.40
Cadmium	(Cd)	0.2	4.1	0.38

it significantly limits the production capacity of SHJ, perovskite and perovskite/c-Si tandem cells [95]. In response to this issue, R&D toward In-lean or In-free SHJ cells is currently underway to pave the way for the massive industrialization of the technology, as discussed in section 4.3.1. The concern about silver (Ag) usage pertains to the metallization of all silicon based solar cell technologies, as the demand for this element in PV manufacturing has already reached 13% of the global demand [96]. The PV community is following a similar strategy for reducing In usage: both Ag usage reduction or complete replacement are being explored through different technological approaches, as discussed in section 4.3.2. Regarding silicon, many improvements are ongoing to reduce and optimize material use (thickness, kerf loses, recycling, etc.), and proposals for the next technology of direct wafer manufacturing are being explored. However, this is beyond the scope of this work. The usage of poly-Si for a Si PV cells has decreased from 6.8 g/W in 2010 to 2.3 g/W in 2022 [97].

4.3.1. Indium concerns & optical improvements

Figure 8 summarizes the state of the art of the conversion efficiencies of SHJ solar cells as a function of indium (In) reduction in TCO layers. The highest efficiency of front/back contact SHJ cells is 26.8%, achieved by Lin *et al.* with In-rich TCOs on both sides [11], as plotted in the top left corner of this figure. Other reference cells with In-rich TCOs are also aligned at an In fraction of 100%, with a wide range of efficiencies [98–100].

There are several approaches for reducing In consumption in SHJ cells. The simplest approach is to replace In-rich TCOs with In-free TCOs, such as ZnO-based [103, 109, 110, 114–119] or SnO_2-based [108, 120] TCOs (In-free approaches). Another approach is to reduce the thickness of In-rich TCOs (In-lean approach) [70, 101–113]. In this approach, thin In-rich TCOs are combined with dielectric layers or other TCOs to meet optical requirements, such as anti-reflection effect on the front. The advantage of this approach is the possibility to leverage the extensive knowledge about standard In-rich TCO-based SHJ cells, though it still requires a certain amount of In. Another interesting approach to eliminate In consumption is TCO-free solar cells, which do not incorporate any TCO layers, whether In-based or not [121–123]. All approaches can be applied either one side or both sides of the cells. Hereafter, we discuss these approaches. It should be noted that hetero back-contact (HBC) approach [14, 124, 125] is also regarded as an In-lean SHJ cell since it does not use any TCOs on the front side. However, it is out of scope in this section due to the additional technological difficulties of rear-side fine patterning.

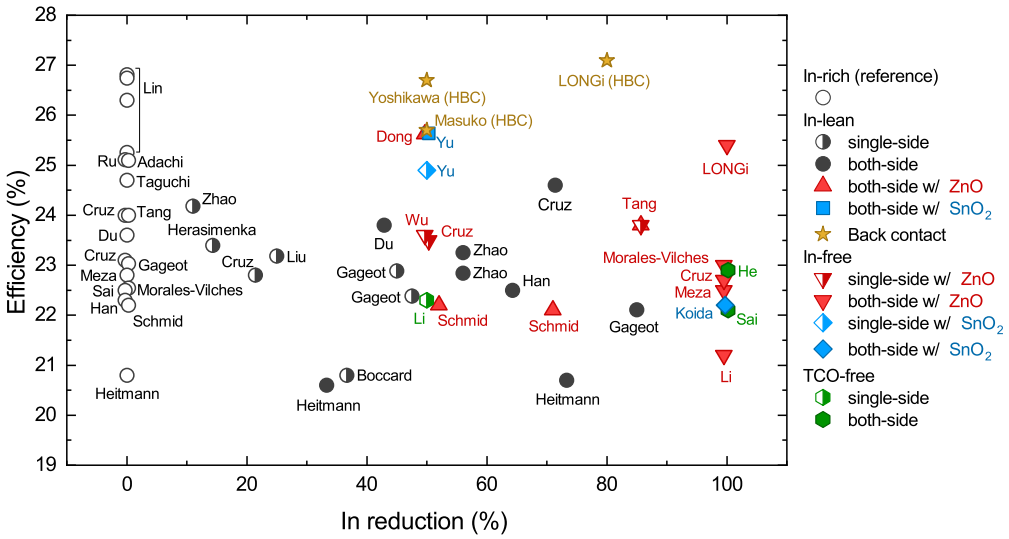

Fig. 8. State of the art of the conversion efficiencies of SHJ solar cells as a function of In reduction in TCO layers. Symbols at In reduction = 0% indicate benchmark SHJ cells with In-rich TCOs [11, 98–100]. The different symbols indicate different approaches to reduce In consumption in SHJ cells: thin In-rich TCOs with dielectric layers or other TCOs [70, 101–113], In-free TCOs (ZnO or SnO_2) [103, 108–110, 114–120], and TCO-free SHJ cells [121–123]. All the approaches can be applied either one side or both sides of the cells. 100% In-reduction means completely In-free SHJ cells. Hetero back-contact (HBC) approach [14, 124, 125] is also regarded as an In-lean SHJ cell as it does not use any TCOs on the front side. The name next to each symbol indicates the first author of the corresponding publication.

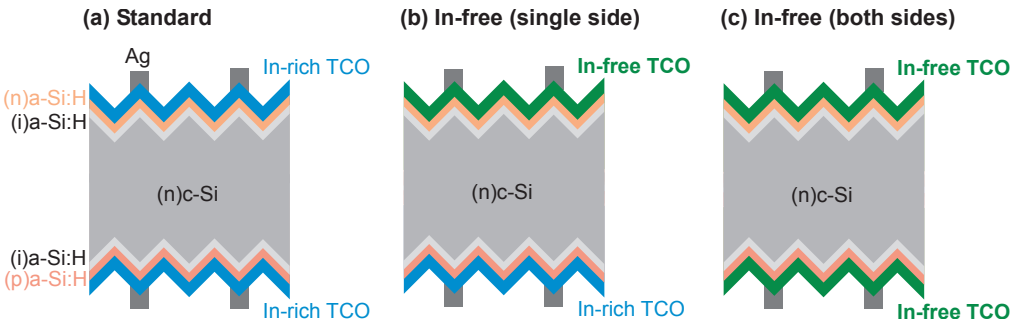

Fig. 9. Schematic illustrations of SHJ cells with In-rich TCOs on both sides (a), In-free TCO on single side (b), and both sides (c).

a) In free TCOs Here, we discuss the study of replacing the TCO on one or both sides of the SHJ cell with an In-free TCO, as schematically shown in Fig. 9. This family of In-free materials mainly concerns ZnO-based and SnO_2-based materials [64]. Zn has a much larger resource availability than In, and therefore ZnO-based TCOs have been expected and developed as an In substitute material for many years [126]. An important advantage of ZnO-based TCO materials is that high conductivity TCOs can be obtained by low-temperature processes such as sputtering, similar to In_2O_3-based materials, though they are slightly inferior to In_2O_3-based materials in terms of opto-electronic properties. This is crucial to apply TCOs to solar cell devices with low heat resistance, such as SHJ cells and perovskite cells. In SHJ cells, many groups have reported studies on the use of Al-doped ZnO as a TCO. In fact, high initial efficiencies comparable to those of In_2O_3-based TCO have been reported, as shown in Fig. 8 as the downward triangle symbols [103, 109, 110, 114–119]. In-free AZO-based SHJ cells with efficiencies of 21.2–23% were reported in 2019 [103, 115–117]. Recently, an excellent example of In-free ZnO-based SHJ cell with an efficiency of 25.4% was reported by LONGi [119].

However, a problem inherent to ZnO-based materials is their weakness to moisture and poor long-term stability. Therefore, ZnO-based SHJ cells have not been commercialized yet. As described later, the chemical stability of ZnO-based TCOs can be improved by capping with In_2O_3-based ones, compared to ZnO-based alone. Alternatively, there is an approach to compensate for this lack of chemical stability in the module sealing technology. In fact, a double glass structure is used to achieve robust sealing in thin-film Si solar cells [127] and CuInGaSe solar cells [128] that were commercialized using ZnO-based TCO. For full-scale commercialization, further research is expected to improve the optoelectronic properties and chemical stability.

SnO_2-based TCOs can also be interesting to replace In_2O_3-based ones. Indeed, SnO_2-based TCOs (SnO_2:F, SnO_2:Sb and SnO_2:Ta) are excellent TCO materials and widely used in various applications, including thin-film Si and CdTe solar cells [129, 130]. Such SnO_2-based TCO films are typically deposited by CVD or sputtering at high temperatures of 400–600°C. The resulting film is polycrystalline with excellent chemical stability. However, the electrical properties of the SnO_2-based film decrease significantly when the deposition temperature is lowered [131] Therefore, SnO_2-based TCOs have not yet been applied to temperature-sensitive devices such as SHJ and perovskite/Si tandem cells. Recently, it has been reported that amorphous SnO_2 (a-SnO_2) can achieve high transparency and reasonable electrical properties even at low-temperature deposition. a-SnO_2 films deposited by reactive plasma deposition (RPD) method have shown resistivity in the order of 10^{-4} Ωcm [120]. The potential of In-free a-SnO_2-based SHJ cells has demonstrated by a lab-scale SHJ cell with a-SnO_2 films on both of front and rear sides by Koida et al [120] as plotted as the blue diamond symbol in Fig. 8. Moreover, the development of a-SnO_2 films by sputtering method is also progressing. Although the resistivity is still higher than that of RPD method, a RJ SHJ cell with sputtered a-SnO_2 on the front side with an excellent efficiency of 24.9% was reported by Yu et al [108] as plotted as the half-filled blue square (In reduction = 50%) in Fig. 8. One advantage of SnO_2 over ZnO is its high tolerance to humidity, which leads to long-term stability for solar cell applications [120].

In short summary, the research and development of TCO materials without In, such as ZnO-based and SnO_2-based materials, is steadily progressing. For the relaxation of resource constraints, early commercialization of c-Si solar cells and perovskite/c-Si tandem solar cells with these materials are expected. Today, those TCOs raise issues with poor contact with Ag or a-Si:H [109, 117, 118, 132], FF losses [109, 110, 112, 117, 118, 132], higher sputtering damage leading to lower V_{oc} [109, 110, 112, 132, 133], lower J_{sc} [109, 110, 112, 118, 132], and poor reliability against humidity [109, 117] compared to In-rich TCOs. Potentially, SnO_2-based TCOs are supposed to be more reliable than ZnO-based ones from the material point of view, but this must be confirmed by extensive reliability tests.

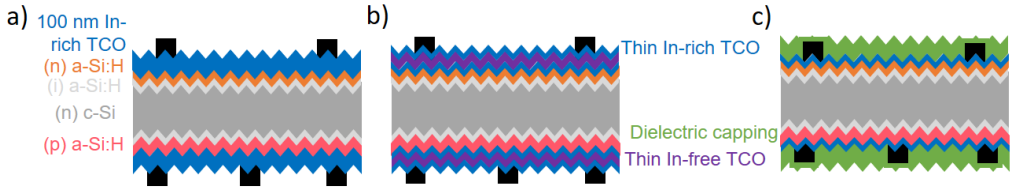

Fig. 10. a) classical SHJ cell, b) In-free + In-rich TCO multilayer cells and c) Thin In-rich + dielectric layer or multiple anti-reflective coating). Note that the TCO changes are represented on both side of the cells, which is not the case in all the cited studies.

b) In lean approach To overcome issues with In-free TCOs, other approaches have been studied in recent years, such as multilayer anti-reflection coatings. Indeed, it is also possible to reduce the indium content by reducing the In-rich TCO layer thickness. On the rear side, the thickness can be lowered by 60% without efficiency losses [134]. However, on the front side, since the TCO acts as an anti-reflection coating, the thickness reduction needs to be compensated by adding another layer. In this case, two different approaches exist:

In-free + In-rich TCO multilayer To circumvent the poor contact of AZO with *a*-Si:H layers, some studies added a thin In-rich layer between the two layers, as shown in Fig. 10(b) [109, 110, 112, 132, 135, 136]. When the In-rich contact layer is used below the AZO layer, it also protects the *a*-Si:H layer from the higher sputtering damage of AZO. On another hand, to cope with the poor damp heat reliability of pure AZO and allow a better contact with the Ag grid, a thin In-rich TCO layer can be used as a capping layer, thus providing a barrier against humidity [109]. By using two contact layers, Tang et Al. reached efficiencies as high as 23.6% (compared to 23.7% for the ITO references) with an 85% In reduction [110]. Dong *et al.* achieved an impressive certified cell efficiency of 25.62% with a 50% In reduction on the front side (only an In-rich contact layer between the selective layer and the AZO layer) [112].

Thin In-rich TCO + dielectric layer or multiple anti-reflective layer Another solution is to use a completely transparent but non-conductive layer as a dielectric layer (SiN_x, $SiON_x$, SiO_x, MgF_2 or AlO_x) [70, 101, 102, 105–107, 113] to compensate the thickness reduction of the TCO layer as shown in Fig. 10(c). Using this solution, the lateral transport is carried out only in the thinner TCO layer (and in the substrate), so optimization of the thinner TCO towards high conductivity is necessary to avoid fill-factor losses. Indeed, since the sheet resistance is inversely proportional to the thickness, a thinner TCO leads to higher sheet resistance. It must be noted that the deposition of a hydrogen-rich dielectric can improve the underlying TCO electrical properties by hydrogen doping: the resistivity of the TCO layer can be reduced by up to a factor 3 [101, 113]. On the other hand, since dielectric layers are more transparent than TCOs, current gains can compensate for small FF losses: the thinner the TCO layer, the lower the parasitic light absorption. Thus, a compromise between FF losses and current gains will dictate the thickness reduction potential. It was also shown that a dielectric capping can improve the damp heat reliability of the cells [104, 113, 137] and that in some case, the thinner ITO layers can show an enhanced UV reliability [113]. Using this type of architecture, Cruz *et al.* [70] reached a remarkable cell efficiency of 23.9% (while the 100% In rich TCO reference is 0.2% lower) using a 20 nm thick In-rich layer on both sides and a SiO_2 capping layer. Another recent study showed that lowering the TCO thickness on the rear side below 20 nm affects dramatically the efficiency, but that it is possible to use ITO layers as thin as 10 nm on the front side without efficiency losses (90% In reduction) [113].

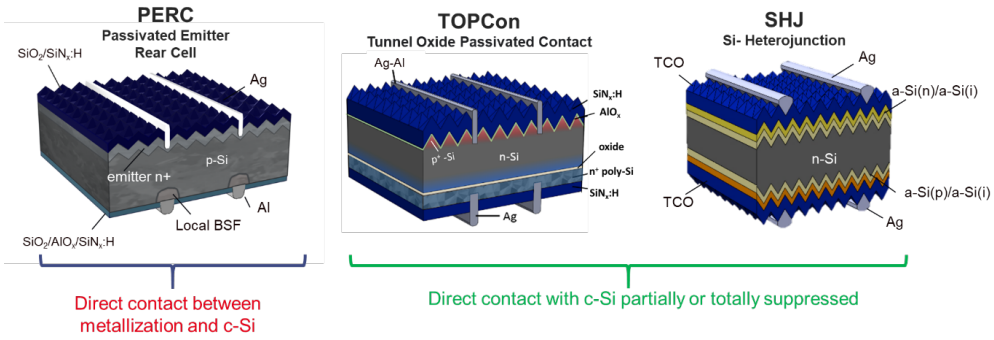

Fig. 11. Representation of bifacial PERC, TOPCon and SHJ devices and corresponding layers, including metallization approaches with direct, partial or no contact with the silicon absorber.

c) TCO free approach The last approach we discuss here is TCO-free solar cells, in which no TCO layers are used, regardless of whether they are In-based or not. This might be a promising approach in SHJ solar cells because the photo-generated carrier density in c-Si cells under illumination becomes rather high by applying state-of-the-art passivating contact technologies such as SHJ. Therefore, the sheet resistance of the base c-Si wafer can be low and comparable to that of TCO layers [138]. In such a situation, the lateral carrier transport could be supported by the c-Si wafer itself without the help of TCO layers. Besides, a TCO-free approach is attractive for cost reduction since the TCO deposition process occupies a non-negligible portion of the production cost of SHJ cells.

TCO-free approach was first demonstrated by Li *et al.*, showing an efficient rear-junction SHJ cell with a TCO-free front contact structure [121]. In addition, He *et al.* took one step further and realized TCO-free SHJ cells using dopant-free contacts on both sides [122]. Sai *et al.* also developed both-side TCO-free SHJ cell with an initial efficiency of > 22% [123]. In that work, it was found that low contact resistivity at carrier selective contacts is more crucial in TCO-free SHJ cells than in normal SHJ cells. It was also pointed out that TCO-free cells suffer from metal diffusion into Si layers, which deteriorates the long term photovoltaic performance of SHJ cells. These results suggest that TCO-free SHJ cells with a high initial efficiency are achievable, and many examples for TCO-free devices are given, but issue of stability was not discussed. New metallization process/architecture are required to solve this reliability problem in the future.

4.3.2. Silver concerns

Metallization of c-Si based solar cells must allow charge carriers collection and transport up to the interconnection ribbons or wires while ensuring low recombination, resistive and optical losses, and be reliable under thermal and mechanical stresses. The mainstream process for metallization is screen-printing using conductive pastes, which are a mix of metallic particles, solvents and other components depending on the cell technology. For high-temperature Si devices like Passivated Emitter and Rear Cell (PERC), with dielectric passivating layers (SiO_x, SiN_x:H, AlO_x), etching agents are needed to ensure a connection to the silicon through these insulating layers (activated during the firing step). Al-Ag based pastes enable contact on p-type silicon, while Ag based pastes are used for contact on n-type Si [139]. For high efficiency cells technologies such as Tunnel Oxide Passivating Contact (TOPCon) and SHJ, there is a limited (TOPCon) or no (SHJ) direct contact with silicon, which allows for drastically reducing recombination losses and achieving higher open-circuit voltages (V_{oc}) [140]. In the currently developed TOPCon technologies, both front and rear sides of the device are contacted with pastes

involving a high temperature firing step. For SHJ, both sides' metallization the deposition is on top of TCO layers, followed by drying and low temperature sintering steps (<200°C). A major drawback of this technology is the higher silver content compared to higher curing temperature pastes. The schematic illustrations of PERC, TOPCon, and SHJ cells are shown in Fig. 11.

PERC devices use Al on the rear side and Ag on the front side [3]. TOPCon and SHJ require different metallization-paste properties, leading to increased Ag usage, with typical laydown of 160 mg and 200 mg, respectively. Table 2 summarizes the metal content in these mainstream devices considered as M10 size in 2022.

Projections on silver demand for the PV sector to meet the net-zero emission by 2050 underline the need to drastically limit the silver content per cell, with an upper limit proposed at 5 mg/W and corresponding Ag demand upper limit at 5 kt/a [96].

Table 2. Aluminum and Silver usage for the different silicon based solar cells mainstream technologies as taken from Ref. [4] for year 2022 as reference. The area is 330.69 cm^2 (M10 wafer size) for all, m and c in the table stand for "mass" and "content per watt" respectively.

	Efficiency (%)	Power (W)	m_{Al} (mg)	c_{Al} (mg/W)	m_{Ag} (mg)	c_{Ag} (mg/W)
m-PERC	23.2	7.7	900	117	84	11
b-PERC	23.2	7.7	300	39	84	11
TOPCon	23.9	7.9	0	0	160	20
SHJ	24.2	8.0	0	0	200	25

Metal laydown using screen-printing technique has been significantly reduced in recent years, mainly due to an increase in the number of busbars (BB). This strategy allows for the deposition of narrow fingers (improving shadowing) with higher line resistance, as the charge carriers will be transported over shorter distances. The transfer of metal particles through narrow screen openings could lead to non-conform or cut lines, but the development of knotless screens with new emulsions enables the processing of lines less than 20 µm in width. Current technologies generally use 9 BB to 12 BB for M10 devices, and some suppliers are expected to release products up to 24BB for G12 wafer size soon. Reducing the silver content at the fingers level implies a greater metal usage for the busbars, increasing the complexity and costs for interconnection and metal consumption at the module level (more ribbons or wires). At some point, this becomes detrimental to photon collection by the PV module, as more ribbons or wires generate more shadowing, even with specific non-flat structures (see Chapter 3). Furthermore, the module reliability can be impacted by the most aggressive metal laydown.

Alternatively, interesting results have been found for TOPCon with direct contact of new Al based pastes compatible with n+ poly-Si or lines deposited in two steps: (i) Ag paste dots in contact with the poly-Si layer (ii) a copper full line on top [141]. For SHJ, metal pastes loaded with Ag coated Cu particles have recently attracted much attention, as they are compatible with screen-printing and can reduce Ag lay-down by more than 40%. Integration of such pastes at the rear side or on both sides in 6BB SHJ devices shows that it is possible to reduce the Ag content by 30% with only a slight impact on efficiency. Thus, 11 mg_{Ag}/W is reached with less than 0.3% absolute efficiency loss, as presented in Figure 12. These results are very promising, and efficiency loss related to higher line resistances (compared with the pure Ag ones) can be reduced using higher quantity of BB or busbar-less designs.

Alternatives techniques for metallization of Ag pastes, allowing narrow fingers with high

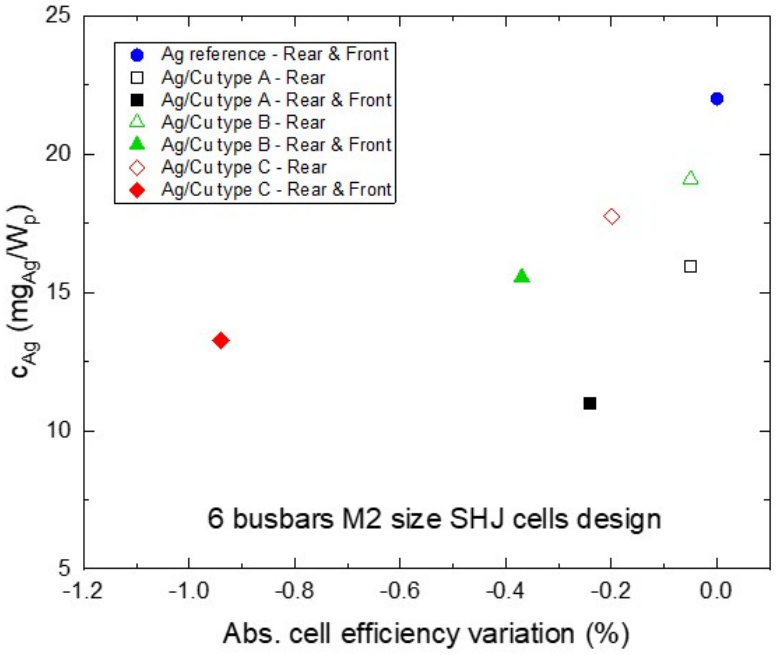

Fig. 12. Influence of Ag content reduction in Ag coated Cu low curing temperature pastes on relative efficiency for 6 busbars SHJ devices prepared on CEA SHJ pilot line. The reference (blue symbol) is a standard Ag paste and the Cu/Ag pastes have been applied only at the rear side (open symbols) or on both sides (solid symbols).

aspect ratio, such as Pattern Transfer Printing (PTP) also referred as Laser Transfer Printing (LPT), Dispensing, Rotary printing and Inkjet printing have been proposed [139, 142]. While the LTP has been used to allow front side shadowing lower than 2% and reach record efficiency for SHJ devices, their compatibility with high throughput and reduced silver usage still needs to be demonstrated [143].

Copper plating processes for Si based solar cells allow for reducing or removing Ag usage. Several works show possible process flows compatible with the different existing Si cells technologies and record efficiencies. The higher cost of this metallization technique compared to screen-printing, together with possible process issues such as parasitic plating and reliability losses, are some of the points preventing its entrance into mass production [144–146]. It is worth noting that in the approaches involving the usage of Cu, its diffusion into silicon must be avoided as it could cause strong reliability issues (local shunts, bulk lifetime degradation). Laser contact opening (LCO) process optimization or the presence of a barrier such as TCO for SHJ are possible strategies for this purpose. There may also be a need to have the Cu metal layer covered by another metal, as its oxidation could strongly affect its conductivity and color, and also lead to reduced module reliability. Finally, moving to Interdigitated Back solar Cells (IBC) technologies enable to suppress entirely front side reflections due to metallization and some have already demonstrated their compliance with strong Ag reduction [12, 147].

4.4. Summary and Advances needed

In conclusion, considering the impressive trend of solar PV installations reaching ≈ 1.5 TW worldwide in 2023 [97], the PV community needs to rethink PV solar systems based on an eco-designed approach where efficiency, reliability and environmental constraints are mandatory. This means that strategies for CRM reduction (or removal) should be at the core of research and innovation activities in the lab to make these processes and technologies possible. Moreover, designing for 100% recyclability is also necessary to maximize material recovery in a circular ecosystem for PV. In the future, the optical challenges in this context can be summarized as follows:

CRM reduction or removing Reduction or alternative technologies for CRMs used in mainstream crystalline silicon solar cells and modules. Typically, the development of device and module technologies that reduce Ag, In, Bi, etc., are required. As for optoelectronic materials, urgent tasks include the development of low-temperature-formed TCO materials with reduced or no In, applicable to heterojunction solar cells and perovskite/Si tandem solar cells, control of interface properties, and verification of long-term stability.

Recycling technologies Recycling technologies for PV modules, or the development and dissemination of PV modules that are easy to recycle. In relation to optics, laser processes are widely used in the manufacturing process of solar cells, and efficient module disassembly technologies utilizing lasers are also an interesting research subject.

5. Luminescence I

P. MANLEY, U. AEBERHARD, M. LEDINSKY, S. BURGER

5.1. Introduction

This chapter covers luminescence, the light leaving the cell or sub-cell of a multi-junction device. We will see that the luminescence of a solar cell gives us insight into both the electrical and optical properties. Furthermore, internal luminescence can be exploited to increase the voltage in single junction solar cells and the current in multi-junction solar cells via the luminescent coupling effect.

5.2. Luminescence

In the detailed balance analysis of Shockley and Queisser many loss channels are assumed to be negligible in order to obtain upper limits of solar cell performance [22]. One loss channel that cannot be set to zero is the emission of photons from the solar cell, called luminescence. This is due to the fundamental reciprocity between absorption and emission [148]. For light to enter the solar cell, we must allow for the fact that it will also be able to leave the solar cell. An interface that is perfectly transmissive for light from one direction and perfectly reflective from the other direction requires rather exotic physics and is not applicable to a solar cell [149, 150]. Secondly, if we allow that light can be absorbed in the solar cell, thereby producing an electron-hole pair, it must be possible for electrons and holes to radiatively recombine and emit light [22].

When an ideal solar cell is illuminated under open circuit conditions, all of the generated electron-hole pairs recombine radiatively and produce luminescence. In reality, both Auger and Shockley-Read-Hall (SRH) recombination will lower the amount of luminescence by non-radiative recombination [151, 152]. The luminescence is a measure for how close our real system is to an ideal one. By increasing the measured luminescence of a solar cell operating at open circuit, we imply that the non-radiative recombination rates have been reduced in comparison to the radiative recombination rates [148].

The real-time monitoring of luminescence may serve as a direct indicator of the evolution of defect states contributing to non-radiative recombination during the growth or crystallization of semiconductor thin films. A notable example involves the utilization of combined in-situ photoluminescence and grazing-incidence wide-angle X-ray scattering (GIWAXS) measurements for investigating the deposition of halide perovskite films through the solution process [153]. The findings allowed for the delineation of two distinct stages in halide perovskite growth. The initial stage is characterized by the rapid growth of individual perovskite grains, as revealed by GIWAXS, accompanied by a linear increase in the luminescence signal. In contrast, the second stage exhibits a significant decrease in growth speed detected by GIWAXS, coupled with a pronounced quenching of the luminescence signal. This phenomenon arises from the formation of grain boundaries when the individual grains begin to interconnect. Grain boundaries, being regions of high defect density, result in a substantial quenching of luminescence by two orders of magnitude due to non-radiative recombination. Interestingly, similar observations have been made through in-situ measurements of evaporated halide perovskite [154] and films prepared using so called pizza oven deposition [155].

Due to the wealth of information that is gained from the spectrum, overall intensity and lifetimes of the photoluminescence from a solar cell, this will become a key characterization technique, especially for high efficiency devices.

5.3. Radiative efficiency

The external radiative external efficiency η_{ext} of a solar cell is the ratio of the external emission rate R_{ext} to the combined total of the external emission rate and non-radiative recombination rate

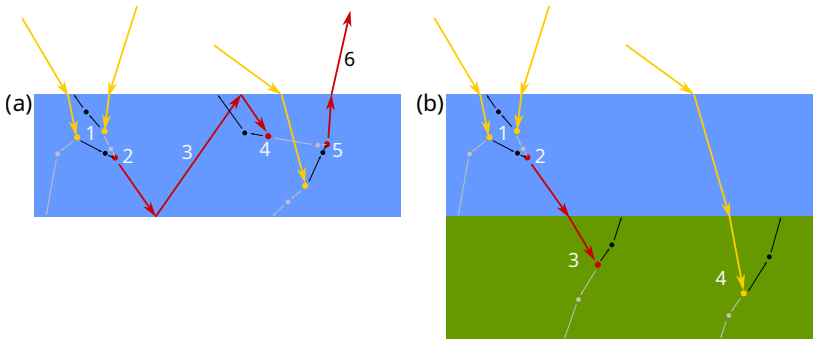

Fig. 13. Schematic description of (a) photon recycling and (b) luminescent coupling in solar cells at the operating voltage. (a)(1) Solar radiation (yellow arrows) incident to the solar cell (blue) is absorbed, generating electron hole pairs. Some charge carriers are collected at the contacts. (2) Some charge carriers recombine to emit luminescence (red arrows). (3) Depending on the emission angle, the luminescence can be trapped via total internal reflection. (4) The corresponding internal photon may be reabsorbed creating a new electron hole pair. (5) Another recombination event leading to (6) a photon that is extracted via luminescence. (b) Steps (1-2) are the same as in (a). (3) Due to low reflection between the upper (blue) and lower (green) absorber, the internally emitted photon is able to enter the lower absorber and to generate an electron hole pair. (4) Some fraction of the incident solar radiation will also reach the lower absorber.

R_{nonrad},

$$\eta_{\mathrm{ext}} = \frac{R_{\mathrm{ext}}}{R_{\mathrm{ext}} + R_{\mathrm{nonrad}}}. \tag{1}$$

Increasing the external radiative efficiency, which is primarily achieved by reducing the non-radiative recombination rates, will reduce the voltage loss of the solar cell at open circuit, V_{oc}, compared to the ideal radiative open circuit voltage $V_{\mathrm{oc,rad}}$,

$$V_{\mathrm{oc}} = V_{\mathrm{oc,rad}} + \frac{kT}{q} \ln \eta_{\mathrm{ext}}, \tag{2}$$

where kT/q is the thermal voltage. The open circuit voltage is determined by the quasi-Fermi level splitting in the absorbing material upon illumination, which in turn depends on the density of generated charge carriers and recombination mechanisms [152, 156]. When charge carriers recombine radiatively, their emission with respect to the angle inside the absorber may be isotropic, in-plane, or out of plane polarized, depending on the material system and photonic environment. Due to the higher refractive index of the absorbing layer compared to the exterior, some of the internal emission is trapped within the device due to total internal reflection. This is reabsorbed to create an electron-hole pair, which restarts the cycle that is also termed *photon recycling*. A schematic overview of this process is given in fig. 13(a), which does not show non-radiative recombination effects present in realistic devices. Note that fig. 13(a) represents operation at a voltage below V_{oc} as some carriers are collected at the contacts. For planar layers, most of the internal emission is trapped due to the very small escape cone [148]. This leads to a higher photon density inside the absorbing layer, resulting in a higher charge carrier density. As previously established, this will directly increase the V_{oc} [157, 158]. This effect has been studied in GaAs, Si and Perovskite devices [159–162]. Due to weak absorption at the band edge, Auger recombination in crystalline silicon is dominant, and thus the radiative efficiency remains far from the ideal limit [151].

The V_{oc} of a solar cell can be brought closer to the ideal value by an optical design that more readily traps light inside the absorbing layer. This requires large η_{ext}, since otherwise the photon

and charge carrier densities do not significantly build up with repeated emission and reabsorption events. For low η_{ext}, the energy is instead lost as heat. The optical design must also not trap light for those angles corresponding to the external solar illumination, otherwise light would not be able to enter the solar cell. In order to reach the efficiency limit for single junction devices, the optical design must also take into account the photonic environment for light emission inside the absorbing layer. This involves including a high reflectivity rear side with low parasitic absorption (favouring dielectric mirrors over metallic reflectors), suitable modification of the front side to provide anti-reflection in the narrow band of angles that receives solar radiation and high reflection of all higher angles [148, 158, 163]. Such a system would be suitable for very low levels of diffuse light and would require a two axis tracking system. Chapter 10 contains a discussion on modelling the diffusivity of sunlight based on average local weather conditions and including aspects such as tracking into cost calculations.

5.4. Luminescent coupling

Multi-junction solar cells have two or more layers absorbing sunlight. Typically, they are arranged from front to back in descending band-gap energies. This allows all of the light with energies below the band gap to be naturally transmitted to the underlying cells. In such a configuration, the luminescence produced by each sub-cell will also be absorbed by the underlying cells but not by those that are closer to the front. If the luminescence from a sub-cell is absorbed by a lower lying sub-cell, it will contribute as an extra illumination source, thereby increasing the current in the lower lying sub-cell. This process is called luminescent coupling and is shown schematically in fig. 13(b). Note that the extra current in the underlying sub-cell comes from the incomplete conversion of absorbed light to current in the upper sub-cell. The luminescence absorbed in the lower lying sub-cell will undergo thermalization of the charge carriers that reduces the energy yield. Despite this, it is still preferable for the luminescence of sub-cells to be absorbed by lower lying sub-cells rather than to be emitted to the environment. This effect has been experimentally verified in high quality multi-junction systems, typically involving III-V materials [164, 165], but also in perovskite tandems [166].

Chapter 7.1 describes the challenge of current matching in series connected multi-junction devices. This requirement is easily met for a given illumination spectrum, incidence angle distribution and temperature. Under real world conditions, the solar irradiance will change its angular spectrum throughout the day and year. Cloud cover may dramatically reduce the intensity, spectral weighting and angular distribution of the solar irradiance. Furthermore, the temperature dependence of the current and fill factor will generally not be equal for the two sub-cells. Due to overall current being limited to the lowest current of all sub-cells in a multi-junction device, such fluctuations in the illumination or temperature can reduce the overall efficiency much more than for a single junction.

The voltage increase due to the external radiative efficiency has also been studied for multi-junction solar cells [167]. The key challenge here is to include wavelength selective reflectors to confine the luminescence for each sub-cell while allowing the transmission over photons with lower energies.

Luminescent coupling may act as a stabilising effect to counteract fluctuations in the illumination [168, 169]. Often, these fluctuations cause an absorption that is too high in the higher lying sub-cells and a too low absorption in the underlying sub-cells. If the conversion of absorption into current in the upper sub-cell is incomplete, it may luminesce and emit light to lower lying sub-cells. Thereby directly increasing the absorption there, as shown in fig. 13(b). Note that this also requires a high radiative efficiency in the upper sub-cell. Additionally, the photonic environment should be constructed to allow light to be preferentially emitted to lower lying sub-cells. For a two junction solar cell this is usually the case as the refractive index of the lower lying cell is much higher than that of air outside the device. This means the escape

cone for light is much larger for emission to lower sub-cells. For devices with more than two junctions, the situation is significantly more complicated, and requires a careful design to ensure the luminescence is primarily directed downwards to increase the luminescent coupling.

By tailoring the amount of luminescent coupling, the current in a multi-junction device can be more easily balanced. This can directly raise the efficiency under ideal conditions, i.e. a clear day with the sun at the optimal azimuth and altitude, in the case of a bottom-limited device, for instance a perovskite-silion tandem with insufficient primary photogeneration in the low-absorbing silicon sub-cell. Luminescent coupling can also reduce the efficiency drop seen for non-ideal conditions, i.e. cloudy day or sun at a non-optimal azimuth and altitude. To quantify the effect of luminescent coupling under ideal and non-ideal conditions, it should be included in energy yield models discussed in chapter 10. This includes modelling of both the electrical and optical properties [170, 171].

5.5. Modelling internal emission

We have seen that modelling the luminescence of solar cells is crucial for reaching the highest efficiency devices. There is a lot to gain by an optical design that preferentially manipulates the luminescence. To achieve such an optimal design, modelling tools are required. Approaches present in the literature have handled the light emission via ray optics with either planar interfaces or approximations to structured interfaces using the idealised Lambertian scattering law [172]. For structures much larger than the wavelength of light, a ray optical picture is appropriate. An approach based on first determining the scattering matrix of such an interface and using this to determine the self-consistent internal field of the absorbing layer can model the radiative efficiency. With knowledge of the SRH recombination rate, the Auger coefficient for the material and the angular dependent rear reflectivity, the luminescence at open circuit can be determined. This directly relates how close the device V_{oc} is to the ideal limit. If the absorbing layer is thick compared to the internal wavelength, interference effects may be neglected. For thin films, the escape probability will be dependent on the position of the photon emission within the absorber due to phase effects.

If the device structuring is on the same order or below the size of the internal wavelength, rigorous simulations are needed to realistically model the wave optical nature of light. Due to the stochastic nature of the internal light emission, we may treat individual emission events as independent from and incoherent with one another. A wide-spread model to describe the characteristics of light emission in thin-film optical cavities is dipole radiation theory [173, 174], heavily used in the fields of organic light emitting devices (OLED) [175, 176] and of the emerging perovskite LEDs [177, 178]. Assessment of photovoltaic performance at the radiative limit - which includes consideration of photon recycling - requires quantification of both, internal emission and external light-outcoupling [179]. Conventionally, internal emission and re-absorption is evaluated by measuring the power dissipated by a radiating dipole in the active medium, while the out-coupled flux is measured via the Poynting vector of the electromagnetic fields generated by the radiating dipoles [180]. In contrast to the situation in optically bulk-like media, where the Van Roosbroeck-Shockley relation linking absorption coefficient and local emission rate can be used [172, 181], the internal emission in thin films depends on the local density of photon states in the cavity. A consistent description regarding dependence on the cavity modes of both, internal emission rate and external flux is found on the basis of the electromagnetic Green's tensor of the dipole fields [180]. An important challenge remains in the propagation of the optical rates of emission, re-absorption and out-coupling to the electrical performance of the solar cell. To this end, the expressions for the local rates and the Poynting-vector in terms of the Green dyads need to be connected to the local value of the quasi-Fermi level splitting [182, 183]. This consistent formulation of light emission, propagation, and re-absorption can also be used to assess on equal-footing the contributions of photon-recycling and luminescent coupling in

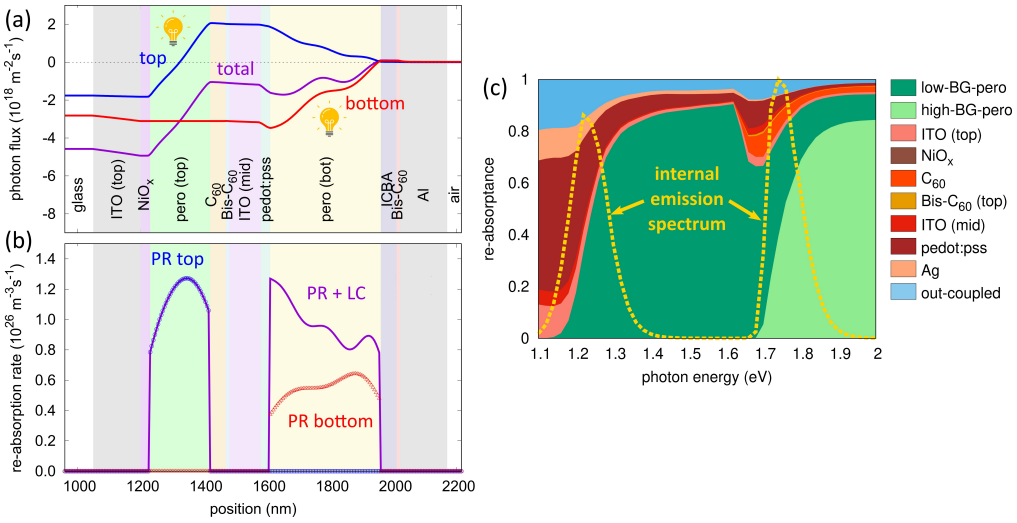

Fig. 14. Optical modeling of internal emission and re-absorption in an all-perovskite tandem solar cell based on the Green tensor formalism: (a) Sub-cell contributions to the total photon flux due to internal emission (blue: top, red: bottom, magenta: sum/total). (b) Spatial profiles of secondary photogeneration rates due to PR and LC. (c) Spectrum (dashed), layer-resolved re-absorptance (green: PR and LC, red: parasitic) and out-coupling (blue) of internally emitted light. (Adapted from Ref. [184], Fig. 5 © 2024 Wiley-VCH GmbH.)

multi-junction solar cells based on thin films, such as all-perovskite tandems [184] (Fig. 14). For tandems including sub-cells with incoherent optics, such as perovskite-silicon tandems, the Green dyad formalism can be coupled to net-radiation or even ray-tracing models (in the presence of scattering at large scale textures) for this purpose [185].

At the same time, device structuring on the nano-scale often results in periodic structures. Models of periodic structures are typically restricted to a single unit cell of the repeating structure. Such a model is valid for a periodically repeating coherent ensemble of sources that differ only by a phase factor. Since we instead wish to model a single incoherent source, we need either to simulate a large supercell of the repeating periodic structure [186, 187] or integrate over values of the phase in reciprocal space [188]. While large supercells are conceptually more straightforward, the reciprocal space integration may offer more room for an efficient approach. The integrand involved is typically highly singular which requires special mathematical treatment, but opens the door to adaptive schemes and rational function interpolation schemes, which may vastly reduce the computational effort required. It should be noted that such issues also appear in integrals of the angular spectrum of simpler structures such as planar interfaces due to the bound waveguide modes. There, reciprocal space integration techniques could also be applied to reduce the computational effort. Indeed, divergences in dissipated power at large values of in-plane photon wave vector in absorbing media are a common issue in dipole radiation theory, and are usually mitigated by a rather arbitrary wave-vector cut-off [177] or the introduction of non-absorbing domains around the dipole position [180, 189]. Since these divergences originate in the presence of near-field energy transfer by longitudinal components of the Green tensor related to the use of a continuum model of the dielectric medium response at microscopic distances, they are removed by transition to a purely transverse Green tensor [182].

Simulation of the entire opto-electronic response of solar cells is crucial to achieving the highest efficiencies. The challenges highlighted in this chapter will require the continued development of

multiphysics approaches in order to accurately and efficiently evaluate device performance.

5.6. Advances needed

Luminescence will play a key role both as an analytical tool and as a design parameter for high efficiency solar cells. The following aspects will be crucial for improving devices efficiencies:

In-Situ Measurements Luminescence will be used as an analytical tool both for fully completed devices and for manufacturing processes through real-time monitoring of in-situ device deposition. This allows for fast and low-cost measurements that provide direct information on how well the device is functioning, allowing for challenges that develop during the deposition process to be investigated and overcome.

Radiative Efficiency Future designs of high performance solar cells will need to incorporate strategies to increase the radiative efficiency. This will primarily bring the open circuit voltages and hence the efficiency closer to the theoretical limit.

Luminescent Coupling For multi-junction devices, luminescent coupling will be included in the design process, thereby allowing multi-junction devices with monolithic connections to obtain higher efficiencies and to operate over a wider range of illumination conditions.

Modelling Internal Emission For luminescence to be included in the design process, improved optical and electronic models are required. These models need to include a range of factors including the statistically incoherent light sources, full wave propagation, nanostructuring, multi-physics, etc. The Green dyad presented in this chapter provides an approach combining many of these components, with the development of further models needed to incorporate other specific factors, e.g. nanostructuring.

6. Luminescence II—There Are Two Distinct Photon Gases Present Inside Every Solar Cell

E. YABLONOVITCH, Z. OMAIR

6.1. Introduction

It has gradually been recognized that incoming sunlight can be trapped within a high refractive index semiconductor, $n \approx 3.5$, owing to the narrow 16° escape cone. The solar light inside a semiconductor is $4n^2$ times brighter than incident sunlight [34]. This is called light trapping and has increased the theoretical and practical efficiency of solar panels. But there is a second photon gas of equal importance that has been overlooked. Inside every forward-biased solar cell there is a gas of infrared luminescence photons, also trapped by total internal reflection. We introduce the idea of *super-equilibrium*, when the luminescence photon gas freely exchanges energy with the two quasi-Fermi levels.

Nonetheless, the loss of a single photon from either gas is equivalent to the loss of a precious minority carrier. Therefore, optical modeling and design become equally important as electron-hole modeling in high efficiency solar cells. It becomes possible to approach the idealistic Shockley-Queisser limit [22], by proper material selection and design of the solar cell optics.

6.2. The two distinct photon gases

Inside a solar cell, the incoming solar photons tend to be trapped by total internal reflection. As illustrated in Fig. 15(a), weakly absorbed rays of sunlight experience multiple internal reflections, forming a photon gas with $4n^2$ absorption enhancement [34], increasing both current and voltage. At the same time, there is second photon gas, illustrated in Fig. 15(b), inside every solar cell. The presence of a non-zero voltage is accompanied by an infrared luminescence photon gas, significantly brighter than Planck's black-body radiation.

These two photon gases are very important for solar cell operation. If a single photon is lost from either photon gas, it is equivalent to the loss of a precious minority carrier. Thus the photon gases need to be included in solar cell modelling, and must be treated on an equal footing with the electron gas, and with the hole gas, that are also present in every solar cell.

6.3. The generalized Planck theorem

In thermodynamic equilibrium, there is only one Fermi level (or chemical potential μ) for electrons in a system. Semiconductors are unusual in that they separately sustain both, an electron gas and a hole gas. In the best materials, the electrons and holes recombine rarely compared to their individual momentum relaxation rates, and they barely interact. The electrons and holes fail to mutually equilibrate, and they have separate Fermi Levels. Since they are out of global

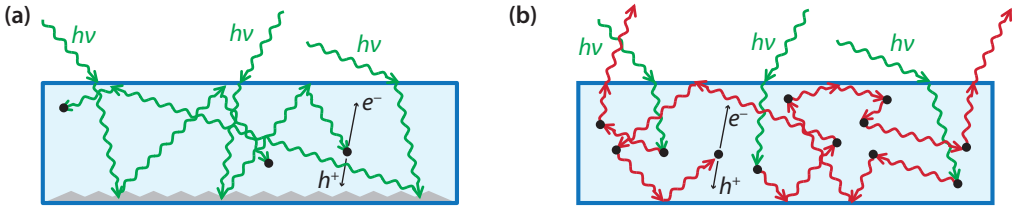

Fig. 15. (a) The photon gas formed by weakly absorbed solar photons (in green), reflected from the random scattering rear surface. The internal brightness is $4n^2$ larger than the incoming sunlight. (b) The other internal photon gas (in red) formed by luminescent infrared photons (adapted with permission from Ref. [158], © 2012 IEEE).

equilibrium, the separate Fermi Levels are called quasi-Fermi levels, $E_{\mathrm{F}n}$ and $E_{\mathrm{F}p}$ respectively, where $E_{\mathrm{F}n} - E_{\mathrm{F}p} = \mu = qV$ with the elementary charge q and the voltage V. The quasi-Fermi level separation $\mu = qV$ represents the internal free energy buildup by sunlight.

In a solar cell there is a further type of equilibrium: The internal luminescent photon gas exchanges energy with the electrons and holes, and can establish a form of equilibrium that includes photons, electrons and holes. We suggest the name *"super-equilibrium"* when the infrared photon gas exchanges energy between the two quasi-Fermi Levels. The photon gas brightness, $\mathcal{B}$, then deviates from the Planck black-body formula,

$$\mathcal{B}(\nu, \mu, T) = \frac{8\pi n^2 \nu^2}{c^2} \frac{1}{\exp\left(\frac{h\nu - \mu}{kT}\right) - 1}. \tag{3}$$

where the brightness $\mathcal{B}$ is the photon number per area, per unit bandwidth, per unit time, and per 4π steradians; n is the refractive index, ν is the photon frequency, T is the temperature, and kT is the ambient thermal energy. This is sometimes called the "Generalized Planck formula". It was first derived by Ross [157], and further elaborated by Henry [190], and in Ref. [191]. If there is no excess carrier concentration, and only a single quasi-Fermi level, there is global equilibrium, $\mu = qV = 0$, and the ordinary Planck formula would apply. But if $\mu \neq 0$, then the "super-equilibrium" would apply, as represented by the "Generalized Planck formula", Eq. (3).

It is odd that a photon spectral distribution, Eq. (3), would contain a chemical potential, μ. Since the photon number is not conserved—photons can be freely created and destroyed—it is usually understood that the creation of photons costs zero free energy, $\mu = 0$. But that only applies to perfect thermal equilibrium. In our case, the photons are closely coupled with, and exchange energy with, the carriers of an excited semiconductor. The photon distribution, Eq. (3), then contains the chemical potential of the semiconductor carriers, the quasi-Fermi level separation.

The quasi-Fermi level separation can be regarded as causing the luminescent infrared photon gas. In "super-equilibrium", this infrared gas brightness $\mathcal{B}$, can be reinterpreted as measuring the voltage V in the photovoltaic cell,

$$qV = \mu = E_g - kT \ln\left(\frac{8\pi n^2 \nu^2}{\mathcal{B}(\nu, \mu, T)c^2} + 1\right). \tag{4}$$

In human experience, we rarely confront light at or near thermal equilibrium. In virtually all human experience, light is much brighter than the thermal equilibrium intensity, except perhaps on a very dark starless night. To the extent that there is sufficient ambient light, Eq. (4) can assign a chemical potential $\mu > 0$ to the light brightness we deal with in our daily lives. It is perfectly reasonable to ask on a sunny day: "What is today's chemical potential as given by Eq (4)?" It would be like a weather report, and combined with ambient temperature, would provide an upper physical limit for that day's photovoltaic cell voltage.

Luminescent infrared photons are not lost to photovoltaics. Owing to light trapping, only the small fraction $1/4n^2 \approx 2\%$ of the internal infrared luminescence escapes. 98% of the infrared luminescence is trapped upon each front surface reflection and is subject to re-absorption. Therefore modeling of solar cell performance must include a full optical analysis, on an equal footing with the analysis of minority carrier transport. Indeed, in a good solar cell, the minority carrier properties are usually close to ideal, and the performance is completely determined by the photovoltaic optics [158]. This is certainly true for the current flat-plate record solar cell, [15], which surpassed the previous record by further improving rear-surface reflectivity.

The remaining 2% of internal infrared luminescence photons, lost to escape from the front surface, are not really lost. The front surface of a solar cell must be open to allow the entry of sunlight. At open-circuit conditions no current is drawn. According to the detailed balance

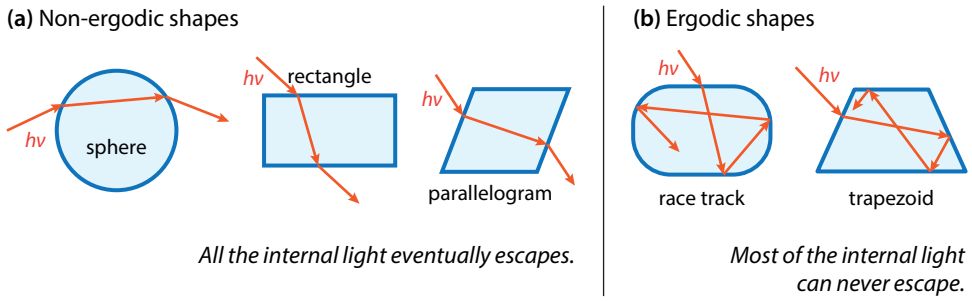

Fig. 16. (a) Non-ergodic: The term ergodic refers to the time average trajectory of a light ray being the same as the phase-space average. The simple geometric shapes, sphere, rectangle, parallelogram fail this test. A light ray that enters such a shape but rapidly escapes, and fails to fill all possible internal angles. (b) Ergodic: In the case of odd shapes, the trapezoid, or the race track, light rays scatter at unusual angles, filling the full internal angle space. The light intensity builds up increasing brightness by $4n^2$, and free energy by $kT\ln(4n^2)$, and the photovoltaic output voltage by $(kT/q)\ln(4n^2)$. Almost all but the simplest geometric shapes are ergodic.

limit [22], those incoming solar photons are replaced by outgoing luminescent photons, from the internal photon gas that is $4n^2$ times brighter than the incident sunlight. Thus the 2% photon escape is a necessity, not a loss mechanism. This also led to the slogan: "A great solar cell also needs to be a great Light Emitting Diode" [158].

In some forms of photovoltaic cell modeling, it is necessary to know the B-coefficient, where Bnp is the rate of spontaneous emission from electron/hole recombination. But the spontaneous emission coefficient can be bypassed by using detailed balance [181] to compute the spontaneous emission; where luminescent emission $L(\nu,\mu,T) = \alpha(\nu,\mu,T) \times \mathcal{B}(\nu,\mu,T)$ is exactly balanced by optical absorption of the internal luminescence photons. Then spontaneous luminescence is

$$L(\nu,\mu,T) = \frac{8\pi n^2\nu^2}{c^2}\frac{\alpha(\nu,\mu,T)}{\exp\left(\frac{h\nu-\mu}{kT}\right)-1}. \tag{5}$$

When the material is only moderately excited, $\mu \ll \nu h$, the absorption spectrum is unchanged from that of unexcited material, replacing $\alpha(\nu,\mu,T)$ with $\alpha(\nu,0,T)$. Thus the spontaneous emission can be known without a knowledge of either the B-coefficient, nor the intrinsic carrier density, n_i, in the semiconductor. Indeed only the conventional absorption coefficient $\alpha(\nu,0,T)$ is needed, and Eqs. (3–5) in this chapter apply equally well to dye molecules as to semiconductors. A dye molecule can have an internal chemical potential determined by the excess probability $p_{\rm ex}$ of being in the excited state, relative to p_0 the usual Boltzmann probability, $\mu = kT\ln(p_{\rm ex}/p_0)$.

6.4. *Ergodic light trapping*

Light trapping inside the solar cell improves the voltage, current, and fill-factor. But it was not exploited in the first 40 years of the photovoltaic industry. One reason is that the first generations of photovoltaic cells consisted of a plane-parallel slab. In semiconductors, the refractive index is high, $n \approx 3.5$ in silicon. By Snell's Law, the refraction inside the slab would always be within an angle $\arcsin(1/3.5) \approx 16^\circ$, a cone adjacent to normal. As shown in Fig. 16(a), the simple geometry of a plane parallel slab fails to scatter light rays in directions outside this narrow cone which only accounts for $(1/4n^2) \approx 2\%$ of 4π steradians. The other 98% of angles remain inaccessible.

This problem is solved by simply leaving the rear surface of silicon rough, as saw-cut, to break the plane parallel slab symmetry. The light propagation becomes ergodic as discussed in Fig.

16(b), and shown in Fig. 15(a). Scattering the internal light by $> 16°$, which would require an 8° rear facet, is usually sufficient. While Lambertian rear light scattering is sufficient for $4n^2$ ergodic light trapping, it is not necessary. Any deviation from perfect symmetry by more than 8°generally converts a non-ergodic geometric shape into an ergodic light trapping shape, providing a voltage and current boost.

Light trapping was not generally adopted by the photovoltaic industry until the late 1990s, but it was already thoroughly exploited in Martin Green's PERC cell [7] a decade earlier. The benefit is to increase the internal optical brightness by $4n^2$, and the optical free energy by $kT \ln(4n^2)$, and the photovoltaic output voltage by $(kT/q) \ln(4n^2)$.

In their analysis of fundamental solar cell efficiency, Shockley and Queisser, S&Q, idealized the optical situation [22]. Optical absorption jumped from zero to infinity at the bandedge. The material itself had 100% luminescence efficiency, and the luminescence was immediately re-absorbed with no losses. There was no need for a distinction between internally trapped light and external luminescence. All of the solar cell optical physics were effectively idealized away, and there was no need to talk about the two internal photon gases.

Shockley and Queisser achieved their goal of placing an upper limit on solar efficiency. The purpose of this chapter is to consider the parasitic optical effects, and to show that these deleterious effects can be largely overcome by proper optical management and design. By maximizing the optical reflectivity in the context of ergodic optics, and selecting materials with very high internal luminescence yield, we can approach the idealized S&Q performance.

6.5. Non-ideal solar cells

We now consider a series of non-ideal solar cells, shown in Figs. 17(b–d). But Fig. 17(a) is an exception: there, we have done the best possible job with the optics. There is a high reflectivity mirror, so that none of the photons are lost. Ergodicity is provided in two ways: by the textured rear reflector, and by the re-absorption and random angle re-emission of the infrared luminescence. The spectral shape of optical absorption and re-emission can be taken into account using the Shockley-Van Roosbroeck [181] principle. The result for GaAs is 33.5% efficiency [158] for standard Air Mass 1.5 illumination [192], similar to the S&Q result, but without the idealistic assumptions. In GaAs, a dirct bandgap semiconductor, we benefit from the very low Auger recombination relative to internal luminescence.

The non-idealities in GaAs solar cells prior to 2011 are represented by several cases in Fig. 17. In Fig 17(b), the material is of top epitaxial quality, but the film rests on the original growth substrates. The substrate is thick, relatively impure, and has no proper rear mirror. The optical quality is assumed poor. The substrate is essentially a sink for bandedge luminescence. This immediately wastes 98% of the luminescent photons, like losing 98% of the minority carriers at open-circuit. The main effect is to lose $\approx (kT/q) \ln(4n^2)$ in open-circuit voltage,V_{oc}. Eliminating this problem by epitaxial liftoff was the reason for all the new solar cell efficiency records in the 2010s.

Consider the opposite non-ideality in Fig. 17(c). The optics are good as in modern c-Si solar cells, but the material is handicapped by being indirect. Although Si is indirect, it still luminesces, and can be an LED [193]. Nonetheless, Si is not efficient enough to build up a high brightness of luminescent photons, which requires an internal luminescence efficiency $> 90\%$ owing to the multiple absorption/re-emission events. The loss of luminescent photons reduces luminescent brightness and by Eq. (3.4) leads to a corresponding drop in open-circuit voltage V_{oc} by $\approx (kT/q) \ln(1/\eta)$, where where η is the internal luminescence yield in the material.

But there is ample motivation for good optical design, in Fig. 17(c), despite Si being an indirect semiconductor. Good optical design increases the effective optical absorption coefficient by about $4n^2 \approx 50$, and allows the silicon to be thinner by the same factor. The photo-carriers from the sun are effectively compressed into a thinner layer, and reside at a higher density by

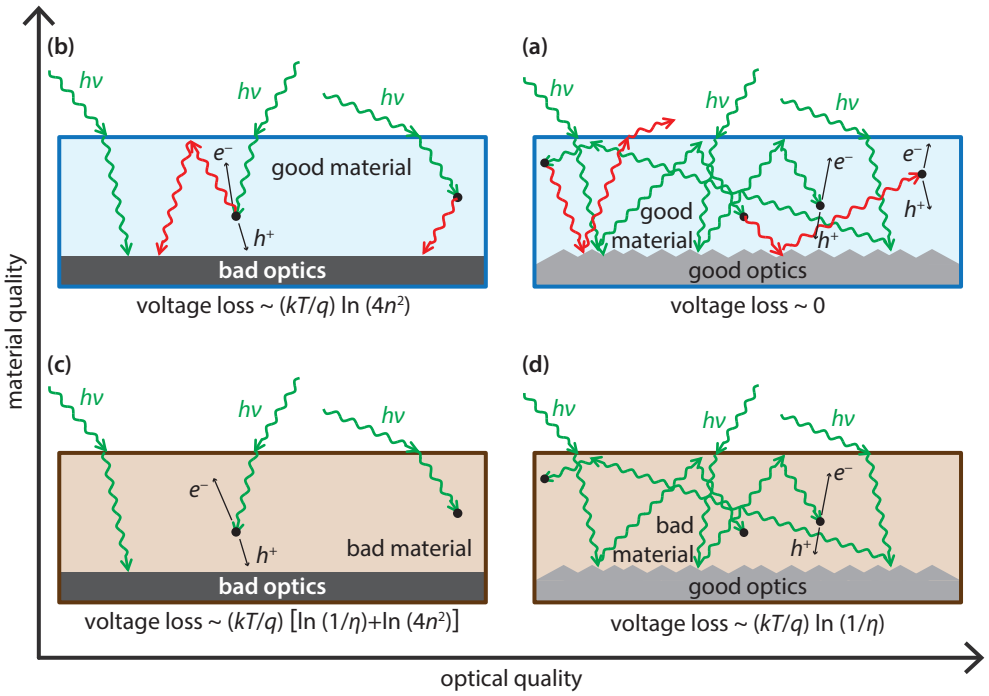

Fig. 17. A comparison of the effect of light-trapping optics on the operating point voltage penalty ΔV_{op} from poor internal luminescence efficiency, η, and/or poor optical design. Case (a) is the ideal case of a perfect scattering rear mirror for ergodicity, combined with the record-breaking internal luminescence efficiency of epitaxial thin GaAs film separated from their growth substrates by epitaxial liftoff. Case (b) represents epitaxial GaAs solar cells before 2011, which were still attached to the original GaAs growth substrates, that were so thick as to effectively absorb bandedge luminescence. Case (c) is a modern Si solar with good light management, but the material is labelled bad since the indirect gap prevents high (>90%) internal luminescence efficiency. Case (d) represents the older generation of Silicon solar cells, (pre-1990), still indirect, but also with no implementation of light trapping.

$\approx 4n^2$ times. The higher density corresponds to less entropy and more voltage. The designer who to uses good optics to make his Si-solar cell thinner would then gain $\approx (kT/q)\ln(4n^2)$ in V_{oc}. But good optical design is already assumed in both Figs. 17(a) and 17(c).

Such good optical design is one of the reasons that Si-solar cells are far exceeding the theoretical limits that were projected in the 1970s [194, 195]. The other reason is that higher performing cells require good material quality. But good material quality also includes low recombination on the surfaces and interfaces. If the surfaces and interfaces dominated the electron-hole recombination, there would be no benefit in making the solar cell thinner. This was first achieved by Swanson [196, 197] using point contact openings on oxidized Si, effectively creating the first double heterostructure [198, 199] on silicon. The oxide coating was particularly compatible with good optical mirror reflectivity.

The remaining case is shown in Fig. 17(d), corresponding to the old-fashioned silicon solar cells before light-trapping and Si heterojunctions became standard. In those days, the rear reflectivity was rather poor, i.e. bad optics, and the material being indirect was yet a second penalty. The material had to be thick enough to absorb the solar photons, with no help from light trapping.

A thicker solar cell means a lower minority carrier concentration, since the same injected carriers occupy a larger volume. Thus, the open-circuit voltage is penalized by $\approx (kT/q)\left[\ln(1/\eta) + \ln(4n^2)\right]$, once for the poor luminescence efficiency, and again for poor optical absorption, necessitating greater thickness.

6.6. Conclusions and Advances needed

For the reasons given in this chapter, the photovoltaic industry employs solar light-trapping in almost all cases. But there is now a second mechanism with the recognition of the internal infrared luminescent photon gas that can build up to a high brightness, many suns, inside direct bandgap materials. If this infrared luminescent photon gas is properly conserved, absorbed, re-emitted, and reflected, then the Shockley-Queisser limit can be approached even under a realistic practical optical design.

In lower performing solar cells, the Luminescent photon gas is very weak, hardly drawing any current away. Nonetheless this second photon gas is present, inextricably linked to voltage by Eq. (4), and that voltage is boosted by $\approx (kT/q)\ln(4n^2)$ using sound optical management.

We now know how to approach the Shockley-Queisser Limit, but it does require material with a high internal luminescence yield, such as GaAs or perovskites. As we have argued in this chapter, these solar cells need good light management to utilize the full luminescent potential.

7. Light management for multi-junction solar cells

C. Becker, B. Ehrler, H. Helmers, O. Höhn, K. Jäger, M. Schmid

The photovoltaic (PV) module right now accounts for only one third of the total costs of a PV system, as the fixed cost essentially scales with the installed module area (see Ref. [4] and Chapter 2). Therefore, the increase in solar cell efficiency is the most effective parameter for the further reduction of the levelized cost of electricity (see Chapter 2). Silicon PV technology is already so far developed that it reaches efficiencies close to its physical limit. Multi-junction solar cells are regarded as the most promising concept to surpass this limit.

In this chapter, we briefly introduce the general multi-junction solar cell concept (Section 7.1) and provide a brief overview of recent multi-junction solar cell technologies based on III–V semiconductors, silicon, CIGS and perovskites, and identifies the specific scientific and technological questions to be addressed to meet the optical requirements (Section 7.2). In the end, we discuss the specific optical challenges occurring in such devices (Section 7.3).

7.1. The multi-junction solar cell concept

Figure 18a illustrates the spectral irradiance of the sun under standard testing conditions (AM1.5G, grey area) and an upper limit estimation of the usable energy by a solar cell based on a semiconductor with electronic bandgap $E_g = hc/\lambda_g$ considering the detailed balance limit [22]. h, c and λ denote Planck constant, vacuum speed and wavelength of light, respectively. The sketch next to Figure 18a visualizes that photons with energies below the bandgap cannot be absorbed at all, whereas higher-energy photons lose a part of their energy due to thermalization to the band edges. As an example, the red area marks the exploited irradiance of a solar cell with $E_g = 1.1$ eV. In addition to the aforementioned non-absorption and thermalization losses also extraction losses according to the detailed balance limit are considered. When a second solar cell, here with $E_g = 1.7$ eV, is added on top of this bottom cell, thermalization losses are reduced and higher energy photons are converted more efficiently (blue area).

The electrical connection of the subcells in a multi-junction device is an essential point to consider. Figures 18b and c represent example configurations of four-, and two-terminal (4T and 2T) tandem devices. In the simplest approach, the top and bottom cells are electrically independent (i.e. four connections in total–4T, Figure 18b), and are only optically, possibly mechanically, stacked. The main benefits are the opportunity to manufacture top and bottom cell separately, which is particularly interesting when high-temperature processes in combination with temperature-sensitive layers are involved, as well as the independent operation of the two cells in their respective maximum power points. Neither concerns about junction directions are needed, nor is the effect of changing performance with varying irradiation conditions. Yet, parasitic losses will be high since the full number and thicknesses of contacts are required for lateral charge carrier extraction in the top-cell whereas the lower current in the bottom cells relaxes slightly the conductivity requirements to the contacts.

In 2T tandems, the top and bottom cell are – mostly monolithically – connected in series (Figure 18c). The orientation of the two cells' junctions has to be aligned. The current will directly pass from one to the other cell e.g. via a recombination junction. Thus, the intermediate layers and with them parasitic optical absorption are minimized, allowing for maximum light exploitation. In return, the current between top and bottom cell needs to be matched because the lower current of the two will dictate the device performance. The current matching in 2T configuration is a key aspect of the optical design of multi-junction solar cells next to minimizing parasitic absorption.

Figure 18d and e show the theoretical efficiency limits for tandem solar cells as functions of the top and bottom cell bandgap energies for 4T cells and for 2T cells, respectively. In this theoretical efficiency limit calculation, we consider the detailed balance approach for single-junction solar

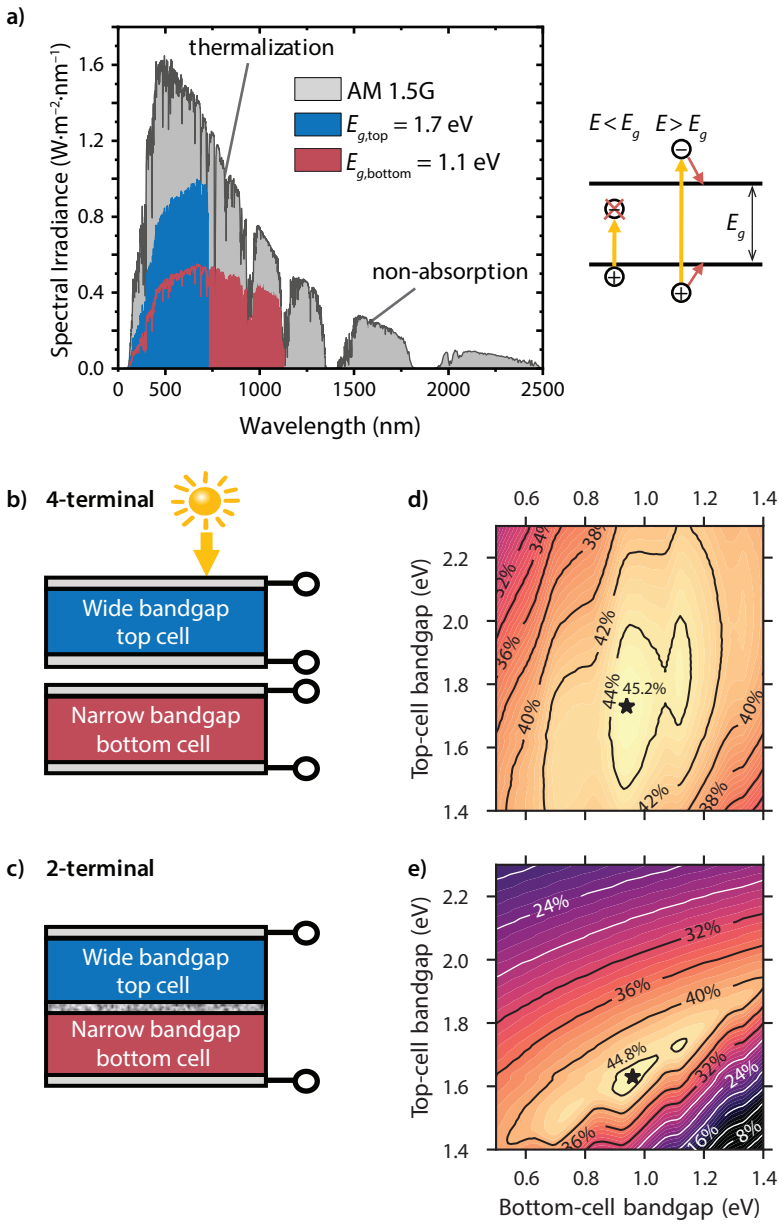

Fig. 18. Multi-junction solar cell concept. a) Exploitation of the solar irradiation (AM1.5G spectrum in grey) by a multi-junction solar cell composed of two subcells with bandgaps E_g = 1.1 eV (red) and E_g = 1.7 eV (blue) considering extraction losses according to the detailed balance limit. Inset: Unabsorbed photons with energy lower than the bandgap and thermalization losses of higher energetic photons. b) and c) Tandem configurations with four terminals (4T) and two terminals (2T) respectively. d) and e) The theoretical efficiency limits for tandem solar cells as functions of the top and bottom cell bandgap energies in 4T and 2T configuration, respectively. [(d) and e) adapted with permission from Ref. [200], © 2022 Wiley-VCH GmbH.]

cells [22]. For 4T cells the efficiencies of the two subcells can be treated nearly independently. That means only the bandgap of the top cell affects the short-circuit current density of the bottom cell. In contrast, for 2T cells the two subcells are electrically connected and the same current density flows through both subcells. Due to this current-matching constraint for the 2T configuration, the power conversion efficiency depends much more on the subcell bandgaps than for the 4T configuration. Details on the calculation can be found in references [200, 201]. While 2T tandem solar cells can act as direct replacement for single junction solar cells, the implementation of 4T devices is more challenging, requiring e.g. more cabling and more complex module design.

7.2. State-of-the-art multi-junction solar cell technologies

Here we give a brief overview of the four classes of semiconductor materials, which are currently leading to the highest power conversion efficiencies in multi-junction solar cells. We describe selected state-of-the-art multi-junction devices, which are currently discussed in the photovoltaics community. Figure 19 summarizes the highest power conversion efficiencies as of October 2024 of a) single-junction and b) 2T multi-junction solar cells as a function of bandgap (a) and bottom cell bandgap (b), respectively.

7.2.1. Absorber materials for multi-junction solar cells

Crystalline Silicon is the most widely used material in photovoltaics for good reason. It is non-toxic, earth-abundant, and stable. Further, silicon is well-known due to its long history in research and development in semiconductor chip industry and photovoltaics. In comparison to the other solar cell materials described above, it has one special feature: It is an *indirect*-bandgap semiconductor, that means to excite charge carriers from valence to conduction band ($E_g = 1.12\,\mathrm{eV}$) they must not only change energy but also momentum. For the optical properties of silicon, this has far-reaching consequences. The absorption coefficient is comparatively low with around $10^3\,\mathrm{cm}^{-1}$ for a wavelength of 800 nm. Even if considering perfect Lambertian light trapping (see Chapter 3), absorbers with several tens of micrometer thickness are required to ensure > 95% absorption of sunlight with $E > E_g$. Further, radiative recombination and all effects associated with it, such as luminescent coupling and photon recycling, can be neglected. Auger recombination and Shockley-Read-Hall recombination will dictate the achievable open-circuit voltage. The detailed balance efficiency limit of silicon single-junction solar cells considering Auger recombination has been calculated to 29.43% [203] and 29.56% [204] without and with exact calculation of an ideal Lambertian light trapping scheme, respectively.

Most **III-V compound semiconductor materials**, such as gallium arsenide (GaAs) and indium phosphide (InP) are direct semiconductors. With an efficiency of 29.1% for a single-junction GaAs solar cell [15], III-V semiconductors have demonstrated the overall highest efficiency among single-junction solar cells (Fig. 19a). Due to their direct bandgap nature, they have much stronger absorption than silicon. Typically, only a few micrometers are sufficient to absorb the targeted sunlight.

Due to their high radiative efficiency, photon recycling [158, 205–207] and in multi-junction solar cells also luminescent coupling [207] are relevant (see chapter 7.3). This high radiative efficiency in combination with excellent rear side reflectors enabled efficiencies close to the thermodynamic detailed balance limit. It should be noted that luminescent coupling is also of particular relevance for multi-junction solar cell measurements, especially of external quantum efficiencies (EQEs). If the devices are highly radiative even at low irradiances, the determination of absolute EQEs becomes challenging [43]. Measured EQE can have an artifact caused by luminescence coupling that is similar to an artifact caused by low parallel resistance [208]. A key advantage of III-V semiconductors extends beyond the highest radiative efficiency and is the tunability of the bandgap. Adjusting the composition of ternary, e.g., AlGaAs and InGaP, and

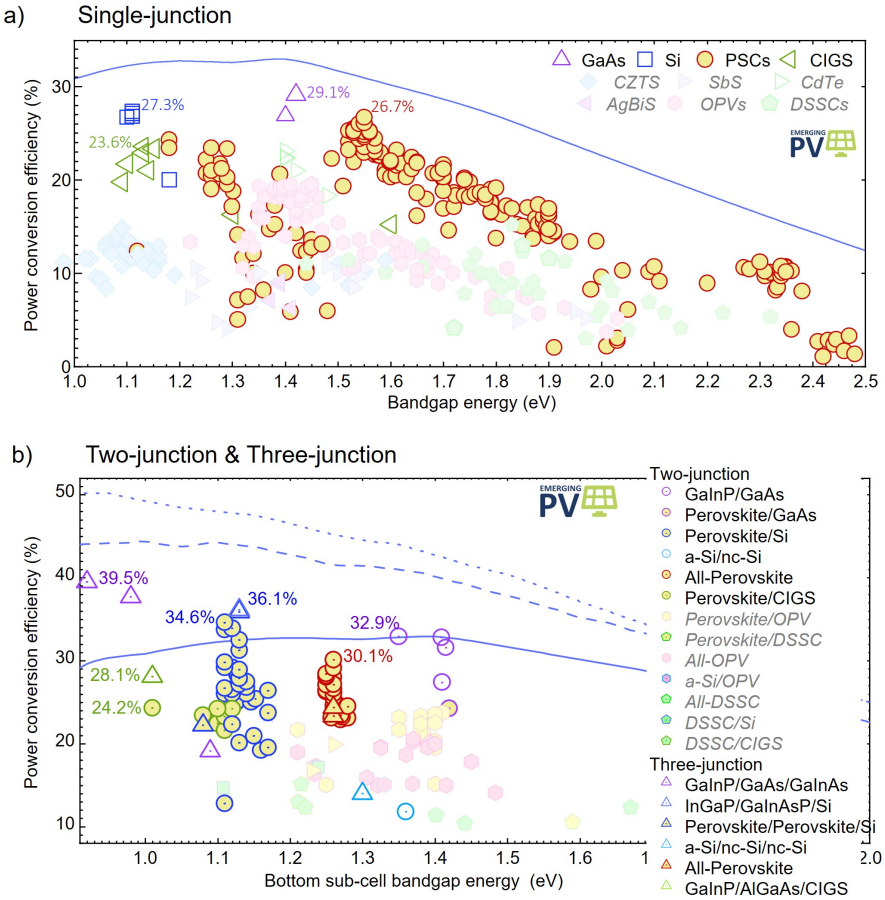

Fig. 19. Power conversion efficiencies for a) single-junction and b) two-terminal multi-junction photovoltaic research cells including up to three junctions as a function of the absorber bandgap energy of the single-junction cell (a) or the bottom subcell of the multi-junction device (b), respectively, for various photovoltaic materials as of October 2024. Materials that are not explicitly considered in this chapter are shaded. The solid, dashed, and dotted lines in the efficiency graph indicate the single junction, the top-subcell-optimized and top- and middle-subcell-optimized detailed balance efficiency limits for one junction, double junction, and triple junction photovoltaic cells, respectively. (Adapted from Ref. [202]. Data by courtesy of the emerging-pv.org database.)

quaternary compounds, such as GaInAsP, allows for tuning the bandgap of III-V semiconductor from 0.7 eV to 2 eV by changing the composition. To decrease material consumption and cost, ultrathin solar cells utilizing multi-resonant photonic structures receive more and more attention [209–211]. Remarkable efficiencies of 19.9% have been achieved using only 205 nm of active III-V absorber material [212].

Chalcopyrite materials Cu(In,Ga)(S,Se)$_2$ (short CIGSSe) are characterized by a direct band gap and a related absorption coefficient in the range of $10^5\,\mathrm{cm}^{-1}$. Compared to crystalline silicon, they can hence be fabricated as thinner films of approximately 2 µm thickness while maintaining complete absorption of photons above the band gap and simultaneously enabling flexible, lightweight, and semitransparent applications with tunable thickness. The challenge of containing rare indium and gallium may be tackled by ultra-thin absorbers joint with light management strategies that are indispensable for efficient multi-junction devices [213]. One major benefit of the Cu(In,Ga)(S,Se)$_2$ (CIGSSe) material system is the tunability of the band gap, ranging from 1.04 eV for pure CISe over 1.45 eV for CIS and 1.68 eV for CGSe up to 2.38 eV for CGS [214]. CIGSSe may hence be used for any absorber of the multi-junction device and all-chalcopyrite devices appear feasible. It has to be noted that for CIGS materials, the increase in band gap above 1.4 eV is a remaining challenge as the V_{oc} deficit significantly rises when the gallium to gallium plus indium ratio surpasses 0.3 [215]. The reasons are amongst others deep defects, grain boundaries, interfacial recombination, and microdomains [216]. Besides, CIGSSe stands out due to its high radiative recombination and high stability making it suitable even for space applications [217].

Metal halide perovskites, characterized by the ABX_3 structure, are particularly suited for multi-junction solar cells because of their wide bandgap tunability and excellent optoelectronic properties for many of these bandgaps. The A-site cation can be a small organic molecule or Cs, the B-site metal is typically lead or tin, and the X-site anion is typically a halide, often a mixture of bromide and iodide. Much of the research has been focused on bandgaps that are suitable for tandem combination with crystalline silicon (1.5-1.6 eV), and those solar cells perform close to the detailed balance limit (see Figure 19) [202]. These perovskites typically contain a large fraction of iodide, and their remarkable performance is a result of the so-called defect tolerance, originating in the fortunate incidence that the valence band contains a large fraction of anti-bonding orbitals [218]. As a result, materials made with simple procedures show remarkably high photoluminescence quantum yield (PLQY) [219]. The high PLQY and small Stokes shift has led to interesting light-management questions, for example the luminescent coupling between various sub-cells [169], the effect of photon recycling [161], and self-absorption [220]. The research field is increasingly focusing on improving the efficiency of the narrow- and wide-bandgap compositions. These are necessary for all-perovskite multi-junction solar cells, but there is a gap between the performance of perovskite solar cells with these bandgaps and the detailed balance limit (see Figure 19). For the narrow-bandgap solar cells, the tin-based compositions show a reduced photocurrent, related to the deficiency in charge transport. Conversely, the wide-bandgap compositions suffer from a voltage loss that is partially related to the tendency for the (bromide-rich) compositions to phase segregate [221] and partially to the lack of suitable transport layers [222]. While the performance of perovskite semiconductors remains remarkable, the long-term stability does not match other solar-cell materials. Extrinsic factors such as sensitivity against water and oxygen can be managed by proper encapsulation [223], intrinsic factors such as ion migration [224] and the phase segregation [221] might pose a more fundamental challenge, whereas issues with reverse bias instability pertain to tandem applications [225].

7.2.2. Selected multi-junction solar cell technologies

Here we give a brief overview about selected multi-junction solar cell technologies that are currently widely discussed in the photovoltaics community (see Figure 7.2b) and where we

believe that they shall play an important role in future photovoltaic energy conversion.

III-V/Silicon multi-junction solar cells are suited for both 2T and 4T operation. Champion efficiencies of 2T III-V-on-silicon devices (record 36.1% [43]) are currently higher than their 4T counterparts [226]. While the optical interface between the two stacked cells of 4T tandems requires careful investigation, 4T tandems promise to be less sensitive for spectral variation outdoors and thus show an increased energy yield in the field. However, it has been shown that this difference can be small if the 2T devices are well designed [227, 228]. In the last years, the focus was on GaInP/GaAs/Si triple junction solar cells as they show the highest efficiency potential, but 2-junction devices with an AlGaAs based top solar cell [229] are of interest because of their potential for lower epitaxy cost. The currently best 2T GaInP/GaAs/Si are realized utilizing a direct wafer bond. To this end the top solar cell is usually grown invertedly on a growth substrate – i.e. GaAs or Ge wafers – and then wafer-bonded to a polished silicon bottom solar cell [42]. Afterwards, the growth substrate can be lifted and potentially be re-used, and the cell structure can be processed into a solar cell. Whether this approach can lead to an economically attractive solution remains to be shown, but the method clearly proves the efficiency potential of the concept. Another option is to use the silicon bottom cell itself as the growth substrate [230].

One option is to use transparent conductive adhesives [231, 232] to bond a III-V cell onto the silicon bottom cell. In this case, a challenge lies in the optics at the interface. The adhesive usually has a low refractive index leading to two counterbalancing effects: reflection losses of the incident light, but also strong internal reflection of radiatively emitted light supporting photon recycling and thus increasing device voltage.

Last, effective light trapping is especially important for the silicon bottom cell. Several different structures have been tried here. The mature random pyramids at the front side cannot easily be used, as for all three sketched routes flat surfaces are required. Thus, light trapping needs to be implemented at the rear side. Here wet chemically etched structures such as random pyramids or the acidic texture as used formerly for multi-crystalline silicon are one candidate. Another option is a metallic photonic grating that scatters light into defined modes [233]. This approach is especially interesting if a planar rear side of the silicon bottom cell is desired, e.g. when using the TOPCon silicon technology.

All-III-V multi-junction solar cells are a very mature technology delivering highest efficiencies so far. Due to the relatively high costs they are used mainly in space applications, but are also being considered for vehicle-integrated photovoltaic applications, drones, and high-altitude pseudo satellites (HAPS) [234]. It can be beneficial to grow III-V subcells on a Ge substrate, which then also yields an active Ge bottom subcell by using a diffused emitter. One standard product has been a triple-junction GaInP/Ga(In)As/Ge solar cell on Ge substrate, however, also approaches with more stacked junctions are available for space.

A distributed Bragg reflector below the Ga(In)As helps to reduce the subcell thickness, mitigating degradation in space and enhancing end-of-life performance, crucial for space solar cell efficiency [235]. Alternatively, invertedly grown metamorphic cells on metal foil allow direct rear-side processing and mirror implementation, improving performance [236] but adding fabrication complexity and cost [237].

III-V multi-junctions also have terrestrial applications, where high efficiencies or superior power-to-mass ratios are required. Here, a GaInP/GaAs tandem cell – also often grown invertedly – with rear side mirror is an interesting option [238]. Also in these devices, the mirror enhances the absorption in the bottom cell, but even more importantly it severely improves photon recycling and thus increases the voltage of the device. The currently best device of this approach has an efficiency as high as 32.8% [15] under the AM1.5G spectrum. A triple junction solar cell even allows for 37.9% [15, 239], or even 39.5%, where the middle cell bandgap was modified using thick GaInAs/GaAsP strain-balanced quantum well (QW) solar cells [15, 240]. This is the overall highest efficiency under one sun.

While those multi-junction devices for one sun on earth are still a niche, 4-6 junction solar cells are state of the art in concentrating photovoltaics (CPV, see Chapter 3). The highest efficiency, 47.6%, was achieved with a wafer-bonded 4-junction solar cell under the AM1.5D spectrum [18]. A 6-junction solar cell reached 47.1% efficiency under 143-fold concentrated sunlight [241]. While these cells are lab cells, industrial 5-junction solar cells on germanium are available for CPV. Lab records are often optimized for 25°C, but CPV operating temperatures are around 60-90°C. Here, the bandgaps can be tailored in a way to ensure that the subcell absorptances do not shift into the absorption lines of the solar spectrum avoiding current mismatch [242].

Perovskite/Silicon tandem solar cells are currently attracting a great deal of attention worldwide. They present an excellent extension to the well-established silicon technology for large-scale applications, meanwhile demonstrating power conversion efficiencies of more than 34% [243, 244], clearly exceeding the efficiencies, which are demonstrated - and theoretically possible - in silicon-only devices. Regarding optical optimization, many research and development efforts concentrate on the compatibility of perovskite top cell growth on silicon bottom cells with industrial standard micrometer-sized pyramidal surface textures (see Chapter 3). Such textures are necessary for optimum light in-coupling and light absorption. A combination of perovskite solution processing, so far leading to the highest perovskite single-junction efficiencies, with these large pyramidal silicon textures is not easily possible. Here, the silicon front surface textures have to be adapted by decreasing their size below the perovskite layer thickness, using nanopyramids [245–248], tailored nanophotonic structures [249], or adpated black silicon [250]. Alternatively, the perovskite deposition method is adapted, for example by using the so called hybrid approach, where the perovskite top cell is conformally grown on the pyramidal textures by evaporation and subsequent infiltration with solution [251], or by evaporation only [252].
Multi-junction-specific optical topics (see Figure 20) discussed in the context of perovskite-silicon tandem solar cells are the consideration of realistic outdoor illumination conditions (see Chapter 10) including spectral deviations from the AM1.5G solar spectrum and bifacial illumination [253–257]. An accurate knowledge of the spectral illumination is crucial in order to ensure current-matching in monolithic 2T devices. Further, the above mentioned high PLQY of perovskites leads to interesting effects via luminescent coupling in 2T [166, 200, 258, 259] and 4T [260] tandem solar cells, which can relax current-matching constraints. Further, effective spectral splitters have been discussed conceptually [261].

Perovskite/CIGS tandem solar cells are currently the most popular and highest efficient tandems with CIGSSe bottom cells, even though the material system would also be suitable for various other combinations as outlined above. We will focus here on the recent development of perovskite/CIGSSe tandems from 2022 onwards as earlier literature is summarized in reference [200]. In 2022 a 2-terminal tandem made of a Cs(MA,FA)Pb(I,Br)$_3$ top cell (E_g = 1.68 eV) and a CIGSe bottom cell (E_g = 1.1 eV) with 24.2% certified efficiency was reported [262]. The remaining current mismatch was assesed numerically and an efficiency of 30% was predicted. A slight variation in material compositions and hence band gaps led to 23.5% certified efficiency [263]. The triple-cation perovskite had a band gap of 1.59 eV and the bottom CIS 1.03 eV, which together with perovskite layer thickness optimization and application of an AR coating allowed an improved current match. Current matching as well as the remaining challenges of CIGSe surface roughness, and hence the risk of shunting due to a non-compact hole-selective layer of the perovskite top cell, can be circumvented in 4-terminal configuration. An extensive optimization of a CsFAPb(IBr)$_3$/CIGSe tandem (band gaps 1.64/1.04 eV) was conducted through significantly reducing parasitic absorption by replacement of the front and rear ITO by IO:H and IZO, respectively, and through minimizing reflections by the application of MgF_2 AR coatings, leading to 27.3% calculated (top plus shaded bottom cell) efficiency [264]. The latest record of (equally calculated) 28.4% 4T-efficiency was achieved for a CsFAPb(IBr)$_{3/}$CIGSe tandem (band gaps 1.67/1.04 eV) with improved perovskite material quality [265]. An efficiency maintained

over 600 h underlines the persistent challenge of stability. A way out of stability issues may be all-chalcopyrite tandems if the challenge of low top-cell performance is overcome. Whilst the efficiency for the CGSe/CIGSe tandem remains below 10% (2T mechanical stack of 8.5% reported [266]), the integration of Ag enables (Ag,Cu)(In,Ga)Se_2/CIGSe tandems approaching higher efficiencies (13.9% in 2T beam-splitting configuration [267]). Further optimization appears feasible by improved material quality of wide-gap chalcopyrites, including alternative compositions.

All-perovskite multi-junction solar cells offer cost-effective fabrication and lightweight, flexible solutions [268, 269]. Their optical challenges fall into two categories: general light management tasks and multi-junction-specific issues.

Losses by reflection and parasitic absorption losses must be reduced, and - particularly in thin narrow bandgap perovskite layers - measures must be taken to increase the light path. Reflection reduction is mainly achieved by low refractive index antireflective layers or by using surface textures. In independently connected multi-junction solar cells, such as 4T tandems, additional and thicker transparent electrodes cause parasitic absorption in the longer wavelength regime. This can be mitigated by the use of high mobility, low free-carrier absorption transparent conductive oxides like indium zinc oxide [270]. Narrow bandgap lead-tin (Pb-Sn) perovskites as used in all-perovskite multi-junction solar cells exhibit a low near-infrared absorptivity. A compensation by increasing the layer thickness is challenging because of low carrier diffusion lengths. Solutions for light path enhancement include light scattering resin particles in the narrow bandgap Pb-Sn perovskite layer [271]. Yu *et al.* developed a SnOCl-basec hole transporting layer with a textured structure that reduces optical losses, simultaneously boosting the carrier diffusion length in the narrow bandgap perovskite subcell [272]. Also the optical improvement potential of nanotextures has been assessed numerically [273, 274].

One major multi-junction-specific challenge of all-perovskite solar cells is the bandgap engineering of different subcells. Perovskites of different bandgap cannot be fabricated with equally high quality, and hence there are certain bandgap regimes where the single-junction efficiencies lag behind the others (Figure 19a). Narrow bandgap perovskites are mainly limited by collection losses and low diffusion lengths, while wide bandgap perovskites suffer from open-circuit voltage losses due to phase segregations and a lack of suitable transport layers. Luminescent coupling has been demonstrated experimentally in all-perovskite layer designs [166] and has shown to relax the current-matching constraint in 2T devices [166, 275]. Studies also investigate the influence of realistic illumination conditions, such as bifacial illumination [271, 276, 277] or deviations of the solar spectrum from AM1.5G [166, 278] in all-perovskite tandem solar cells.

7.3. Advances needed

In conclusion, multi-junction solar cells are currently developing at a rapid pace, which is reflected in rapidly increasing power conversion efficiency records. In the future, the optical challenges in the field can be summarized by:

a) **Reduction of optical losses:** In every solar cell, regardless of the number of junctions, optical losses via reflection, transmission, and parasitic absorption in contact and recombination layers must be reduced to a minimum (see Chapter 3). The technological implementation of these measures varies greatly depending on which absorber materials are involved in the multi-junction solar cell. For instance, random micro-pyramidal textures as used for the minimization of optical losses in silicon solar cells are not directly transferable to solution-processed perovskites or III-V semiconductors. Creative scientific and technological solutions are required enabling the implementation of optical loss reducing measures, which are compatible with the respective absorber material fabrication method.

As detailed in part 7.1 the distribution of solar photons to the different subcells is crucial

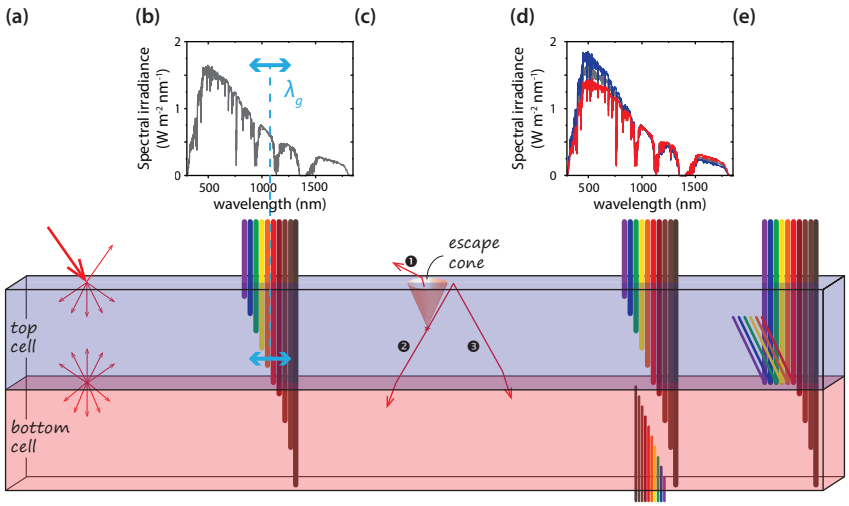

Fig. 20. Optical design of multi-junction solar cells requires the consideration of various aspects: a) Reduction of optical losses, b) bandgap engineering, c) luminescent coupling, d) illumination different from standard testing conditions, e) effective spectrum splitting.

for obtaining the highest power conversion efficiencies in multi-junction solar cells. For multi-junction solar cells, which are connected in series (2T configuration), current-matching is even *the* central design aspect, as here the overall current of the device is limited by the subcell with smallest short circuit current density. From an optical point of view several aspects must be therefore considered in multi-junction solar cells as illustrated in Figure 20.

b) **Bandgap engineering:** To tap the full efficiency potential of multi-junction solar cells and to optimally harvest the solar spectrum, the bandgaps of the subcells must be matched to each other (Figure 18d and e). While deviations from the ideal bandgap combination have less influence on the maximum achievable power conversion efficiency in the 4T configuration, there is a sharp maximum in the 2T configuration due to the current-matching constraint. The crystalline silicon bandgap can be regarded as fixed, whereas, in other solar cell material classes such as III-V semiconductors, perovskites, and CIGS, the bandgap can be more easily adapted by changing their compositions. It must be noted that bandgap engineering creates its own technological and material specific challenges such as a voltage deficit for wide bandgap perovskite semiconductors and chalcopyrite materials (see part 7.2).

c) **Luminescent coupling** is the sibling of the phenomenon photon recycling, which has already been described in Chapters 5 and 6. It occurs in semiconductors close to the radiative limit where excess carriers dominantly recombine by emission of radiation. The radiated photons from a subcell with a high bandgap can be coupled to an underlying subcell with a narrower bandgap and absorbed therein. Luminescent coupling can relax current-matching constraints if the multi-junction device is limited by a lower bandgap subcell. In this case, excess generated carriers in the wide bandgap subcell radiatively recombine and the radiated photons find their way to the narrow bandgap subcell where they can be absorbed.

d) **Variable illumination conditions:** Deviations from standard irradiance spectrum (AM1.5G) require solar cell design adjustments. In bifacial multi-junction solar cells, the rear-sided narrow bandgap subcell receives additional light, influenced by albedo, shadowing, and

varying illumination conditions. Spectrum shifts (blue or red) affect photon distribution among subcells. Independently connected multi-junction cells, like 4T tandems, are less sensitive to spectral changes and don't need current-matching. Detailed energy yield estimations (see Chapter 10), considering real solar spectra and annual yield, are necessary to determine the optimal configuration for bandgaps and layer thicknesses.

e) **Effective spectrum splitting:** Multi-junction solar cells need tailored optical measures to ensure each subcell absorbs its designated part of the solar spectrum. In layer stack geometry, structures or films between subcells must transmit photons below the top cell's bandgap to the narrow bandgap subcells and reflect higher energy photons back to the top cell to reduce thermalization losses. The spectrum can also be split using semi-transparent mirrors guiding different parts of the solar spectrum to spatially separated solar cells. Such a spectral splitter could be accompanied by a photonic structure that guides the light into trapped modes to enhance absorption in the respective sub-cells.

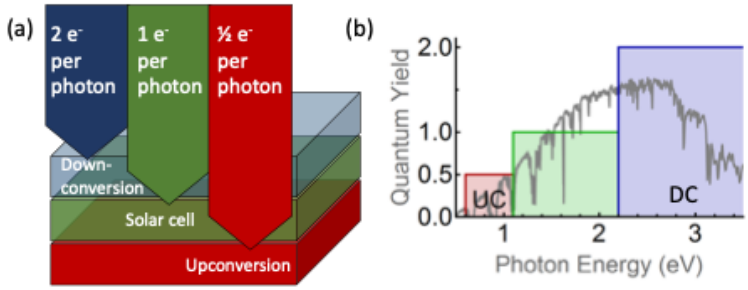

Fig. 21. (a) 3-bandgap single junction solar cell using a downconverter (blue, DC) to increase the energy converted from the high-energy part of the spectrum and an upconverter (red, UC) to convert previously unused below-bandgap photons, with (b) ideal quantum yield compared to the solar spectrum (grey).

8. Spectral shaping/conversion

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Conventional single junction solar cells are limited in efficiency because they absorb the broad solar spectrum by means of using a single, narrow bandgap. Any photon that is absorbed contributes the same energy for conversion, independent of the original photon energy. Tandem solar cells are the most prominent way to overcome this efficiency limitation, by dividing the spectrum into several parts, each absorbed by an individual sub-cell with better-matching bandgap (see Chapter 7). In this part we discuss optical ways to convert the solar spectrum into a spectrum that better matches to bandgap of the solar cell, which has a similar effect on the achievable efficiency [279, 280].

Broadly speaking there are three ways to convert the solar spectrum for better energy conversion, all of which require advances in light management for increasing efficiency Figure 21. The first is downconversion, the conversion of high-energy photons into a larger number of lower-energy photoexcitations. The second one is upconversion, where below-bandgap photons are converted into a (lower number) of above-bandgap photons. The third is to concentrate the sunlight at the expense of downconversion, often with luminescent solar concentrators. All categories increase the excitation density of a solar cell and thereby its power conversion efficiency.

8.1. Downshifting and Downconversion

A downconversion layer would be placed in front of the solar cell because it converts the high-energy light into lower-energy particles, either photons or excitons. Downconversion to increase the solar cell efficiency can be achieved with a range of different mechanisms. The simplest one is the absorption of photons in an area of the solar spectrum where the solar cell performs poorly, usually the UV part, and emission in an area where it performs well, often called downshifting [281]. To increase the efficiency, however, the radiative efficiency of the downconversion layer needs to be close to 1, and the emission needs to be coupled into the underlying solar cell. Silicon solar cells have improved their performance in the UV-part of the solar spectrum in the past years, so that need for such downshifting has shifted more towards a reduction of UV-induced degradation by absorbing the UV photons and downshifting them to a region where they can contribute to the photocurrent [282].

Downconversion by carrier multiplication, also called quantum cutting or photon multiplication, on the other hand, has potential for increasing the efficiency beyond the detailed-balance limit for a single-junction solar cell. In fact, the thermodynamic efficiency limit is almost the same

as with a two-terminal tandem cell [279]. In other words, a simple downconversion layer on a single-junction solar cell could be as efficient as a tandem solar cell.

The main material classes currently investigated for downconversion are organic materials that make use of singlet fission and rare-earth doped materials, including rare-earth doped high-bandgap perovskites. Singlet fission is a process in organic semiconductors by which a single photoexcited exciton is converted into a pair of excitons where each has roughly half the energy of the original excited state [283]. This conversion is possible because of the spin-nature of the exciton state in organic semiconductors. The photoexcited exciton is in a singlet configuration, but in organic semiconductors with a large exchange energy, the triplet exciton has a much lower energy. The combination of two triplet excitons can be in a singlet configuration, so that the conversion of a single singlet exciton into two triplet excitons is energy- and spin-allowed. Efficiencies of this conversion of 200% have been observed for pentacene [284], tetracene [285] and other materials [286, 287]. For the application in solar cells, these triplet excitons also need to have an energy larger than the bandgap of the solar cell, and the energy needs to be transferred to the solar cell. This transfer could be photonic by the transfer of the triplet exciton to a radiative emitter, but one could also imagine direct transfer of the charges or excitons. The direct transfer of energy has already been shown to contribute to the external quantum efficiency of a silicon solar cell [288,289] and has even lead to an improvement of the quantum efficiency recently [290]. However, each of these mechanisms has advantages and disadvantages, and it is not yet clear if any of these will be successful in increasing the overall solar cell power conversion efficiency. To do so, very stringent requirements for each step in the process need to be fulfilled.

For exciton or charge transfer, the distance of the downconversion material to the solar cell active layer needs to be within the transfer distance (charge or Dexter energy transfer), which is only a few nanometers [291]. This poses a range of practical challenges, for example the surface passivation in case of silicon solar cells [292]. The challenges associated with photonic transfer are, perhaps expectedly, more photonic in nature [293]. The triplet exciton is in itself not emissive, but it can transfer its energy to an emitter, for example a quantum dot [294, 295]. Then the emission needs to be directed towards the silicon solar cell, which can for example be achieved by careful placement of the emitter on top of a dielectric structure [296]. In addition, the contrast in refractive index between the organic material and the underlying solar cells helps in this directionality of emission. The third challenge is to shape the emission spectrum such that it can be optimally absorbed by the underlying solar cell. Especially in silicon solar cells, the absorption near the band edge is rather poor, so that the emission energy of the downconverter needs to be placed somewhat above the silicon bandgap. This poses a tradeoff, as the increase in emission energy also increases the energy from which it can absorb the photons it will downconvert (because of the thermodynamic requirement of energy conservation). Photonics can help in steering the light towards the underlying solar cell, and in increasing the absorption of the silicon solar cell in a narrow region around its bandgap [233]. Another, perhaps unexpected advantage of using an organic downconversion material is that it becomes transparent once it degrades. The downconversion foil then becomes a passive layer on top of the solar cell upon degradation, operating just like a normal single-junction solar cell [297]. This relaxes the requirement for the long lifetime of organic solar cells, which hampers many other applications of organic semiconductor in solar energy conversion.

Another way to efficiently downconvert high-energy photons is by the use of rare-earth doped large-bandgap perovskites [298, 299]. In these materials the term "quantum cutting" is commonly applied. Some rare-earth materials show emission close to the bandgap of silicon, and these materials are characterized by a very long emission timescale. To populate this emissive state, the strong absorption of the perovskite host is utilized. A large bandgap perovskite, for example $CsPbCl_3$ absorbs at an energy above twice the silicon bandgap. Providentially, in this material some rare earth ions such as Yb^{3+} assemble in a defect complex with a single metal vacancy

and two Yb^{3+} ions. In this configuration, the excitation in the perovskite quickly splits into two excitations on the Yb^{3+} ions via a defect state [300]. Once the ions are excited, the state is very stable and emits on a long lifetime. If this emission can be directed towards a silicon solar cell, then the quantum efficiency for conversion of high-energy photons could be increased. In addition to the light management challenges mentioned for the singlet fission downconversion systems, these quantum cutting systems experience power saturation, which means that the emissive states are populated faster than they emit light.

8.2. Upconversion

Upconversion for solar cells is an appealing prospect. All the photons below the bandgap energy in a solar cell are normally transmitted through the absorber layer and either emitted through the rear surface or, in case of a rear reflector, transmitted again though the absorber for emission through the front surface. On the way they have multiple occasions to be absorbed to generate parasitic heat. If these photons could be converted into electrical energy, the efficiency would be improved, and the cell temperature potentially reduced [301].

An upconversion layer would be placed behind the active layer of a solar cell to absorb only the photons transmitted by the cell. This requires both electrical contacts to be transparent, similar to a front cell in a four-terminal tandem solar cell, with all the light-management challenges associated with transparent contacts (see Chapter 4). Just like downconversion, upconversion can proceed via lanthanide ions or in organic semiconductor materials.

In organic semiconductors it proceeds via the annihilation of triplet excitons (triplet-triplet annihilation, TTA), as the reverse process of the above-mentioned singlet fission. For a solar cell, the triplet excitons need to be photogenerated. Since the direct absorption of light to generate triplet excitons is spin-forbidden, it is extremely weak in materials with small spin-orbit coupling such as typical organic semiconductors. However, the triplet excitons can be generated by a senstizer, such as an inorganic quantum dot or metallated porphyrin molecules [301]. For solar cells, however, these donors would need to absorb below the bandgap of silicon. There are only few examples of semiconductors with triplet excitons that have an energy below the silicon bandgap and upconversion from that spectral region has only been demonstrated recently [302].

In lanthanide ions, the upconversion process combines the energy of two infrared (IR) photons to promote the upconversion material to a higher-energy excited state [303–305]. From this state, either a photon with an energy that is approximately doubled with respect to the initial IR photon is emitted to be absorbed by the silicon active layer, or the double-energy exciton is transferred to the silicon cell, and directly split into charges. Combinations of lanthanide ions with the proper energy level structure allows for the two consecutive energy transfer steps in which a neighboring lanthanide ion is raised from the ground state to an excited state. When the system is in the (long-lived) first excited state, a second transfer raises the ion to a higher excited state giving upconversion emission of photons of higher energy. Upconversion efficiencies of 12% have been realized for monochromatic excitation [306]. A known drawback of the lanthanide-based approach is that the IR absorption is weak and spectrally narrow. Similarly to the TTA upconversion, this can be overcome by functionalizing lanthanides nanoparticles (NPs) with antennas which transfer the absorbed energy to the NP core where the upconversion takes place. Broad-band absorption in dye-sensitized upconversion has been reported for NIR-to-visible upconversion [307–309] but so far not for IR-to-NIR upconversion as required for c-Si solar cells.

8.3. Luminescent solar concentrators

Luminescent solar concentrators (LSC) consist of large sheets of transparent materials, such as polymers or glass, embedded with pigments known as dyes or luminophores. Luminophores absorb sunlight and subsequently re-emit fluorescent light, which is then guided and concentrated towards small solar cells positioned either at the back or at the edges of the sheet (Figure 22).

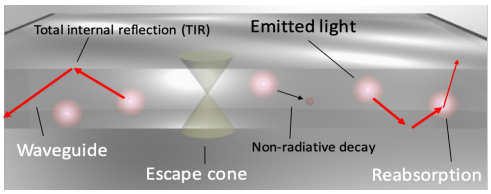


Fig. 22. Schematic of the working principle of LSCs

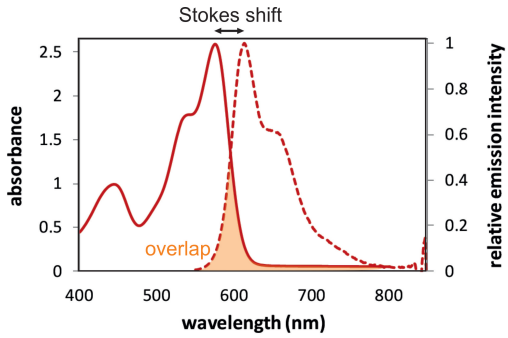


Fig. 23. Representative absorption and emission spectra of a fluorescent dye (Lumogen F Red 305 (200 ppm) in PMMA), highlighting the spectral shift between the two processes (i.e. Stokes shift). The shaded area indicates the spectral overlap between absorption and emission (adapted with permission from Ref. [317]).

This dramatically reduces the area of solar cells needed, as in traditional concentrators. Unlike conventional light concentrating methods (i.e. with lenses), LSCs exhibit the unique capability to effectively concentrate diffuse irradiance in addition to the direct irradiance, a significant component of solar radiation scattered by the atmosphere and terrestrial surfaces, and thus it eliminates the need for tracking. Although the functional principle of LSCs was originally proposed in the late 1970s [310, 311] reported concentration efficiencies are still far below the theoretical limit and scalability poses a challenge [312].

LSCs involve two key optical components: luminophores and the sheet waveguide. Luminophores are typically organic dyes or inorganic quantum dots that absorb well-defined spectral bands from the incident sunlight, which is then isotropically emitted with lower energy photons due to the Stokes shift. Organic dyes, such as various types of chromophores, offer tunability in terms of absorption and emission wavelengths through chemical modification of their molecular structures. Inorganic quantum dots, on the other hand, exhibit size-dependent optical properties, allowing precise control over absorption and emission spectra by adjusting their nanoparticle dimensions [313]. Both organic dyes and inorganic quantum dots have been extensively studied and employed as luminophores in LSCs due to their high quantum efficiency, photostability, and compatibility with transparent substrates [314].

From the photonic perspective, LSCs are capable of concentrating light with a wide angular distribution into waveguided light with a narrow angular distribution, thereby reducing photon entropy. The second law of thermodynamics requires that this reduction in photon entropy is balanced by a reduction in photon energy, leading to a minimum required Stokes shift that increases logarithmically with concentration factor [315]. For instance, a concentration of 100 requires a minimum Stokes shift of $\approx$ 100 meV. While Stokes shifts as large as 200 meV have been reported, the practical concentration factor scales sub-linearly with the sheet size or luminophore density [316].

Just because a photon has been confined within the lightguide, it does not necessarily mean that it will actually make it to the PV element. Two main fundamental challenges hamper scalability of LSCs in terms of waveguide length. Firstly, fluorescent light can be re-absorbed by other luminescent particles (or even the matrix material) intercepting the optical path of photons if the overlap between the emission and absorption spectra is large (shaded area in Figure 23). Because fluorescent light is emitted in a random direction, light emitted within the escape cone of the glass-air interface will unfortunately out-couple from the waveguide. This results in the gradual reduction of light intensity with concentrator size [318].

Many efforts have been focused on the chemical manipulation of luminophores to minimize spectral overlap without excessive Stokes shift. Bronstein et al. [319] showed that LSC's doped with CdSe/CdS QDs can exhibit 30-fold concentration of irradiance. This is achieved by coupling of a wavelength-selective photonic mirror to an LSC to form an optical cavity where emitted luminescence is trapped. Li et al. [320] used colloidal core/shell QDs resulting in efficiencies of more than 10% for dimensions of tens of centimeters. For even larger LSCs one also needs to consider the matrix material, as even the weak absorption of vibrational modes can become significant [321].

8.4. Advances needed

In conclusion, spectral shaping and conversion could play a significant role in increasing the efficiency and applicability of solar energy. In the future, the optical challenges in the field can be summarized by:

Optical coupling: Increasing the power conversion efficiency by up-and downconversion requires that the emission needs to be directed towards the solar cell, and the conversion efficiency of the underlying solar cell needs to be high enough in the spectral range where the photon multiplier emits. Therefore, directional emission of these photons, or scattering into the correct angular emission is required. The emission is typically very narrow-band, which suggests that a suitable nanostructure could direct the light. Another aspect of optical coupling is to maximize the absorption strength of the solar cell in the spectral region where the up- or downconverter emits.

Power saturation: Besides the optical coupling, the rare-earth photon multipliers pose an additional challenge. The slow emission efficiency of the rare-earth emitter yields power saturation once the incoming photon flux is too high [322]. The excitation rate cannot be higher than the emission rate, which means that the density of emitters needs to be maximized and at the same time the incoming power needs to be distributed in an optimal fashion throughout the downconverter. The power saturation only plays a role at high solar intensities, but can still limit the efficiency gain from the photon multiplier. Photonics could play a role by reducing the lifetime of the emitters by increasing the local density of states the material can emit into. Other optical ways to distribute the incoming solar intensity into different, spatially separated parts with its own emitters might further decrease the density of excitations that the rare-earth ions need to carry. Despite all these challenges, an increase in power conversion efficiency has been demonstrated [323], which indicates the exciting opportunity these downconverters offer.

Transmission of upconverted light: The light management challenges for upconverters are subtly different from those for downconverters. While for upconverters the light needs to be steered towards the solar cell, this can be trivially achieved for upconverters with a simple mirror on the back of the solar cell stack. However, for solar cells the upconversion layer is ideally optically thick, which means that it absorbs all light below the silicon bandgap but above its own bandgap. However, this poses a challenge. The higher-energy

emitted light is likely to be self-absorbed, reducing the number of upconverted photons hitting the solar cell. One way around this limitation would be to transmit the high-energy upconverted exciton into the solar cell by energy transfer or charge transfer, which has not been demonstrated to date. Alternatively, one needs to engineer a transmission window into the upconversion layer in the spectral range where the upconverter emits. This could be achieved by fabricating the upconverter from a dye that is optically thick in the IR, but has an transmission gap in the NIR. Alternatively, photonic strategies might be developed to generate the transmission gap.

Breaking reciprocity for efficient LSCs: Reciprocity requires that incoupling and absorption efficiency of sunlight must be the same as outcoupling and emission efficiency for the same photon energy and angle. This means that efficient incoupling of sunlight and waveguiding of emitted light can only occur simultaneously if there are large asymmetries in the angular and energy distribution of incoming and emitted light. Otherwise, any attempts to improve waveguiding will simply increase the reflection of sunlight from the LSC surface. New advanced photonic nano-designs are needed to break the reciprocity, taking advantadge of the fact that the wavelength of absorbed and waveguided light is fundamentally different. For instance, fine-tuning directional emission in the in-plane of the waveguide would minimize escape cone losses.

9. Optics for thermal management of photovoltaic modules

J. MANDAL, A. P. RAMAN

A central challenge facing photovoltaic modules operating in the field is the elevated temperatures they typically encounter. Under hot ambient conditions and parasitic heating by sunlight, a typical solar module can easily reach 55–60°C in typical scenarios, and significantly higher temperatures in hot desert environments where large PV systems are often deployed, or in concentrator architectures [324, 325]. The source of this heating is both due to fundamental heat generation mechanisms in the active photovoltaic material and also due to absorbed sub-bandgap light in other materials in the overall PV module architecture such as front- and back-sheets, metallic reflectors and cover glass. These elevated temperatures, distinct from the lab-scale conditions often used to report solar efficiencies, can greatly reduce both the practical operating efficiency and lifetime of the module [326]. Thus, in recent years, thermal management has emerged as an important research field to improve the real-world operating efficiency and lifetime of photovoltaic modules.

Optics and photonics hold the potential to play a unique, perhaps essential role in enhancing thermal management of photovoltaic panels through two separate but related mechanisms: 1) maximizing radiative cooling to the sky to enhance heat loss; 2) reflecting sub-bandgap photons that would otherwise parasitically heat the photovoltaic module and not be usable by the active layer. Here, we highlight past work on both these efforts and opportunities that lie ahead to enable effective scaling of these concepts to the Terawatt scale.

9.1. Radiative cooling of photovoltaic modules

While the Sun represents the ultimate renewable heat source accessible to us here on Earth, our planet is also surrounded by the ultimate heat sink: outer space itself. Radiative cooling refers to the harnessing of this heat sink by radiative heat transfer of terrestrial objects that face the sky. As all terrestrial objects under the sky are heated by sunlight, so do they radiate some of their heat upwards as longwave radiation. While the atmosphere does absorb and send back much of this thermal radiation, a significant fraction eventually escapes to space, thereby enabling a sky-facing surface to cool itself down passively below its surroundings [327, 328]. Radiative cooling thus represents a complementary technology to solar-based technologies; where solar systems harness the heat of the sun for either thermal or electrical ends, radiative cooling enables cooling that could also be leveraged for either thermal or electrical work.

Recent interest in radiative cooling has largely been motivated by sub-ambient daytime radiative cooling, first demonstrated in 2014 [329]. The considerations for daytime radiative cooling are primarily around high solar reflectance and suitably high thermal emittance . Given the goal of daytime radiative cooling is to maintain sub-ambient temperatures, it has also been noted that *selective* thermal emittance—preferential thermal emission within the primary atmospheric window between 8 and 13 µm—can allow objects to reach colder temperatures than with a blackbody, if the radiative cooling surface is sufficiently insulated. Such considerations however do not apply to radiative cooling of photovoltaic modules.

9.1.1. Radiative cooling heat transfer model

We briefly elucidate the radiative heat flows experienced by a PV module outdoors. Consider a PV module with spectral angular emissivity $\epsilon(\lambda, \Omega)$ at a temperature T. When the PV module is exposed outdoors it is subject to both solar irradiance, and thermal radiation from the atmosphere (corresponding to ambient air temperature T_{amb}). The PV module's steady state temperature T is determined from the following heat balance equation:

$$P_{\text{rad}}(T) - P_{\text{atm}}(T_{\text{amb}}) - P_{\text{sun}} + P_{\text{cond+conv}} = 0. \tag{6}$$

In Eq. (6), the thermal emission power radiated out by the PV module as a whole is

$$P_{\text{rad}}(T) = \int \mathrm{d}\Omega \cos\theta \int_0^\infty \mathrm{d}\lambda \, I_{\text{BB}}(T,\lambda)\epsilon(\lambda,\Omega). \tag{7}$$

Here,

$$\int \mathrm{d}\Omega = \int_0^{\frac{\pi}{2}} \mathrm{d}\theta \sin\theta \int_0^{2\pi} \mathrm{d}\phi$$

is the hemispherical integral,

$$I_{\text{BB}}(T,\lambda) = \frac{2hc^2}{\lambda^5} \frac{1}{\exp\left(\frac{hc}{\lambda k_B T}\right) - 1}$$

is the spectral radiance of a blackbody at temperature T. h is the Planck constant, c is the velocity of light, k_B is the Boltzmann constant, and λ is the wavelength of emitted light.

$$P_{\text{atm}}(T_{\text{amb}}) = \int \mathrm{d}\Omega \cos\theta \int_0^\infty \mathrm{d}\lambda \, I_{\text{BB}}(T_{\text{amb}},\lambda)\epsilon(\lambda,\Omega)\epsilon_{\text{atm}}(\lambda,\Omega), \tag{8}$$

is the downwelling atmospheric irradiance absorbed the PV module.

$$P_{\text{sun}} = \int_0^\infty \mathrm{d}\lambda \, \epsilon(\lambda,\theta_{\text{sun}}) I_{\text{AM1.5}}(\lambda) \cos(\theta_{\text{sun}}) \tag{9}$$

is the absorbed solar power (including for example sub-bandgap light) that collectively results in heating of the solar module. In Eqs. (8) and (9), we have used Kirchhoff's law to replace absorptivity with emissivity $\epsilon(\lambda,\Omega)$.

The angle-dependent emissivity of the atmosphere is given by

$$\epsilon_{\text{atm}}(\lambda,\Omega) = 1 - t(\lambda)^{1/\cos\theta}, \tag{10}$$

where $t(\lambda)$ is the atmospheric transmittance in the zenith direction. The solar irradiance is represented by the AM1.5 spectrum. The P_{sun} is devoid of an angular integral, and the structure's emissivity is represented by its value at incidence angle θ_{sun}. Finally,

$$P_{\text{cond+conv}} = h_c \left(T - T_{\text{amb}}\right), \tag{11}$$

is heat loss due to non-radiative heat exchange. Here h_c is a total non-radiative heat coefficient that accounts for conductive and convective processes due to the contact of the PV module with its immediate environment.

PV modules will necessarily operate at significantly above-ambient temperatures during the daytime under sunlight due to P_{sun} being significantly larger than net cooling at T_{amb} at long-wave infrared wavelengths [i.e. $P_{\text{rad}}(T_{\text{amb}} - P_{\text{atm}}(T_{\text{amb}})$]. Thus the primary goal of radiative cooling in the context of PV modules is to maximize their infrared emissivity over all relevant thermal wavelengths; i.e. to ensure the module as a whole behaves as a blackbody [330, 331]. This is distinct from goals of enable selective infrared emissivity within the atmospheric window one typically encounters with daytime radiative cooling, where the goal is to reach sub-ambient temperatures. Since we expect steady-state temperatures to be well above ambient, high broadband emissivity is the goal. While a nominally simple goal, this task has had a fundamental technical challenge associated with it: the glass panels that form the top layer of most PV modules have comparatively low emissivity (0.84) due to the *Reststrahlen* band of SiO_2, the primary constituent material in typical solar glass.

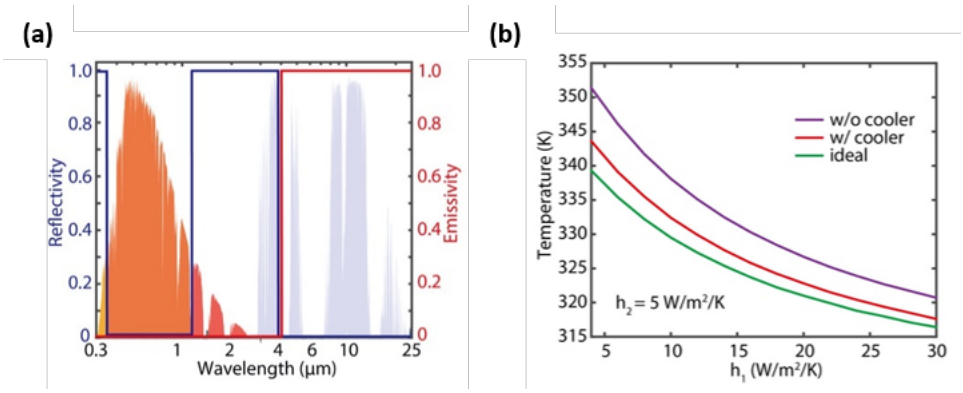


Fig. 24. a) The ideal spectral reflectivity and emissivity of a photovoltaic module. Sub-bandgap solar light is perfectly reflected (here assuming Si's bandgap), while over long-wave infrared wavelengths > 1 μm the module exhibits unity emissivity. b) The temperature impact of the ideal surface compared to a photonic design as well as baseline glass, for values of convective heat exchange on the front and back surface. In relatively modest wind conditions a temperature difference of > 10 K is possible, yielding substantial gains in operating efficiency and improved module lifetime. (Adapted with permission from Ref. [335]. © 2017 American Chemical Society.)

9.1.2. Photonic strategies to enhance emissivity

Early work identified a remarkable opportunity if the emissivity of front-surface glass were enhanced to ≈ 1 while maintaining net transmittance into the underlying solar cell: in hot, desert conditions, where radiative cooling effects are particularly prominent, a temperature reduction of as much as 5°C might be accessible [330]. Later experimental work introduced a photonic crystal into the front surface of a silica wafer atop a Silicon absorber, demonstrating a 1°C temperature reduction in more temperate weather conditions [332]. Crucially, this design demonstrated a slight light trapping effect as well, ensuring that the amount of sunlight reaching the underlying photovoltaic material actually exceeded that of the baseline glass scenario.

Motivated by these demonstrations, several strategies have been explored to enhance front-surface glass emissivity, from microspheres and voids, to multilayer thin films [333–338]. The latter strategy is the most easily scalable, but enhanced emissivity over long-wave infrared wavelengths has resulted in quite thick designs, posing potential cost challenges. Such an approach may be particularly important for concentrating photovoltaics [339], where strategies involving adjacent daytime radiative cooling surfaces for heat rejection have also been demonstrated [340].

9.2. Integrated sub-bandgap sunlight reflection

A related thermal management strategy has also emerged in recent years: reflecting sub-bandgap sunlight, thereby minimizing parasitic heating from these otherwise useless photons in various constituent layers inside a PV module [335, 337]. A key parameter explored has been placing such a selective reflector either on the front surface of the glass, or immediately beneath it [335, 341–343]. An advantage of placing the spectrally selective reflector on the front surface is that one can, in principle, simultaneously optimize for three factors: i) sub-bandgap reflection, ii) infrared emissivity, and iii) anti-reflection over above-bandgap solar wavelengths.

This functionality, the ideal form of which is depicted in Fig. 24a, could have a significant impact on overall operating temperature of a solar module, as illustrated in Fig. 24b. In low wind conditions, for instance, the net impact of this relative to a baseline glass-based solar module

could be greater than 10°C temperature reductions.

9.3. Towards cooler and more climate-friendly photovoltaic panels

Photovoltaic energy conversion, and the parasitic heating accompanying the process, mean that PV panels have two distinct effects on the climate. The conversion of solar energy to electricity is a zero carbon process and helps to reduce greenhouse gas emissions. This emissions reduction in turn reduces greenhouse heat trapping in the atmosphere, making photovoltaic panels critical for climate change mitigation [344]. On the other hand, the dissipation of absorbed heat into the environment represents a weaker but significant antagonistic effect. The high operational temperatures of PV panels, arising from their parasitic solar heating and less than ideal thermal emittance, causes them to convectively and radiatively dissipate significant low-grade heat that is trapped in their environment. This warming effect on Earth, while significantly smaller than the cooling effect of CO_2 emissions reductions, does reduce the net environmental benefit. Secondly, heat from large-scale deployment of PV panels can lead to photovoltaic heat islands [345, 346]. In built environments, this can raise cooling loads, causing part of the renewable energy generated by PV panels to effectively be used to mitigate their own heating effect. This reduces both the climate change reductions benefit and effective efficiency of PV panels.

By reflecting solar wavelengths that would be converted to parasitic heat, and increasing the emittance of PV panels in the longwave atmospheric transmittance window, radiative coolers cool PV panels by sending heat to space and reduce their heating impact on the environment. Relative to ordinary photovoltaic panels, this leads to a cooling impact, as well as better overall energy utilization by lowering self-generated cooling loads. While inferable from first principles, accurately quantifying these benefits of radiative coolers requires systematic studies that consider not only the energy-generation or optical and thermal aspects of PV panels, but also their intersections with the energy infrastructure, and built and broader environments.

9.4. Advances needed

While intriguing in its potential, the role of optics for PV thermal management faces numerous challenges. Optimal designs that can deliver functionality close to that of the ideal spectral response have entailed either very thick multi-layer thin film stacks, or complex patterning into the front surface of PV panels. Given the cost sensitivity of PV modules both these approaches face numerous practical challenges for wider adoption. An alternate approach has been to explore significantly simpler designs, often single or bilayer coatings made of low-cost materials. These designs can easily deliver small increases in sub-bandgap reflection (low 10s of W/m^2 reduction in heating), but ultimately may yield only 1°C reductions in operating temperature.

Enhancing infrared emissivity via a thin film approach that preserves other optical requirements has typically entailed significantly thicker films. However, lower cost materials, including a range of UV-stabilized polymer films with suitable emissivity may play a useful role here. Alternatively, low-cost chemical processing of the front surface of the glass to introduce tailored microstructures may yield desired optical functionalities. While a broad range of strategies have been explored in literature, a practical, scalable and low-cost approach that might yield multiple degrees °C of cooling remains lacking, and represents an exciting opportunity for terawatt-scale photovoltaics.

It is also important to note that the impact of radiatively cooling photovoltaic panels remain to be wholistically calculated. Prior works in the literature have quantified the benefits for individual PV panels [347]. However, such models assume major convective cooling into the environment - in reality, PV panels often exist as arrays, with convective heat dissipation impacting the performance of neighboring PV panels. In other words, convection may be less effective in such cases, and the impact of radiatively cooling PV panels on energy yields may be considerably greater than what single-panel models indicate. Likewise, the potential urban climate impact of radiatively cooling widely deployed rooftop solar panels may also also increase the effective

efficiency of PV panels by reducing urban cooling loads. Further research on these topics can motivate material and optical design of thermal management strategies for PV panels.

10. Beyond standard testing conditions: Illumination models for accurate energy yield prediction

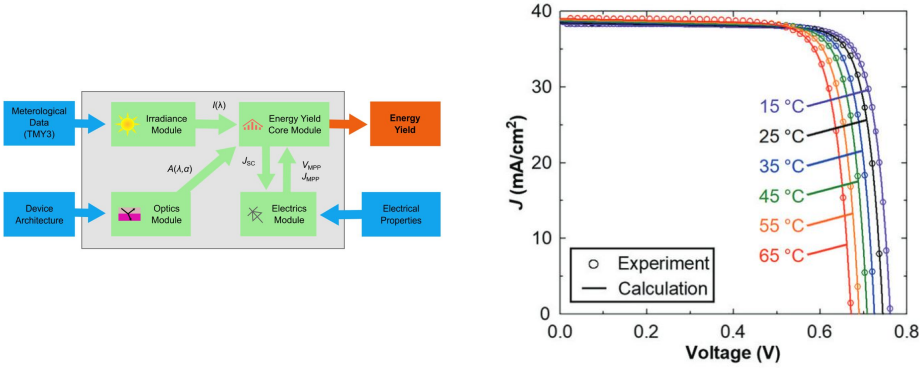
M. JOŠT, U. PAETZOLD, R. SAIVE

The performance of photovoltaic (PV) systems is assessed by a variety of key performance indicators such as levelized cost of electricity (LCOE), energy payback time (EPT), emissions per kWh, or resource efficiency. All of these performance indicators assess the total amount of energy harvested from the PV installation, taking into consideration seasonal and daily variations in irradiation conditions, spectrum, temperature, as well as all the details of the installation (e.g. module orientation, type of tracking, shadows, soiling, etc.). Therefore, predicting energy yield (EY) is pivotal for PV systems and device architecture design of solar modules. While reasonable extrapolations can be made from the power conversion efficiency (PCE) to the EY for many opaque single junction PV technologies installed in terrestrial locations, the PCE fails to provide accurate design rules for more complex device architecture or application scenarios. Prominent examples that require detailed energy yield modelling and will be discussed in the following are: (A) optimization of more complex multi-junction PV technologies (e.g. perovskite-silicon tandem PV) and (B) bifacial PV. For example, it was shown in that the PCE determined under standard test conditions is not suitable to determine the optimal bandgap combination of perovskite-silicon tandem solar cells nor the perovskite layer thickness in bifacial perovskite-silicon tandem solar cells [254, 348, 349].

10.1. Performing energy yield calculations

In energy yield modeling, the energy produced over a whole year is calculated by integrating the generated energy of a solar module (or solar cell) produced for given time intervals, e.g., every hour over a year. The basic approach is illustrated in Figure 25a. It comprises, as depicted with green boxes, (1) determining the irradiation conditions and outdoor temperature, (2) determining the optics of the solar cell for a given angle of incidence, (3) the electrical characteristics of the solar cell for a given interconnection scheme and generation rate in each subcell, and (4) the energy yield calculation itself, which represents an integral over a representative time period, taking into consideration the installation aspects such as solar module, tracking systems or bifacial characteristics of the PV system. The EY modelling requires three key input parameters, depicted with blue boxes: i) position of the sun, spectral irradiance (diffuse and specular) and air (or module) temperature at a given time, and ii) optical response (EQE) for a given angle of incidence and photon energy and iii) the electrical device performance for a given generation rate and temperature.

Obtaining the whole set of input parameters can be challenging. i) depends on geographical parameters (position of the sun on the horizon, surface) and weather conditions, namely direct and diffuse irradiance, air temperature and wind speed. The complete experimental datasets of spectrally and timely resolved irradiance that discriminates between specular and diffuse irradiance are extremely rare and, in most cases, only available for limited or incomplete periods (e.g. one or two years). Such short periods are not enough for general conclusions as the data could be from a hot and sunny, or cloudy and rainy year. For these reasons, most EY modelling studies are based on the typical meteorological year (TMY) dataset, which comprises the weather data of twelve years. NREL provides TMY dataset for the U.S.A. in their NSRDB database [352, 353], and it has recently been upgraded to cover the whole world. Alternatively, SMARTS model can be used to generate, the so-called "clear sky" irradiance data [354, 355]. In combination with a cloud model this data can provide an hourly and spectrally resolved dataset of specular and diffuse irradiance data for a wide range of locations covering most of the relevant climate zones. The module temperature is often calculated from ambient conditions through models such as, e.g. the NOCT, Ross or Duffie-Beckman model [356, 357]. Especially NOCT



(a) (b)

Fig. 25. Schematic flow of the modular EY modelling. The irradiance module computes the spectral irradiance I, the optics module the absorptance A, and the energy yield module calculates the short-circuit current density J_{SC} and EY with the help of the electrics module. b) Temperature variations of *J-V* characteristics of a Si heterojunction solar cell with a certified efficiency of 23.27%. The open circles show the experimentally derived data, whereas solid lines indicate the fitted results. [(a) reprinted from Ref. [350], (b) reprinted with permission from Ref. [351], © 2022 John Wiley & Sons Ltd.]

model is often employed due to the absence of better models and/or a detailed knowledge of the temperature in the solar module. All in all, the inclusion of temperature into the energy yield model can induce a 5 to 10% penalty [262] (Figure 26b), depending on the temperature coefficient of the studied structure. This makes an efficient thermal management key to obtaining high energy yield. For example, longwave heat flow, which is in details discussed in Chapter 9, can help reduce the operational temperature of the PV modules and increase the energy yield.

The ii) describes optical performance (EQE, and consequently J_{SC}) at different incident angles that occur during the suns path over the horizon. It is usually provided by performing optical simulations of the device stack using ray tracing and transfer matrix models, for which inputs are the thicknesses and refractive indices of the layers. These calculations can take some time, especially if the thicker, textured layers that require ray tracing are included, such as glass, encapsulant and silicon. However, they can be prepared in advance for the selected device stack and integrated in the energy yield model [350].

Finally, iii) the electrical performance at different temperatures and irradiances can be measured in laboratory by e.g. changing temperature and irradiance of the sun simulator in a wide range (25–85 °C and 100 to 1200 W/m^2 should cover most locations, Figure 25b, or by simulating *J-V* curves using one-diode parameters. For each interval in a year, a PMPP from the *J-V* curve is selected based on outdoor conditions and optical response, and summed over a year. The complete methodology of energy yield calculations has been throughly described in [349, 350].

Further analysis of energy yield results can be used either in hourly intervals or integrated over a year. The latter is useful to compare locations, technologies and orientations and is in more detail analyzed below. The former, however, is especially handy when determining the short-term stability in outdoor testing of novel technologies, such as perovskite solar cells, where stability is measured in weeks or months rather than years as in the case of the established silicon modules. Thus it is important to regularly and continuously track the degradation of devices. This is not trivial, since diurnal and weather changes make it hard to estimate devices performance [358] as

the device output is determined by irradiance, angle of the sun and temperature, all important parameters of energy yield modelling. Therefore, by comparing the device output with the energy yield simulations [359] can serve as an efficient tool to estimate and monitor device performance in outdoor operation, and in turn keep track of possible degradation or potential other effects, such as light soaking.

10.2. Energy yield modelling for perovskite-based tandem solar cells

A prominent example of the importance of energy yield modelling is the performance of multi-junction solar cells in terrestrial applications. The multi-junction concept and their main optic challenges are covered in Chapter 7, while here we will focus on the perovskite-based tandem solar cells. To extract as much current out of the tandem device as possible, optimal balance between the two (or more) subcells has to be achieved, namely their current matching. This is typically done for AM1.5G irradiance as defined in STC, optimizing the device layer stack in terms of perovskite bandgap and thicknesses of all the layers. Using simulations, one could easily compare the PCE potential of single-junction devices with tandem devices, either in monolithic 2T, 3T or 4T configurations. And, importantly, also optimize device fabrication towards record PCEs, measured at certification labs under STC.

While this is necessary to reach high certified PCEs, the outdoor conditions often significantly defer from STC, both in temperature, irradiance intensity and its spectra. Especially temperature and spectra influence the ratio between the currents produced in the subcells and their current matching [360, 361]. For example, the irradiance spectra in several different KGPV zones [362] in U.S.A. (NREL database) is blue rich, causing more current in the top cell compared to the AM1.5 condition and consequently not extracting all the potential from the tandem device. Thus, the AM1.5 optimization is often not the perfect case for best outdoor operation (Figure 26c). Instead, a more thorough analysis involving energy yield calculations have soon appeared, providing fairer comparison through better and more complete results [349]. Optimizing tandem device architectures (in most cases this means perovskite bandgap and potentially also its thickness [363, 364], Figure 26d for maximal generated energy over the year has shown that wider perovskite bandgaps are required in case of blue rich spectra. This result is not only important for tandem design to achieve the highest energy generation but also from stability perspective, since wider perovskite bandgap is obtained with higher bromide content and thus more prone to phase segregation [365].

Typical application of energy yield in perovskite-based tandem research have been calculations of energy produced at different geographical locations. This allows comparison between sunnier and cloudier places as well as hotter, colder and rainier. It can even indicate if the device stack has to be adapted for different locations or climate zones. Due to availability of the input weather dataset, such calculations have mostly been applied to locations within U.S.A. (Figure 26). Similarly important are also comparisons between single junction and 2T or 4T devices (Figure 26a), as well as the analysis of bifacial modules that are entering the market as a single-junction technology but might become profitable also for the tandems [255, 256]. Such calculations can present accurate benefits of tandem architecture and can also serve as guidelines for business models. For example, if the perovskite/silicon tandem produces 40% more energy than silicon single-junction device, then the additional costs of perovskite fabrication should not exceed 40%. Finally, static, 1-axis or 2-axis tracking operation can be efficiently estimated with energy yield [366]. The tracking can increase the generated energy by 30%, however, the amount of energy for tracking and cost of the tracking system often make such systems unprofitable.

10.3. EY in bifacial photovoltaics: challenges and opportunities

In assessing realistic irradiance conditions, it becomes evident that the incident illumination in real world applications of solar modules is not solely derived by direct sunlight and light diffused

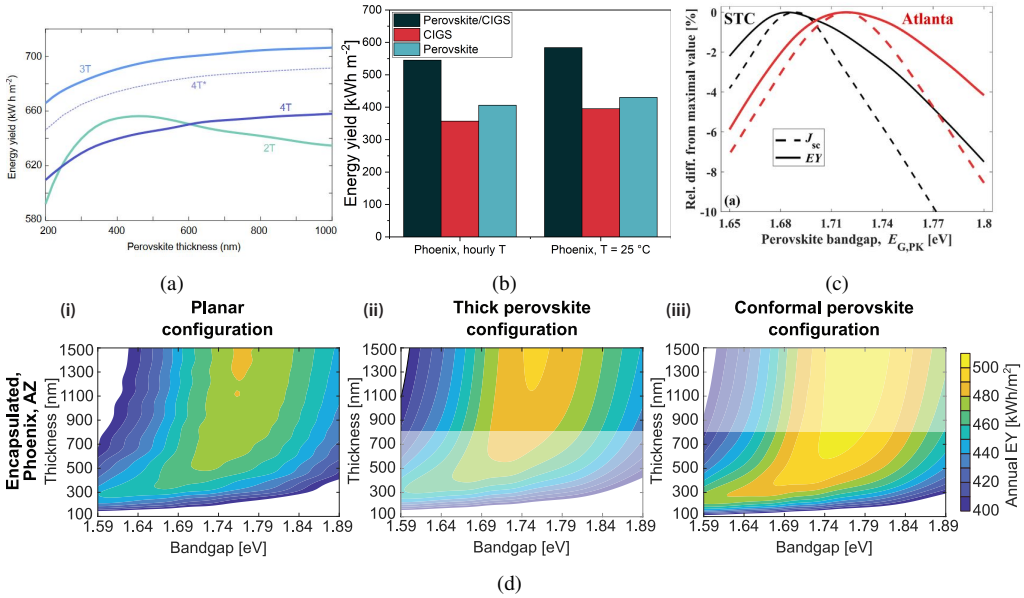
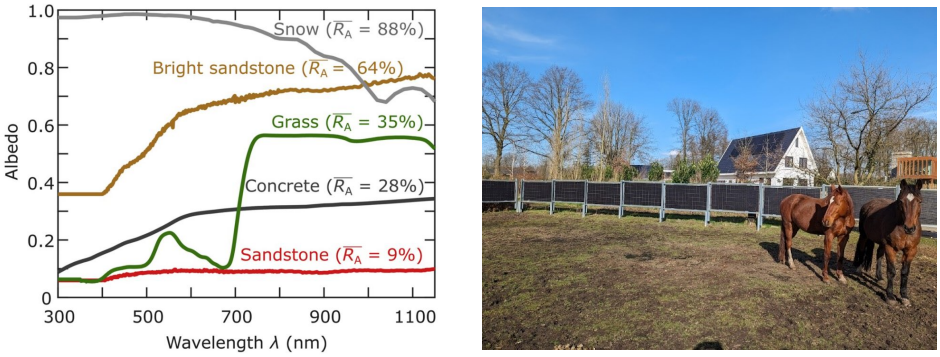


Fig. 26. (a) Annual EY as a function of the perovskite thickness for 2T, 3T, and 4T architectures. Results for state-of-the-art morphologies: double-textured c-Si bottom cell, with conformal perovskite top cell in 2T and 3T architectures and planar top cell in 4T architecture are illustrated with solid lines. Results for a hypothetical 4T architecture with textured perovskite top cell, labeled as 4T*, are drawn with a dashed line. The band gap of the perovskite layer is 1.72 eV. (b) Energy yield of perovskite/CIGS, CIGS and perovskite technologies. Encapsulated devices were considered. Bars on the left show the case where hourly temperatures (daily profiles) were considered, while the bars on the right show results where temperature was fixed to 25 °C. (c) Relative losses of short-circuit current density and energy yield as a function of EG,PK for the cases of STC and Atlanta-specific realistic operating conditions. (d) Contour plots showing the PCE as a function of perovskite bandgap and thickness for encapsulated tandem solar cells with planar (i), thick perovskite (ii) and conformal perovskite (iii) morphologies. [(a) reprinted from Ref. [348] with permission from Elsevier, (b) reprinted from Ref. [262], (c) reprinted from Ref. [349], (d) adapted from Ref. [364].]

at the sky (i.e. clouds). Surrounding elements such as the ground and buildings also reflect light, contributing significantly to irradiance from below [367, 368]. This phenomenon, typically measured as albedo or the reflectivity of a surface, plays a crucial role in determining the overall irradiance. For instance, water surfaces, with an albedo of less than 10%, absorb most sunlight, whereas snow, with an albedo of 90%, reflects nearly all incoming light. Given that the energy output of a solar power installation is highly sensitive to the incoming light spectrum, the spectral characteristics of albedo are vital for optimizing solar energy yield, as depicted in Figure 27a, which illustrates the spectral albedo of common surfaces.

Scattered light, emanating from both the sky and terrestrial surroundings, necessitates the design of solar modules capable of capturing light from multiple directions. Bifacial solar panels, which harness light from both their front and rear faces, have emerged as a solution, enhancing energy yield through novel configuration possibilities [369]. However, the integration of albedo light from various angles, combined with new application scenarios, significantly complicates accurate yield forecasting. To address this, recent efforts have focused on employing optics and optical simulation techniques [370–375] to refine energy yield predictions for bifacial installations



(a) (b)

Fig. 27. Reflection spectra of grounds used for the simulation of albedo irradiance. Additionally, the mean albedo of each ground in the wavelength range of 300–1150 nm is specified in the legend (reprinted from Ref. [254] with permission from Elsevier; original data taken from ecosystem spaceborne thermal radiometer experiment on space station (ECOSTRESS) spectral library). b) Bifacial solar fence used for a horse pasture.

under realistic conditions [367, 368]. Such analyses must account for the spectral [376–380] and angular [367, 368, 381] distribution of incoming light, alongside realistic reflections on system losses and gains, necessitating advanced irradiance models or measurements and detailed optical simulations. This complexity underscores the need for efficient algorithms [382] capable of navigating vast data sets and multi-dimensional parameter spaces, presenting a ripe area for research and development within the optics community. The incorporation of machine learning and artificial intelligence stands to significantly expedite this process.

The International Technology Roadmap for Photovoltaics (ITRPV) 2024 [3] highlights the growing dominance of bifacial solar cells, which currently constitute 85% of the market, with projections suggesting an increase to 90% over the next decade. Although not all these cells are utilized in bifacial modules, the market share of such modules is expected to rise from 50% to over 70% by 2034. This trend is buoyed by the enhanced performance and versatility afforded by bifacial technologies. Notably, applications such as bifacial solar fences (e.g. Figure 27b) and sound barriers [383–385] are gaining traction. Additionally, the burgeoning field of agriphotovoltaics (AgriPV), which synergizes photovoltaic systems with agriculture [386–391], stands to greatly benefit from bifacial technologies. Initial deployments integrating PV with crop cultivation and livestock rearing have yielded promising outcomes. In this context, optical modeling and optimization are paramount for enhancing yield predictions and achieving a balance between energy production, agricultural productivity, and aesthetic considerations. Vertical bifacial PV systems facing east and west also offer the potential for more evenly distributed energy generation throughout the day and across seasons, optimizing output in the morning and evening [369, 390, 392] and boosting the energy yield during winter [393, 394].

10.4. Advances needed

In conclusion, energy yield modeling for photovoltaics is critical for accurately predicting the amount of electricity generated by solar panels over time. In the context of advancing optics for solar energy harvesting, energy yield modelling is of uttermost relevance for the following reasons:

Performance Prediction: Energy yield modeling allows scientists to accurately predict the performance of optics in solar cells/modules for a wide variety of application scenarios

(e.g. different locations, orientations, tilt angles, and weather patterns). By simulating these scenarios, scientists can make informed decisions regarding the suitability of a novel optical component, coating or device architecture for the envisaged application scenario. For example, the optimal module orientation or color of a solar module can be determined even for non-trivial application scenarios, such as building integrated photovoltaics or bifacial photovoltaics.

Device Optimization: Energy yield modeling serves as a crucial tool for researchers and developers working on advancing PV technology. By simulating the performance of novel materials, new device architectures, and emerging photovoltaic technologies, scientists can identify promising avenues for research and development to enhance the efficiency, reliability, and affordability of PV systems. A prominent recent example in this regard are the multiple energy yield studies on perovskite/silicon tandem photovoltaics that are essential to guide the research on optimizing device architectures for this technology.

Assessment of Imperfections and Failures: Energy yield modeling allows for the assessment of the actual performance of PV systems in real-world conditions. By considering factors such as device degradation, soiling, shading, unexpected weather conditions, and system losses, energy yield models provide insights into how much electricity a PV system will produce over its operational lifetime even in non-optimal installation conditions. In this regard, a very prominent research topic in the future will be in assessing the long-term performance of new PV technologies, such as perovskite-based tandem photovoltaics. However, for inclusion of long-term energy yield it is necessary to understand the optoelectronic performance of the studied devices. Thus the theoretical application of energy yield modelling heavily depends on obtaining experimental through thorough outdoor and in lab testing. Several studies have already tried to connect indoor and outdoor testing results [359, 395].

Cost-Benefit Analysis: The performance of photovoltaic (PV) systems is assessed by a variety of key performance indicators such as levelized cost of electricity (LCOE), energy payback time (EPT), emissions per kWh, or resource efficiency. For all these performance indicators, energy modeling is required to determine the lifetime energy production of a PV system under realistic conditions. In conclusion, energy yield modeling is essential for optimizing the performance, economic viability, and integration of photovoltaic systems into the energy landscape. By accurately predicting energy production and assessing the feasibility of solar projects, energy yield modeling plays a crucial role in advancing photovoltaics and in particular optics in photovoltaics.

11. Color and aesthetics of photovoltaic modules

J. C. Ortiz Lizcano, O. Isabella, B. Bläsi, M. Schmid

The construction sector is one of the most significant contributors to greenhouse gas emissions (GHG) with an estimated global share of 35% [396]. The International Energy Agency (IEA) reports that by 2060, projected population growth will require an additional 240 million square meters of built area, representing the largest increase in human history [397]. The urban environment must transition from an energy consumer to an active producer. To achieve this goal, policies around the world aim to ensure that buildings meet near-zero energy standards in the near future. For example, Europe aims to mandate zero energy housing by 2030, the United States is looking to retrofit half of its commercial building sector and transform them into net-zero projects, and similar efforts are beginning to occur in Australia, China, and Japan, to name a few [398]. Efforts toward a near-zero energy infrastructure include reducing the carbon footprint of materials used in the building sector, improving the energy performance of residences and office buildings, and the production of energy on site [399].

Installation of photovoltaic (PV) systems on site is becoming a common way to improve the energy performance of buildings. PV systems are versatile and straightforward, since their basic layout is consistent in small-, medium-, and large-scale topologies that require very moderate maintenance [400]. The implementation of photovoltaic systems in buildings is usually classified into two categories: Building-added (or attached) photovoltaics (BAPV), where the modules are installed on existing building surfaces (such as roofs), and building-integrated photovoltaics (BIPV), where PV modules act as the building envelope, replacing conventional materials used for this purpose, such as facades and skylights [345].

BIPV systems are also an excellent alternative for renewable energy production in densely populated areas where land use is limited and needs to be reserved for other human activities, such as farming and preservation. By 2022, the BIPV market was valued at USD 19.82 billion with a projected compound annual growth rate (CAGR) of 21% until 2030, reaching USD 89.80 billion [401]. Experts have highlighted the importance of incorporating BIPV projects since the design stage of new building developments, particularly considering their aesthetic appeal [402]. Shape, texture and color have been proven to be essential in accepting BIPV products, both for architects and homeowners [403] [400]. Color, in particular, has been shown to be a critical factor in adoption, brand recognition, and purchasing decisions [404]. Studies indicate that potential customers are willing to pay premium prices for a colored BIPV system, and they are preferred over standard BAPV systems based on standard dark blue and black colors [405]. Discrete integration of photovoltaic energy is essential in heritage buildings [406] [407], and stakeholders in rural and urban areas prefer to harmonize the color of photovoltaic modules with their surroundings [408]. This work summarizes the research and industrial efforts on the most commonly used coloring techniques in the production of BIPV modules. Note that these same approaches also apply to BAPV solutions.

11.1. Challenges for colored BIPV systems

The Photovoltaic Power Systems Division of the International Energy Agency (IEA PVPS Task 15) categorizes the integration of photovoltaic modules into buildings by three main functions. Roofs, facades, and external integrated devices [409]. Each of these functions can be divided into different categories of applications. For example, roofs can be divided into discontinuous, continuous, and atrium / skylights. Facade applications include rain screens, double skin, curtain walls, windows, and masonry walls. External devices can be parapets and balustrades or canopies and shading structures. One of the most challenging aspects of BIPV products is that each application has specific technical requirements. These requirements range from fire safety certification, mechanical resistance, hygrothermal performance, and electrical insulation, among

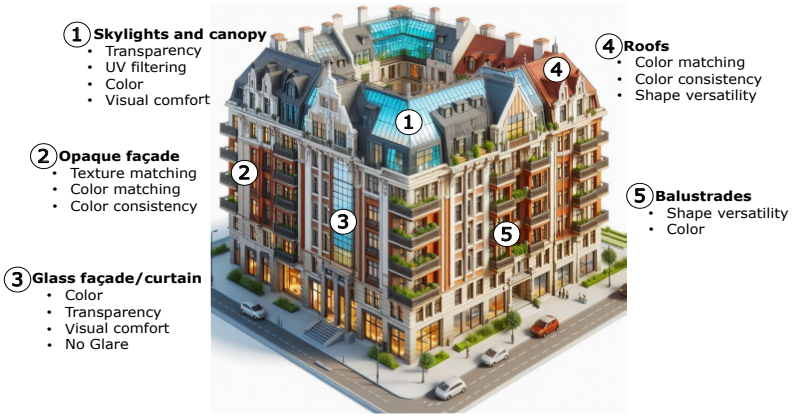


Fig. 28. Different integration applications within the building environment. **1** Skylight or canopy. **2** Opaque facade. **3** Glass facade / glass curtain. **4** Roofs. **5** Balustrades or external devices. Each application has its particular technical challenges. Image generated via Microsoft Designer – Dall·E3 image creator using the following query: *A colored 3D model of a European heritage apartment building with a portion of its roof as a glass ceiling.*

others [410]. Regarding the color appearance, Figure 28 presents the main technical requirements for BIPV modules for every integration application. Depending on their applications, color photovoltaic modules can be required to be completely opaque, such as when replacing masonry facades, roofs, and specific external devices, or they can require certain levels of transparency.

For the case of opaque photovoltaic modules, one of the main requirements is to conceal its active area and mimic a wide variety of colors commonly used in the construction sector, such as those defined by the RAL system [411]. Color matching is essential for renovation projects that involve heritage buildings, where the aesthetic of the building must be maintained [412]. If photovoltaic modules replace masonry, architects are reluctant to implement them due to their glass-pane appearance and feel, so trying to match the texture of the material is important for this application [413]. The replacement of large facades and roofs can involve the use of a large number of photovoltaic modules, making color consistency essential. The coloring technique must ensure color stability at different observation angles and a reliable manufacturing process, ensuring minimal discrepancies between modules. The availability of bright colors is also preferred by architects and consumers, but glare should be avoided as it reduces visual comfort and can become a safety hazard [414].

Integrating photovoltaics into canopies, skylights, glass facades, and fenestration requires semitransparency that ensures external and internal visual comfort. Internal visual comfort is estimated based on the color temperature and the color rendering index of the incoming ambient light [415]. This requirement represents an additional challenge for the photovoltaic module that replaces the glass structure and any color module whose reflectance can affect its surroundings.

The manufacturing techniques used to produce color photovoltaics must meet the abovementioned requirements and be easily scalable and economically feasible for their market to reach terawatt scales of production. Moreover, the produced color must have a reliability equivalent to or superior to that of the photovoltaic module. BIPV products must have lifetimes similar to the building materials they replace, so the coloring technique should not interfere with this objective by producing colors that change or fade after a few years.

The technological and economic evaluation of a BIPV system requires a complete understanding of the expected electrical performance, the available financial incentives, the social and

environmental benefits, and other regulatory frameworks required for its installation. Gholami *et al*. [416] found that a life cycle analysis evaluation that considers this demonstrates that BIPV systems can become economically feasible. The authors expanded the methodology from the European scenario [417] to other places, such as Brazil, China, and Bahrain, obtaining similar conclusions. From a performance perspective, Zimmerman *et al*. [418] found that module efficiency and lifetime were critical parameters to verify whether a vertically mounted photovoltaic system could achieve levelized cost of electricity (LCOE) values similar to grid prices in the US.

Understanding the effect of coloring a photovoltaic device requires a combination of colorimetry, optical, and electrical models. Human color perception of a non-luminous object is modeled based on the CIE standard observer [419], which quantifies the chromatic response of human vision [420] [421] to stimuli from a given light source and the observed object reflectance. The result of these calculations is the three-dimensional XYZ color space, which is the basis for deriving various alternatives using transformation matrices [422]. The most commonly used color spaces are sRGB, CIE La * b *, and Hue, Chroma, and Luminosity (HCL). The last one is beneficial, as it is the basis of the formula for color difference [423]. This factor denoted ΔE_{00}, quantifies the difference between two colors and represents a valuable figure of merit for the validation of computational models and the analysis of color consistency. Theoretically, studies have estimated the maximum efficiency achievable in a colored photovoltaic device. Peharz and Ulm [411] and Halme and Mäkinen [424], for example, calculated that colors can induce relative power losses between 5% - 20 % compared to a perfectly absorbing device. Both authors concluded that the most impactful colorimetry parameter is the luminosity (brightness) of the color, and the most impacted performance parameter was the photogenerated current on the solar cells due to the reflectance loss needed to provide color.

The main challenge in modeling the electric yield of color BIPV systems is to accurately calculate the irradiance that effectively reaches the solar cells. Since the relationship between the output power of a photovoltaic module is nearly linear with the irradiance it receives, inaccuracies in estimating this parameter can lead to important errors in the obtained energy yield. Although several studies have focused on finding ways to reliably estimate this power output under the complex surrounding conditions of urban installations for standard modules [425–429], the same is not currently available for color modules. The additional reflectance loss and its spectral dependence on the coloring technique increases the complexity of accurately estimating the expected electrical efficiency. Furthermore, coloring a photovoltaic module has the potential to reduce its operating temperature [430], which can have a significant impact on its reliability [431]. A modeling tool that considers color perception, color stability, accurate energy yield, accurate operating temperature, and expected lifetime is instrumental to studying the feasibility of color BIPV products.

11.2. Approaches for coloring BIPV products

Several techniques have been developed to provide color to photovoltaic modules. This chapter presents the techniques that have reached, or have the potential of reaching, large-scale production. Substantial information on all different coloring approaches can be found in the review works by Meddeb *et al*. [432], Sehati *et al*. [433], Basher *et al*. [400], and Li *et al*. [434].

In practice, the coloration of photovoltaic modules is done using a wide variety of techniques. These techniques can be applied directly to the solar cells or at the module level by adding or coloring a layer of the photovoltaic module, such as the front glass, the encapsulant, or the back sheet. Examples of these different levels of application are found in the work of Pelle *et al*. [435], Kutter *et al*. [436], and Lisco *et al*. [437].

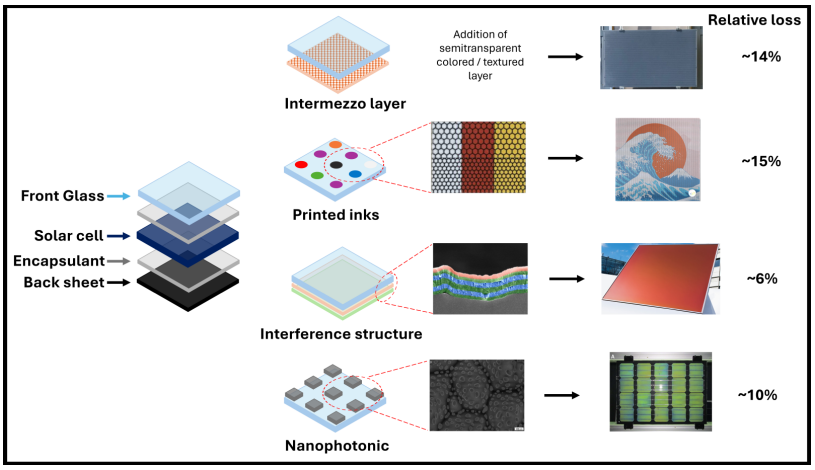


Fig. 29. Coloring techniques for opaque photovoltaic modules. These techniques aim at concealing the active area (solar cells). From top to bottom: Color textiles or layers can be added to any of the front layers of the module to change its color appearance (Photograph used with permission of The Institute of Electrical and Electronics Engineers, Incorporated (IEEE), from Ref. [438]; permission conveyed through Copyright Clearance Center, Inc.). Digitally printed inks (Photographs reprinted with permission from Kameleon Solar [439]). Interference structures that selectively reflect light via interference effects. (Image and photograph reprinted form Ref. [440]). Nanostructures that produce wavelength specific light scattering (Photographs reprinted from Ref. [441] with permission from Elsevier). The last column indicates the reported average relative efficiency loss compared to a standard photovoltaic module.

11.2.1. Opaque photovoltaic modules

For opaque photovoltaic modules, four techniques have industrial terawatt-scale potential given their large-area feasibility, high industrial throughput, and minimal impact on the standard manufacturing process of solar cells and photovoltaic modules. These techniques are summarized in Fig. 29 and are presented starting from those based on readily available industrial methods to those with potential for industrial production.

***Intermezzo* or added color layer** Refers to retrofitting existing commercial photovoltaic modules to change their color. These approaches are based on techniques available in other industrial sectors, but are tailored to photovoltaic modules. An example is presented by Gewohn *et al.* [438], who developed imprinted textiles that can be laminated to existing photovoltaic modules via an inkjet hybrid printer using a halftone technique. The results show that the technique can effectively change the color of a standard PV module with current losses in the range of 15%.

Another example of intermezzo layering is the work of Morlier *et al.* [413] which proposes a way to provide standard photovoltaic modules with the look and feel of stone veneer sheets using different stone laminates. The main drawback of this method is its significant power loss. Relative losses for stone-shaped samples ranged from 47% to 76%. However, the successful integration of these aesthetic options is a promising starting point for future research.

Masuda et al. [442] carried out experiments to understand the feasibility of using automotive paints in photovoltaic modules. The aim was to investigate which of the best painting techniques commonly used in the automotive industry was suitable for manufacturing potential lightweight photovoltaic modules. The study concluded that mica pigments could confer a rich color to the module while maintaining a relatively high level of light transmittance, with relative efficiency losses around 20%.

Microscopic ink patterns on the front glass consists of creating patterns (like dots or hexagons) separated in such a way that, at a distance, it is impossible to discern by the human eye. Basher *et al*. [443] present a concept that consists of creating a 50 μm separated dot pattern printed on glass using a UV-sensitive white ink (UV-curable technique). The area of glass covered by the ink transmits light within the UV and near-infrared (NIR) regions, while the gaps transmit the whole light spectrum. The result, from a distance, is a fully concealed photovoltaic module. Shin *et al*. [444] tested the screen printing method to create single-color photovoltaic modules. The technique prints the dotted pattern directly onto low iron glass and then fires it at high temperature to ensure adhesion. Riedel *et al*. [445] found that for ceramic inks applied via digital printing, the optical and electrical performance was almost independent of the geometry of the microscopic pattern. The aesthetic potential of this technique is essentially limitless, since any high-resolution image can be used to create any design of the photovoltaic module. The most commonly used techniques to apply color, silk screen printing, digital UV-printing and digital ceramic ink printing, all reach industrial scale status for large-scale production. In addition, digital ceramic ink printing has proven reliability. Kameleon Solar, for example, claims that this technique provides coloring with a useful life of close to fifty years [439].

Despite its aesthetic potential, the colors obtained through this technique have comparatively limited saturation values [436]. Furthermore, the absorptive nature of inks can produce significant relative losses, some colors almost halving the electrical output [445]. Modeling the impact of this technique is time consuming and complex, and care must be taken in the design of the pattern as excessive irradiance inhomogeinity on the solar cells can lead to performance and reliability problems.

Interference structures (IS) are one of the most studied techniques for coloring photovoltaic modules. These devices offer the advantage of producing color without absorbing dyes, thus reducing unnecessary optical losses. Additionally, color saturation can be maximized by creating reflectance spectra that can be similar to those of a monochromatic source. They are manufactured by depositing thin dielectric layers in a given sequence (alternating high and low refractive indices). The width of reflectance around the created peak depends to some extent on the difference in the refractive index of the materials used [446]. Macleod [447] provides an in-depth mathematical approach to the engineering possibilities of these optical systems.

The materials most commonly used, given their suitable optical properties, are titanium dioxide TiO_2, silicon nitride SiN_x, silicon dioxide SiO_2, and magnesium flouride MgF_2. Soman and Antony [448], Røyset *et al*. [449], Wessels *et al*. [450], Ingenito *et al.* [451], Ortiz Lizcano *et al*. [430], and Bläsi *et al*. [440] present comprehensive examples of the aesthetic potential of this approach. Furthermore, this approach has reached commercial status, due to manufacturing techniques readily available within the photovoltaic industry, such as sputtering and atomic layer deposition. Products such as those offered by LOF Solar [452], Soluxa [453], Kromatrix™ [454], and Megasol [455] are based on this technique. Similarly to the case of nanostructures, the relative losses reported using this technique are among the lowest. Bright colors can have relative losses as low as 5%.

One of the main drawbacks of ISs is poor color stabilization and the potential to create significant glare. However, several studies have provided approaches to ameliorate these obstacles. Stabilizing color perception at different angles of observation represents an essential challenge for these devices. Bläsi *et al*. proposed the deposition of these optical systems on textured glass surfaces. This layout creates a 3D interference structure named MorphoColor [440], which improves the stability of the color at different angles of observation. Furthermore, the use of second-harmonic designs made with materials with a high refractive index (such as TiO_2) can help create bright and stable colors. Similarly, a glass-based texturization layout with inverted pyramids on the front side and random texturing on the back, where the structure is deposited, provides excellent color stability for observation angles up to 80° [430]. Jolissaint *et al*. [456] also

provide insight into how texturing the front glass helps reduce unwanted glare effects and helps conceal the solar cells.The above-mentioned works are only a few examples of approaches to coloring photovoltaic modules based on ISs; other contributions using this approach are Rudzikas *et al*. [457] and Xu *et al*. [458].

Nanostructures exploit the effects of wavelength-specific light absorption and scattering and have been shown to be successful in the coloration of photovoltaic devices and modules. Perharz *et al*. [441] demonstrated the potential of this technique by applying metallic nanoparticle structures based on silver (Ag). The authors deposited thin Ag films on a commercial monocrystalline surface using DC sputtering, followed by an annealing process at 300 °C, thus creating a coating based on Ag nanoparticles. The second row of Fig. 29 presents scanning electron microscope images of Ag nanoparticles deposited on the surface of the pyramidal-textured solar cell with sizes ranging from 50 to 150 nm. These nanoparticles create plasmonic scattering that produces a reflectance peak at 500 nm. This shift in reflectance changes the perceived color from blue to green.

Similarly, Neder *et al*. [459] demonstrated that green colors could be produced by using c-Si nanocylinders that scatter light at a wavelength value around 540 nm. Other colors have also been proven by Uleman *et al*. [460] with the design of semitransparent meta-grating based on silicon nanowires. The layout allowed control of light scattering over a wide range of angles by modulating the pitch of the structures, the final design provided a red, matte appearance that emulates roof materials. Zhou *et al.* [461] also studied the aesthetic potential of using a poly (methyl methacrylate) matrix that contains nanoparticles based on $Si-SiO_2$ core shells. In general, the reported relative efficiency losses of nano-structural approaches ranged from 2% [462] to 13% [460]

The use of metal-based nanostructures has the disadvantage of inducing absorptive losses that hinder the electrical output of the photovoltaic module; however, alternative dielectric-based structures could reduce this problem. The main advantage of this approach is its unique ability to modulate light in a wavelength-dependent manner using a single layer. In this respect, the fundamental principles of obtaining colors using these structures is well known, [463] as it is their application in photovoltaic devices [59]. However, to date, only single-module demonstrators or small area devices have been showcased. The technique is still in its infancy when it comes to mass production, with no clear method that could be translated into a large area, reliable, and cost-effective industrial application. However, some recent approaches, such as that presented by Das Gupta *et al.* [464], offer promising results in terms of versatility and potential scalability.

11.2.2. Semi-transparent photovoltaic modules

For integration layouts that require transparency, such as glass facades, skylights, and canopies, thin-film-based photovoltaic modules have reached a significant level of maturity at the industrial level. The same approaches discussed for opaque photovoltaic modules can be applied to provide color to semitransparent modules. As stated in the previous section, the challenge is to provide the transmitted spectra required according to the application. For indoor office lighting, semitransparency and color must comply with health and safety requirements [415]. In applications such as agrivoltaic systems, the quality and nature of the incoming light spectra can affect the quality and growth of the produce [465]. This means that the design of the product must consider both color transmittance and color reflectance. Kim *et al*. [466] demonstrate that nanostructures made with SiO_2 and TiO_2 in hexagonal patterns can create colorful CIGS solar cells. Yoo *et al*. [467] presented coloring concepts for CIGS solar modules based on a triple layer photonic crystal made with SiO_2 and TiO_2. The authors focused on semitransparent modules and presented designs for a blue, yellow, and red photovoltaic module for window applications.

Amorphous silicon (a-Si:H) is an extremely versatile technology with respect to customized modules with different levels of transparency. Lee *et al*. [468] created semi-transparent colored

solar cells based on thin films of a-Si:H and cuprite Cu_2O. Myong and Jeon [469] discuss ways to produce colored and semitransparent glass-to-glass (GTG) photovoltaic modules based on a-Si:H solar cells, including the use of colored materials for encapsulation and transparent contacts. Given the transparency achievable in solar cell fabrication, the colored layer is placed on the back side of the active area, thus avoiding optical losses. Neugebohrn et al. [470] focused on the use of oxide-metal oxide stacks made of aluminum-doped zinc oxide ZnO:Al and silver in $Cu(In, Ga)Se_2$ solar cells. Adjusting the physical properties of this stack changed the color produced.

Products based on this solar cell technology have an outstanding level of maturity and development. Onyx Solar [471] is one of the largest BIPV manufacturers in the world, with a significant portfolio of projects, many of which are based on semitransparent and even colored a-Si:H photovoltaic glass. Their main drawback, compared to potential new alternatives (semi-transparent c-Si-based products, perovskite approaches), is their lower power conversion efficiency, which, depending on their level of transparency, can range between 4% and 10%.

11.3. Advances needed to meet future challenges

In general, a wide range of coloring techniques have reached industrial-scale technological readiness. For example, products based on microscopic ink patterns and interference structures are now readily available with all the necessary conditions to evolve into a terawatt-level market. Nanophotonic structures, on the contrary, still need significant technical development to reach this same status, but their advantage of wavelength modulation with only one applied layer represents a promising approach for industrial applications. Other approaches using add-on layers (here called *intermezzo*) use established industrial processes and have the potential for rapid implementation. In general, the aesthetic potential and versatility of all these combined techniques offer unlimited design options to architects and customers.

Furthermore, color photovoltaic products can be produced with considerable electrical efficiency. Colors based on interference structures can induce relative losses well below 10%. Methods using nanophotonic structures have reported relative losses close to 10%. Other approaches, such as microscopic ink patterns and added color layers, result in higher losses. However, with c-Si modules reaching higher efficiencies, there is still the possibility of producing modules with all the techniques mentioned above with electrical efficiencies close to or above 20%.

However, some barriers remain. Pelle *et al*. [435] has highlighted the need for more comprehensive and accurate models for color BIPV modules. The main challenge is that the modeling needed usually requires detailed optical characterization of all the layers within the module. Any change in the layout or properties of these materials can produce a change in the behavior of the final product. For interference structures, modeling textured surfaces usually requires a complex combination of ray tracing techniques [256, 472–474] and models based on the transfer matrix method [450, 475]. A change in the textured pattern implies a reconfiguration of the model input. Additionally, useful optmization algorithms that could reduce unwanted optical losses, such as the needle technique [476], are not yet available when working on texture surfaces with roughness in micrometers. For the case of ceramic inks, the transmittance of each of the materials and dyes used must be characterized to estimate their induced optical loss. Comprehensive CAD tools that address these aspects could reduce the time and costs required to develop new products.

More modeling efforts are needed to include the impact that any coloring technique can have on the operating temperature of a photovoltaic module. The published performance loss is usually estimated under laboratory conditions, where temperature effects are not taken into account. This may lead to an underestimation not only of the power output of a color photovoltaic module but also of its potential lifetime, both extremely important parameters in life-cycle and LCOE

analysis.

It is also important that researches and industry agree on a standard way of assessing color matching and color stability, particularly for applications in which these aspects are critical, such as heritage buildings or seamless integration into open environments. Some works utilize the CIEDE2000 color difference standard ΔE_{00}, which is defined in the HCL color space, while others use the CIE76 color difference standard ΔE_{76}, based on CIELAB. There are important differences between these two approaches, especially in terms of perceptual uniformity. Standardizing these approaches, as well as the limiting values of perceived color differences according to different hues, is essential to guarantee excellence in the final product. In this sense, Borja Block *et al*. [477] proposes the use of an innovative large area colorimeter that allows to accurately characterize the color of BIPV products.

Data sheets for color BIPV products should be more oriented toward the building sector. The performance of a given BIPV product will depend on the layout of the installation. Information about expected performance in different orientations and integration layouts could be beneficial to their marketing. For example, a company that offers substantial information for a preliminary feasibility study is Onyx Solar [478]. Based on their experience, they developed a tool that allows potential users to estimate the environmental and economic benefit, per meter squared, of the implementation of any of their solutions. This can be assessed for two different module technologies (c-Si and a-Si:H) for four different types of orientation. These initiatives are key in generating better engagement with end users.

12. Conclusion

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In this article, we presented a selection of optical research topics that we currently, as of late 2024, consider to be crucial for the further expansion of photovoltaics on a terawatt scale. We were guided by the question:

> *Where can innovative optical concepts be used to accelerate the further expansion of photovoltaics and thus the transformation of the energy system?*

We started with two chapters that summarized the current state of photovoltaics and classic light management concepts in solar cells. Based on the challenges identified to promote the expansion of photovoltaics, we addressed the following optical research topics in the subsequent chapters: The development of eco-friendly and earth-abundant optical materials enabling the sustainable production of photovoltaic cells on terawatt scale. With the aim of achieving higher power conversion efficiencies, we selected the topics luminescent processes in the solar cells, the optics of multi-junction solar cells and spectral shaping. For an extension of the module lifetime and a maximization of energy yield, we discussed the topics thermal management and accurate energy yield predictions. Finally, we treated the importance of color and an aesthetic appearance of the modules aiming at a broad social acceptance of photovoltaics in the built environment. At the end of each chapter we identified optical advances that need to be addressed in the coming years.

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Tristan Gageot is a physics researcher working at CEA, the French Alternative Energies and Atomic Energy Commission (CEA), Le Bourget-du-Lac, France. He received the Ph.D. degree in Material Science at the Grenoble Alpes University (UGA), France, in 2024. Since then, he has been working on the PECVD processes for silicon heterojunction solar cells.

Ivan Gordon obtained his Ph.D. from the University of Leuven, Belgium, in February 2002. He started to work in the field of photovoltaics in June 2003 at IMEC, Leuven, Belgium. Currently, he is director of the IMOMEC department of IMEC, and vice-director of the Institute of Material Research (IMO) of Hasselt University, Belgium. Next to this, he is also part-time professor in Digital Photovoltaics at Delft University of Technology, the Netherlands, and Editor-in-Chief of the international scientific journal Solar Energy Materials and Solar Cells. Since January 2016, he is the coordinator of the joint program on Photovoltaics of the European Energy Research Alliance (EERA) and a steering committee member of the European Technology and Innovation Platform Photovoltaics (ETIP-PV).

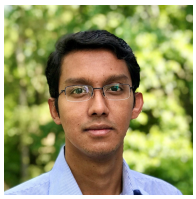
Henning Helmers studied physics and philosophy in Oldenburg, Germany and in Lund, Sweden. He received his Ph.D. from University of Oldenburg in 2013. Since 2019, he is the Deputy Head of Department "III-V Photovoltaics and Concentrator Technology." His research interests include high efficiency device design for III-V solar cells and photonic power converters, multi-junction device architectures, micro-concentrating photovoltaics (CPV), and power-by-light technology. He is co-chairing SPIE Photonics West 2025: Physics, Simulation, and Photonic Engineering of Photovoltaic Devices XIV.

Oliver Höhn received his Ph.D. degree in physics in 2015 from Albert-Ludwigs-University, Freiburg, Germany. He joined the Fraunhofer Institute for Solar Energy Systems ISE, Freiburg, Germany, in 2008. There, he has been head of the group "III-V semiconductor technology" since 2022. In December 2023, he received an ERC Consolidator Grant and thus started a group at University Freiburg to work on ultrathin III-V tandem solar cells. His main research interests include III–V multi-junction solar cells, optical modeling and realization of micro- and nanostructured surfaces and optical modeling of high efficiency solar cells.

Olindo Isabella (prof. dr. ir.) graduated in electronic engineering from University of Naples Federico II, Naples, Italy. He holds a Ph.D. degree (cum laude) on advanced light management applied to thin-film silicon solar cells from Delft University of Technology, the Netherlands. He was a visiting researcher at AIST, Tsukuba, Japan, working on plasma conditions for stable thin-film solar cells based on silicon-germanium. Since 2012 his research focuses on crystalline silicon solar cells and related applications up to system level. From materials science, to devices and systems, he has interest in multi-scale modelling with several works specialized on PV modules modelling and distributed PV systems in the urban environment. Since 2019 he leads the Photovoltaic Materials and Devices group at Delft University of Technology and he is there full professor since 2021.

Marko Jošt received his Ph.D. from the University of Ljubljana, Slovenia, and Technical University of Berlin, Germany, in 2017. Between 2017 and 2020, he was employed as a postdoctoral researcher at the Helmholtz-Zentrum Berlin, Germany, developing perovskite-based tandem solar cells. Since 2020, he is employed as an assistant professor at the Faculty of Electrical Engineering, University of Ljubljana. He continues to research perovskite solar cells in the LPVO laboratory, with the aim of improving the stability of long-term operation under realistic external conditions.

Martin Ledinský received his Ph.D. in 2009 from Charles University in Prague, Czech Republic. Following his doctoral studies, he undertook a postdoctoral fellowship at EPFL's Photovoltaics and Thin Film Electronics Laboratory (PV-LAB) in Neuchâtel, Switzerland (2013–2014), and completed a research stay at KAUST, Saudi Arabia (February–April 2018). Since 2018, he is leading the Thin Films for Photovoltaics group at the Institute of Physics of the Czech Academy of Sciences (FZU) in Prague, Czech Republic. His primary expertise is in the optical characterization of active photovoltaic materials and their passivation. Additionally, he is dedicated to the popularization of photovoltaics and physics in general, regularly giving lectures for audiences ranging from preschool to university students.



Jyotirmoy Mandal is an assistant professor in the Department of Civil and Environmental Engineering at Princeton University, Princeton, New Jersey, U.S.A. His research involves understanding and controlling nano-to-macro-scale radiative heat flows in both natural environments and artificial surfaces, with characterizing and mitigating ambient heat in a warming world as a guiding theme.

Phillip Manley obtained a Masters in Physics from Durham University, U.K., in 2012 and a doctorate in Physics at the Free University Berlin, Germanny, in 2016. He was employed as a post-doc at the Helmholtz Zentrum Berlin, Germany, from 2017 until 2021. Since then, he has worked as a senior research scientist at JCMwave GmbH, Berlin, Germany. His research focuses on modelling nano structuring for high efficiency optical devices.

Delfina Muñoz is strategic project manager and senior researcher in the solar energy department at CEA-LITEN, Le Bourget-du-Lac, France. She is industrial engineer and holds a Ph.D. in photovoltaics from Universidad Politécnica de Cataluña, Barcelona, Spain. She has more than 60 publications and more than 100 conference presentations, mostly in science and materials for PV. She is in the Board of the Chilean ATAMOSTEC project related to reliability of PV in desert areas, in the steering committee of the heterojunction and tandemPV workshops, and topic organizer of WCPC, PVSEC and IEEE conferences. Since 2019, she is in the steering committee of the European Technology and Innovation Platform Photovoltaics (ETIP-PV). She still combines project activity with the laboratory research, directing Ph.D. students and developing the next generation of photovoltaic technology.

Zunaid Omair is currently a product engineer at Lam Research, Fremont, California, U.S.A., where he focuses on new hw concepts for high aspect ratio dielectric etch. He obtained his M.Sc. (2020) and Ph.D. (2021) from the University of California, Berkeley, California, U.S.A., and performed postdoctoral research at Stanford University (2021-2022), Stanford, California, U.S.A. He has previously worked on designing coherent and incoherent imaging systems for extreme ultraviolet lithography, optical design, and imaging system development.

Juan Camilo Ortiz Lizcano received a B.Sc. degree in mechanical engineering at the Universidad Industrial de Santander, Colombia, and worked as an engineer in the field of natural gas compression. Afterwards, he decided to continue his studies at Delft University of Technology, the Netherlands, where he obtained an M.Sc. degree in Sustainable Energy Technology. In mid-2017, he started his Ph.D. studies in performance modeling of innovative concepts for integrating PV systems into the urban environment at Delft University of Technology. Currently, he works as a researcher on the design and technical implementation of photovoltaic systems to energize The Green Village.

Ulrich W. Paetzold is a Professor at the Karlsruhe Institute of Technology (KIT), Germany, where he leads the research division "Next Generation Photovoltaics" at the Institute of Microstructure Technology and the Light Technology Institute. He was a doctoral student at Forschungszentrum Jülich, Germany, and received his Ph.D. in physics from RWTH Aachen University, Aachen, Germany, in 2013, then continued as a postdoc at imec in Leuven, Belgium. In 2016, he joined the Karlsruhe Institute of Technology (KIT) and started to build-up his research group. His team's research is focused on the fabrication, upscaling, characterization, and understanding of device physics of perovskite photovoltaics and perovskite-based tandem photovoltaics. In 2023, Ulrich W. Paetzold was awarded the prestigious ERC Consolidator Grand by the European Union. In the next five years, his ambition is to advance the stability and scalability of perovskite-based (tandem) photovoltaics.

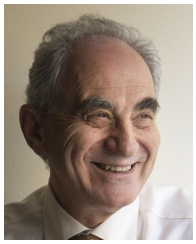
Aaswath P. Raman is an Associate Professor of Materials Science and Engineering at the University of California, Los Angeles. His research interests include radiative cooling, nanophotonics and energy systems more generally. He is known for first demonstrating daytime radiative cooling in 2014, as well as radiative cooling's use for solar cells in subsequent work. He received his Ph.D. in Applied Physics from Stanford University in 2013, and has received early career awards from the Materials Research Society, DARPA, NSF and MIT Technology Review. He is also co-founder and chief scientific officer of a startup commercializing daytime radiative cooling technology, SkyCool Systems.

Hitoshi Sai is a Principal Senior Researcher at Renewable Energy Research Center in National Institute of Advanced Industrial Science and Technology (AIST), Japan, and a visiting professor at Tsukuba University. He received the Ph.D. degree in mechanical engineering from Tohoku University, Sendai, Japan, in 2004. He joined Toyota Technological Institute, Nagoya, Japan, in 2004 as a JSPS post-doctoral fellow for PV device research. In 2007, he joined AIST. Since then, he has worked for developing thin-film silicon, crystalline silicon solar cells, and tandem cells, with a great interest in light management.

Rebecca Saive is a Professor of Applied Physics at the University of Twente, the Netherlands. Her research focuses on advanced light management techniques for photovoltaic systems, such as photonic metamaterials for enhanced light collection and effectively transparent front contacts. Prof. Saive's work bridges fundamental physics and applied technology, from computational modeling to prototyping. Furthermore, her group develops novel micromanufacturing techniques and advances optoelectronic scanning probe microscopy. Prof. Saive earned her Ph.D. from the University of Heidelberg, Germany, and completed postdoctoral research at the California Institute of Technology, Pasadena, California,

U.S.A. She co-founded a successful startup in the semiconductor sector and was named one of the Innovators Under 35 Europe and Global by MIT Technology Review in recognition of her contributions to solar energy.

Martina Schmid is a Professor of Experimental Physics and Head of the MultioptiX group at the University of Duisburg-Essen, Germany, since 2017. Before, she was a Junior Professor at the Freie University Berlin (FUB), Germany, and Head of a Helmholtz Young Investigator Group at the Helmholtz-Zentrum Berlin für Materialien und Energie, Germany (since 2013/2012). She pursued postdoctoral research at the California Institute of Technology, Pasadena, California, U.S.A., and the University of Ljubljana, Slovenia. During her Ph.D., which she obtained from FUB in 2010, she also spent a research stay at the University of New South Wales, Australia. Her major research interest is resource-efficient energy conversion including multi-optical concepts for tailored light guiding and concentration.



Eli Yablonovitch is Professor in the Graduate School, Electrical Engineering & Computer Sciences Dept., University of California, Berkeley, California, U.S.A. He introduced the idea that strained semiconductor lasers could have superior performance due to reduced effective mass (holes). With almost every human interaction with the internet, optical telecommunication occurs by strained semiconductor lasers. In his photovoltaic research, Yablonovitch introduced the $4n^2$ ("Yablonovitch Limit") light-trapping factor, in worldwide use for almost all commercial solar panels. His mantra "a great solar cell also needs to be a great LED", holds the world record for solar cell efficiency, 29.1% at 1 sun. He was elected to NAE, NAS, NAI, AmAcArSci, and as Foreign Member, UK Royal Society.

Christiane Becker is head of the department *Optics for Solar Energy* at Helmholtz Zentrum Berlin für Materialien und Energie (HZB), Germany, and Professor at Hochschule für Technik und Wirtschaft Berlin, Germany. Before, she was a Young Investigator Group Leader at HZB (since 2013) and a guest scientist at University of Lund, NanoLund, Sweden, in 2017. She received her Ph.D. from Karlsruhe Institute of Technology, Germany, in 2006. Her current research interests are the optics of perovskite multi-junction solar cells, concepts to improve the aesthetic appearance of solar modules, and energy yield calculations.